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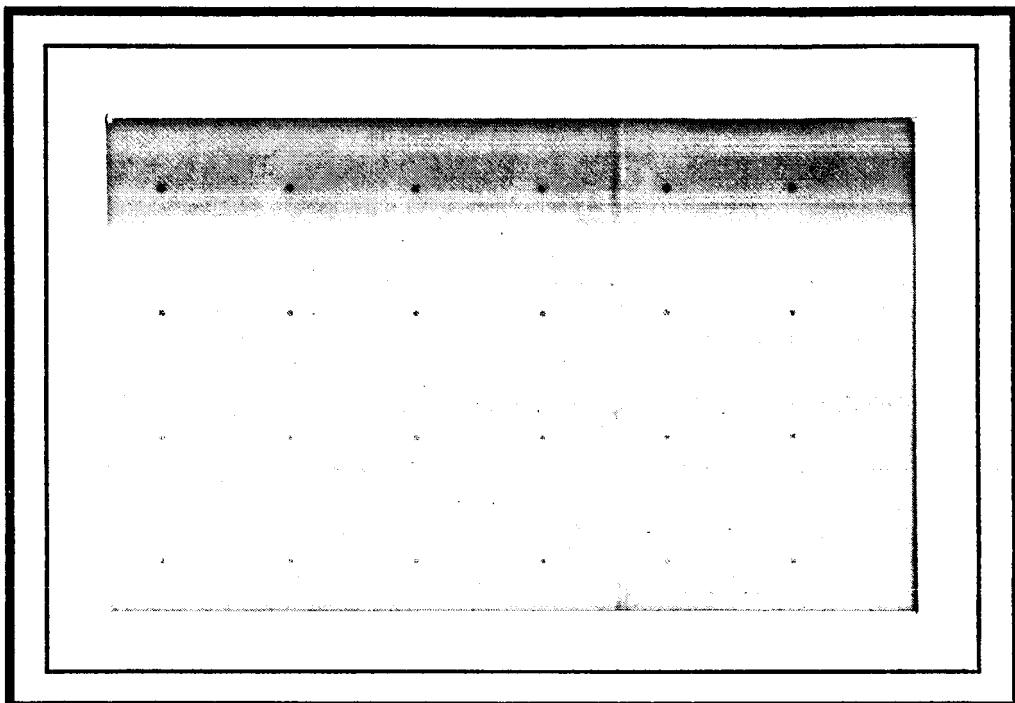
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DESIGN SENSITIVITY ANALYSIS WITH APPLICON
IFAD USING THE ADJOINT VARIABLE METHOD

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ABSTRACT

A numerical method is presented to implement structural design sensitivity analysis using the versatility and convenience of existing finite element structural analysis program and the theoretical foundation in structural design sensitivity analysis. Conventional design variables, such as thickness and cross-sectional areas, are considered. Structural performance functionals considered include compliance, displacement, and stress. It is shown that calculations can be carried out outside existing finite element codes, using postprocessing data only. That is, design sensitivity analysis software does not have to be imbedded in an existing finite element code.

The finite element structural analysis program used in the implementation presented is IFAD. Feasibility of the method is shown through analysis of several problems, including built-up structures. Accurate design sensitivity results are obtained without the uncertainty of numerical accuracy associated with selection of a finite difference perturbation.

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LIST OF SYMBOLS

| | |
|---------------------------|---|
| a_u | Bilinear form which is dependent on u |
| ℓ_u | Load linear form which is dependent on u |
| u | Design vector |
| ℓ | Design sensitivity vector; Gauss quadrature counter; Local coordinate system of a beam |
| ψ, ψ_i | Various constraint functionals |
| ψ', ψ'_i | Design sensitivities of various constraint functionals |
| δu | Perturbed design vector |
| h | Thickness of membrane; height of beam |
| t | Thickness of bending plate |
| b | Width of beam |
| E | Young's modulus |
| ν | Poisson's ratio |
| $\hat{D}(u)$ | Flexural rigidity of plate |
| J | Torsional rigidity of beam; determinant of the Jacobian |
| W, W_ℓ | Gauss quadrature weight factor |
| G | Shear modulus |
| $\hat{\delta}$ | Kronecker Delta |
| ϵ, ϵ^{ij} | Strain |
| σ, σ^{ij} | Stress |
| $\lambda, \lambda^{(i)}$ | Adjoint variable vector |
| Ω | Domain of the system considered |

| | |
|--|--|
| Γ | Boundary of the system considered |
| \sum | Summation |
| z, z^i, z_λ^i | Displacement |
| F, F^i, F_λ^i | Applied body force |
| T, T^i | Applied traction |
| \bar{z}, \bar{z}^i | Virtual displacement |
| δh | Perturbation of h |
| δb | Perturbation of b |
| δt | Perturbation of t |
| m_p | Characteristic function |
| ∂ | Partial derivative |
| [] | Matrix |
| \bar{d} | Virtual displacement of an element |
| $z_{ii}, z_{xx}, z_{xx_\lambda}$ | Beam curvature due to z |
| $\bar{z}_{xx}, \bar{z}_{ii}$ | Beam curvature due to \bar{z} |
| k | Element counter |
| γ | Material density |
| $\bar{\lambda}_{xx}, \lambda_{xx_\lambda}$ | Beam curavature due to $\bar{\lambda}$ |
| L | Length of a beam element |
| A | Area of a triangle |
| ϕ | General function |

CHAPTER I

INTRODUCTION

1.1 Purpose

To date there exists a wide variety of finite element structural analysis programs that are used as reliable tools for structural analysis. They give the designer pertinent information such as stresses, strains and displacements of the mechanical system being modeled. However, if this information reveals that the mechanical system does not meet specified constraint requirements, the designer must make intuitive guesses as to how to improve the design. If the mechanical system is complex, it becomes very difficult to decide what step must be taken to improve the design. There is however, substantial literature on the theory of design sensitivity analysis, which predicts the effect that structural design changes have on the performance of a mechanical system. Use of this technique has been primarily confined to papers in structural optimization literature.

The purpose of this work is to develop and implement structural design sensitivity analysis using the adjoint variable method that takes advantage of the versatility and convenience of an existing finite element structural analysis program and the theoretical foundation in structural design sensitivity analysis that is found in Ref. 1. The finite element program that will be used is IFAD [3]. It is developed

by Applicon Inc. and has been provided to the Center for Computer Aided Design for the use in this study.

In order to check the feasibility of using the design sensitivity analysis technique with IFAD, an approximation of the differential ψ' of a structural performance measure ψ is made using the finite difference method. An appropriate design perturbation δu must be selected in order to insure accuracy of the perturbation $\Delta\psi$ of the constraint functional. If δu is too small, $\Delta\psi = \psi(u + \delta u) - \psi(u)$ may be inaccurate due to loss of significant digits in the difference. On the other hand, if δu is too large, $\Delta\psi$ will be influenced by nonlinearities and the differential approximation will be inaccurate. The feasibility check procedure is outlined in the flow chart of Fig. 1. Details of the calculations of the constraint functionals, the adjoint loads, and the design sensitivity vectors for each constraint functional are described in Chapter II, for different types of finite elements. The design sensitivity ψ' of the constraint functional is the scalar product of the design sensitivity vector ℓ and the design variable perturbation vector δu . If the design variable is constant throughout the finite element model of the mechanical system, this becomes a scalar multiplication. If the design sensitivity is an accurate prediction of the performance of the mechanical system due to a design change, it should be equivalent to the difference of the constraint functionals of the two finite element models, the original and the perturbed model.

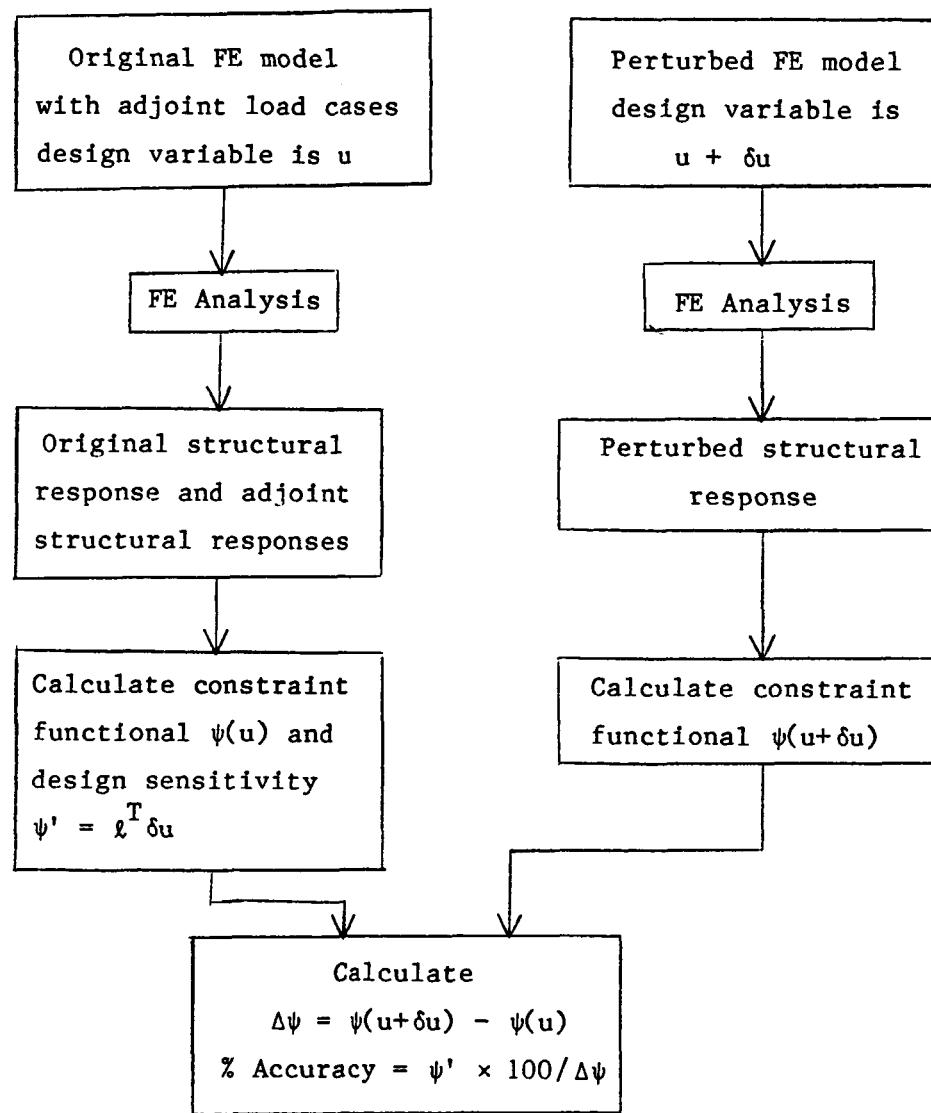


Figure 1. Flow Chart of Feasibility Check Procedure

1.2 Adjoint Variable Method

A number of methods could be used to implement structural design sensitivity analysis with an existing finite element code, but the most powerful is the adjoint variable method. This method can be implemented outside of an existing finite element code, using only postprocessing data. This is convenient, because the source code for most finite element programs is not readily available. If the code is available, less programming is involved. The same subroutines for the element shape functions used in the finite element model can be used in the design sensitivity analysis, since this method is dependent on element type. Generality is another factor that adds flexibility to the adjoint variable method. The code can be written to include basic design variables, constraints and loading conditions. This enables the designer to choose what design variables to modify to give the best design improvement.

The adjoint variable method can easily be used for complex mechanical systems that have more than one structural component. The details of this procedure are discussed in Section 2.2. Design sensitivity of a built-up structure is formed by combining the design sensitivities of each structural component. The only precaution that is necessary is in making sure that the interaction between the components is taken into account.

1.3 Adjoint Variable Method Results

The design sensitivity vector is the derivative of the constraint functional with respect to the design variables. It has the same number

of components as there are elements in the finite element model. The magnitude of each component reflects how sensitive the element is to a change in design relative to the constraint functional. If the vector component is negative, the corresponding design variable should be decreased to increase ψ . Likewise, if the vector component is positive, the design variable should be increased to increase ψ . In addition, if the magnitude of the vector component is large, then the corresponding design variable will have a more substantial effect on design improvement.

When a designer uses a finite element structural analysis in design of a mechanical system, it is most likely that a number of program runs are necessary before a substantially improved design is obtained. With the aid of a design sensitivity vector, the designer will know what direction to take to improve the design most efficiently.

CHAPTER II
DESIGN SENSITIVITY ANALYSIS METHOD

2.1 Calculation Procedure for Structural Components

To implement the adjoint variable technique of design sensitivity analysis, the adjoint load for each constraint functional must be calculated. This procedure is developed in Ref. 1 using compliance, displacement, stress and natural frequency as constraint functionals. For the compliance functional, the adjoint equation is the same as the state equation. In this special case the adjoint system does not need to be solved. For the displacement functional the adjoint load is a unit point load acting at the point where the displacement constraint is imposed. To calculate the adjoint response it is necessary only to restart the finite element analysis with unit loads applied at varying points along the structure. For the stress functional the shape function of the structural component used in the finite element analysis must be known. This shape function is used to calculate the adjoint load for a stress constraint of a specific element of the structure. From this point the procedure is similar to the displacement functional, in that a restart of the finite element analysis must be completed using the adjoint loads of elements as other load cases.

The flow chart of Fig. 2 shows the overall process. This procedure is implemented after the structural response of the finite element

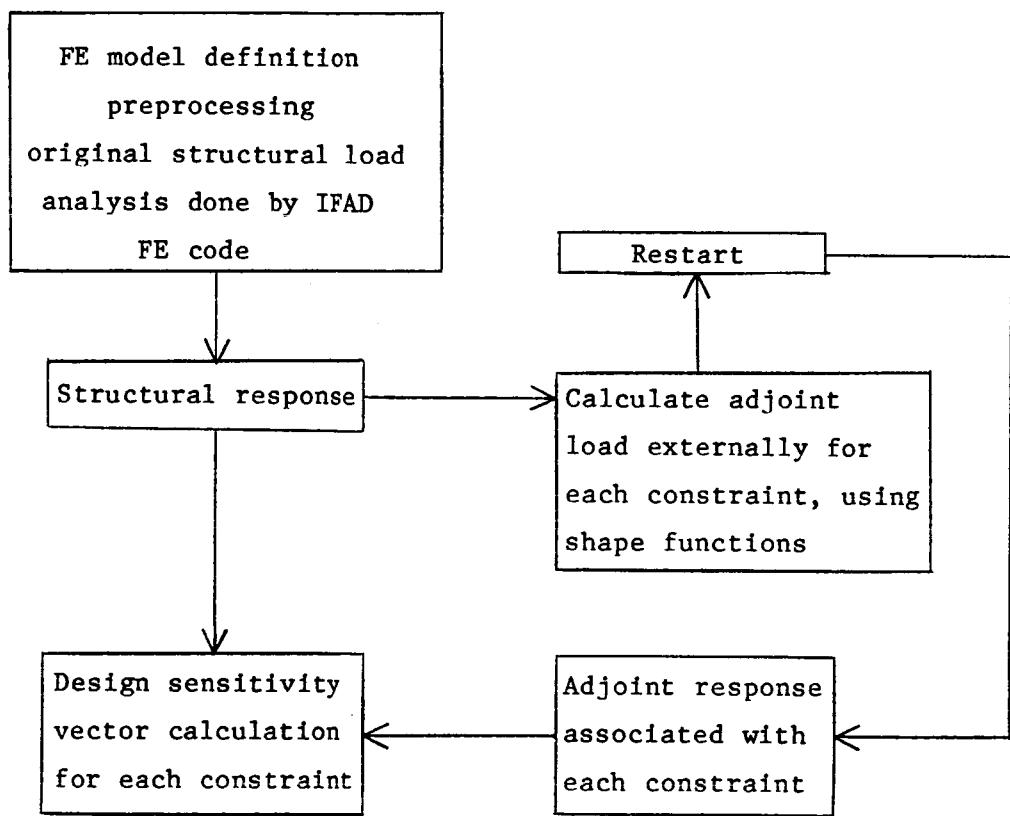


Figure 2. Flow Chart of Design Sensitivity Calculation Procedure

model due to the original load has been solved. The original structural response plus the adjoint response for each constraint is then utilized to calculate the design sensitivity vectors.

The following sections give detailed explanations of the calculation procedures and equations necessary for analyzing membranes, bending beams and bending plates.

2.1.1 Membranes

Consider a variable thickness thin elastic clamped solid, as shown in Fig. 3. The design variable is taken as the variable thickness $u = h(x)$ of the plate.

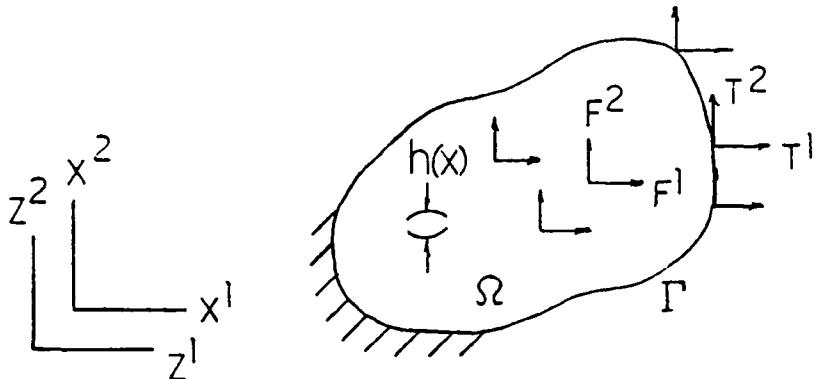


Figure 3. Clamped Elastic Solid of Variable Thickness $h(x)$

The energy bilinear form and the load linear form of the plane elasticity problem are given as [1]

$$a_u(z, \bar{z}) = \iint_{\Omega} h(x) \sum_{i,j=1}^2 \sigma^{ij}(z) \epsilon^{ij}(\bar{z}) d\Omega \quad (1)$$

and

$$\ell_u(z, \bar{z}) = \iint_{\Omega} h(x) \left[\sum_{i=1}^2 F^i z^i \right] d\Omega + \int_{\Gamma} \left[\sum_{i=1}^2 T^i z^i \right] d\Gamma \quad (2)$$

where $z = [z^1, z^2]^T$ is the displacement, $F = [F^1, F^2]^T$ is the applied body force, $T = [T^1, T^2]^T$ is the traction, and $\sigma^{ij}(z)$ and $\epsilon^{ij}(z)$ are the stress and strain fields associated with the displacement z and the virtual displacement \bar{z} respectively. The state equation is given as [1]

$$a_u(z, \bar{z}) = \ell_u(\bar{z}) \quad (3)$$

for all kinematically admissible virtual displacement \bar{z} .

First consider the functional representing the compliance of the structure as

$$\psi_1 = \iint_{\Omega} h(x) \left[\sum_{i=1}^2 F^i z^i \right] d\Omega + \int_{\Gamma} \left[\sum_{i=1}^2 T^i z^i \right] d\Gamma \quad (4)$$

The first variation of Eq. (4) is

$$\begin{aligned} \psi'_1 &= \iint_{\Omega} \left[\sum_{i=1}^2 F^i z^i \right] \delta h \, d\Omega + \iint_{\Omega} h \left[\sum_{i=1}^2 F^i z^i' \right] d\Omega \\ &\quad + \int_{\Gamma} \left[\sum_{i=1}^2 T^i z^i' \right] d\Gamma \end{aligned} \quad (5)$$

In order to eliminate the dependence on the state variable in Eq. (5), it is necessary to define the adjoint equation as [1]

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} h \left[\sum_{i=1}^2 F^i \bar{\lambda}^i \right] d\Omega + \int_{\Gamma} \left[\sum_{i=1}^2 T^i \bar{\lambda}^i \right] d\Gamma \quad (6)$$

for all kinematically admissible virtual displacement $\bar{\lambda}$. Since Eq. (6) is identical to Eq. (4) if $\lambda = z$ and $\bar{\lambda} = \bar{z}$, the adjoint equation does

not need to be solved. Using the adjoint variable method of design sensitivity analysis gives [1]

$$\begin{aligned}\psi'_1 &= \iint_{\Omega} \left[\sum_{i=1}^2 F^i z^i \right] \delta h \, d\Omega + \iint_{\Omega} \left[\sum_{i=1}^2 F^i \lambda^i - \sum_{i,j=1}^2 \sigma^{ij}(z) \epsilon^{ij}(\lambda) \right] \delta h \, d\Omega \\ &= \iint_{\Omega} \left[2 \sum_{i=1}^2 F^i z^i - \sum_{i,j=1}^2 \sigma^{ij}(z) \epsilon^{ij}(z) \right] \delta h \, d\Omega\end{aligned}\quad (7)$$

since $z = \lambda$ for the compliance functional.

To numerically integrate Eqs. (4) and (7), a two-point Gauss quadrature formula is used. The equations become

$$\psi_1 = \sum_{k=1}^N \left\{ h_k \left[\sum_{\ell=1}^2 \sum_{i=1}^2 F_{\ell}^i z_{\ell}^i W_{\ell} J + \sum_{i=1}^2 T^i z^i \right] \right\} \quad (8)$$

and

$$\psi'_1 = \sum_{k=1}^N \left\{ \sum_{\ell=1}^2 \left[\sum_{i=1}^2 2F_{\ell}^i z_{\ell}^i - \sum_{i,j=1}^2 \sigma_{\ell}^{ij}(z) \epsilon_{\ell}^{ij}(z) W_{\ell} \right] J \delta h_k \right\} \quad (9)$$

respectively, where J is the Jacobian, N is the total number of elements, subscript ℓ is the counter for the number of Gauss points, subscript k is the counter for the element number, W is the weighting constant for the ℓ th Gauss point, and superscript i is the direction of the force and the displacement.

Next consider the functional representing the displacement z at a discrete point \hat{x} as

$$\psi_2 \equiv z(\hat{x}) = \iint_{\Omega} \hat{\delta}(x - \hat{x}) z(x) \, d\Omega \quad (10)$$

where $\hat{\delta}(\mathbf{x})$ is the Dirac measure in the plane, acting at the origin. The first variation of Eq. (10) is

$$\psi_2' = \iint_{\Omega} \hat{\delta}(\mathbf{x} - \hat{\mathbf{x}}) z'(\mathbf{x}) d\Omega \quad (11)$$

The adjoint equation in this case is [1]

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} \hat{\delta}(\mathbf{x} - \hat{\mathbf{x}}) \bar{\lambda}(\mathbf{x}) d\Omega \quad (12)$$

for all kinematically admissible virtual displacement $\bar{\lambda}$. This equation has a unique solution $\lambda^{(2)}$, where $\lambda^{(2)}$ is the plate displacement due to a unit point load acting at a point $\hat{\mathbf{x}}$. Using the adjoint variable method of design sensitivity analysis gives

$$\psi_2' = \iint_{\Omega} \left[\sum_{i=1}^2 F^i \lambda^{(2)i} - \sum_{i,j=1}^2 \sigma^{ij}(z) \varepsilon^{ij}(\lambda^{(2)}) \right] \delta_h d\Omega \quad (13)$$

where $\lambda^{(2)}$ is the solution of Eq. (12).

For this constraint two equations must be solved. The adjoint load of Eq. (12) is just a unit load applied at a discrete point in the finite element model. All that is necessary is a restart of the model so that load cases of applied unit loads at various nodal points can be analyzed. The resulting strains due to the adjoint load are then used in calculating Eq. (13). Note that for each displacement constraint there is a different adjoint load.

With numerical techniques applied as in the compliance constraint case, Eq. (13) becomes

$$\psi'_2 = \sum_{k=1}^N \left\{ \sum_{\lambda=1}^2 \left[\sum_{i=1}^2 F_{\lambda}^i \lambda^{(2)i} - \sum_{i,j=1}^2 \sigma_{\lambda}^{ij}(z) \epsilon_{\lambda}^{ij}(\lambda^{(2)}) \right] w_{\lambda} \right\} J \delta h_k \quad (14)$$

Finally consider the general functional representing a locally averaged stress on an element as

$$\psi_3 = \iint_{\Omega} g(\sigma(z)) m_p d\Omega \quad (15)$$

where m_p is a characteristic function defined on a finite element Ω_p as

$$m_p = \begin{cases} \frac{1}{\int_{\Omega_p} d\Omega}, & x \in \Omega_p \\ 0, & x \notin \Omega_p \end{cases} \quad (16)$$

The first variation of Eq. (15) is

$$\psi'_3 = \iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(z') \right] m_p d\Omega \quad (17)$$

Replacing the variation in state z' by a virtual displacement $\bar{\lambda}$, the adjoint equation is obtained as [1]

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(\bar{\lambda}) \right] m_p d\Omega \quad (18)$$

for all kinematically admissible virtual displacements $\bar{\lambda}$. Eq. (18) has a unique solution for a displacement field $\lambda^{(3)}$. Using the adjoint variable method of design sensitivity analysis gives

$$\psi'_3 = \iint_{\Omega} \left[\sum_{i=1}^2 F^i \lambda^{(3)i} - \sum_{i,j=1}^2 \sigma_{\lambda}^{ij}(z) \epsilon_{\lambda}^{ij}(\lambda^{(3)}) \right] \delta h d\Omega \quad (19)$$

where $\lambda^{(3)}$ is the solution of Eq. (18).

With numerical techniques applied as in the displacement constraint case, Eqs. (15), (18), and (19) become

$$\psi_3 = \sum_{\lambda=1}^2 [g(\sigma_\lambda(z)) m_p w_\lambda] J \quad (20)$$

$$\begin{aligned} & \iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(\bar{\lambda}) \right] m_p d\Omega \\ &= \sum_{\lambda=1}^2 \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(\bar{\lambda}) \right] m_p w_\lambda J \bar{d} \end{aligned} \quad (21)$$

and

$$\psi'_3 = \sum_{k=1}^N \left\{ \sum_{\lambda=1}^2 \sum_{i=1}^2 F_\lambda^i \lambda^{(3)}_i - \sum_{i,j=1}^2 \sigma_\lambda^{ij}(z) \epsilon_\lambda^{ij}(\lambda^{(3)}) \right\} w_\lambda J \delta h_k \quad (22)$$

respectively. The numerical calculation of the adjoint load is considerably more difficult in the stress functional case. The shape function of the element must be known so that $\sigma^{ij}(\bar{\lambda})$ can be calculated using the finite element technique [2]

$$\sigma = [E][B]d = [E]\epsilon \quad (23)$$

where $[E]$ is the elasticity matrix, $[B]$ is the strain-displacement matrix, which relates to the element shape function, d is the displacement vector, and ϵ is the strain vector.

For a plane stress problem,

$$[E] = \frac{E}{1 - \nu^2} \begin{bmatrix} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 0 & 0 & \frac{1-\nu}{2} \end{bmatrix} \quad (24)$$

The adjoint load becomes

$$\iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(\bar{\lambda}) \right] m_p d\Omega \quad (25)$$

where F is the adjoint equivalent nodal force. Since m_p is a characteristic function on the finite element Ω_p , F acts only on the nodal points of element Ω_p .

After the adjoint load is calculated for various elements, a restart of the finite element model for each load case corresponding to each element adjoint load is made. The strains resulting from these adjoint loads are then used in calculating Eq. (22) for the sensitivity of each functional.

When principal stress is selected as the functional,

$$g_1 = (\sigma^{11} + \sigma^{22})/2 + \tau_{\max} \quad (26)$$

$$\tau_{\max} = \{[(\sigma^{11} - \sigma^{22}/2)^2 + (\sigma^{12})^2\}^{1/2} \quad (27)$$

and

$$\begin{aligned} \frac{\partial g_1}{\partial \sigma^{11}} &= \frac{1}{2} + \frac{1}{4} (\sigma^{11} - \sigma^{22})/\tau_{\max} \\ \frac{\partial g_1}{\partial \sigma^{22}} &= \frac{1}{2} - \frac{1}{4} (\sigma^{11} - \sigma^{22})/\tau_{\max} \\ \frac{\partial g_1}{\partial \sigma^{12}} &= \sigma^{12}/\tau_{\max} \end{aligned} \quad (28)$$

and when von Mises' stress is selected as the functional,

$$g_2 = [(\sigma^{11})^2 - \sigma^{11}\sigma^{22} + (\sigma^{22})^2 + 3(\sigma^{12})^2]^{1/2} \quad (29)$$

and

$$\begin{aligned}\partial g_2 / \partial \sigma_{11} &= \frac{1}{2} (2\sigma^{11} - \sigma^{22})/g_2 \\ \partial g_2 / \partial \sigma^{22} &= \frac{1}{2} (2\sigma^{22} - \sigma^{11})/g_2 \\ \partial g_2 / \partial \sigma^{12} &= 3\sigma^{12}/g_2\end{aligned}\quad (30)$$

2.1.2 Bending of Beams

Consider a cantilever beam with variable width and height and self weight, as shown in Fig. 4. The width and height are the design variables, $u = [b(x), h(x)]^T$.

The energy bilinear form and the load linear form of the beam are

$$a_u(z, \bar{z}) = \int_0^L E \frac{bh^3}{12} z_{xx} \bar{z}_{xx} dx \quad (31)$$

and

$$l_u(\bar{z}) = - \int_0^L (F + \gamma bh) \bar{z} dx \quad (32)$$

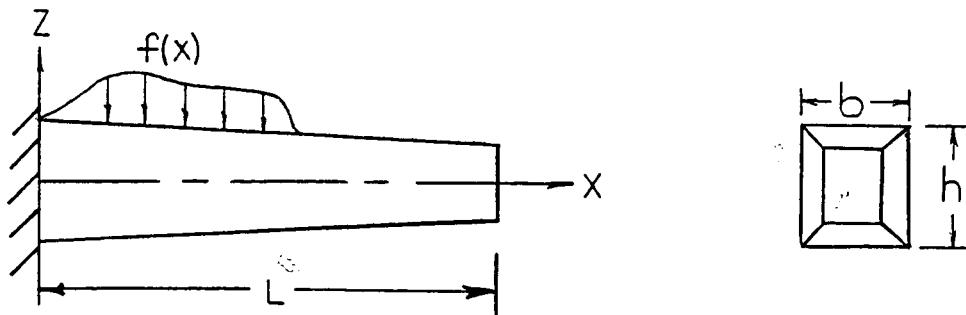


Figure 4. Cantilever Beam with Variable Width and Height

where γ is the weight density of the beam material, F is the distributed load, E is the modulus of elasticity of the beam material, $bh^3/12$ is the moment of inertia, \bar{z} is the virtual displacement, z_{xx} is the beam curvature, and \bar{z}_{xx} is the beam curvature due to the virtual displacement \bar{z} .

The negative sign in the load linear equation is due to the fact that the load is applied in the $-z$ direction.

The state equation is [1]

$$a_u(z, \bar{z}) = \lambda_u(\bar{z}) \quad (33)$$

for all kinematically admissible virtual displacements \bar{z} .

First consider the functional representing the compliance of the structure as

$$\psi_4 = - \int_0^L (F + \gamma b h) z \, dx \quad (34)$$

The first variation of Eq. (34) is

$$\psi'_4 = - \int_0^L (F + \gamma b h) z' \, dx - \int_0^L -h\gamma z \, dx \delta b - \int_0^L b\gamma z \, dx \delta h \quad (35)$$

To replace the variation in state z' by a virtual displacement $\bar{\lambda}$, the adjoint equation is defined as [1]

$$a_u(\lambda, \bar{\lambda}) = - \int_0^L (F + \gamma b h) \bar{\lambda} \, dx \quad (36)$$

for all kinematically admissible virtual displacements $\bar{\lambda}$. Since Eq. (36) is identical to Eq. (34), if $\bar{\lambda} = z$ the adjoint equation does not need to be solved. Using the adjoint variable method of design sensitivity analysis gives

$$\begin{aligned}\psi'_4 &= \int_0^L [-2\gamma h z - (Eh^3/12)(z_{xx})^2] dx \delta b \\ &\quad + \int_0^L [-2\gamma bz - (3Eb h^2/12)(z_{xx})^2] dx \delta h\end{aligned}\tag{37}$$

To numerically integrate Eqs. (34) and (37), a three-point Gauss quadrature formula is used. These equations become

$$\psi_4 = \sum_{k=1}^N \left\{ \sum_{\ell=1}^3 [F_{\ell} + \gamma b_k h_k] z_{\ell} W_{\ell} \right\} \delta b_k \tag{38}$$

and

$$\begin{aligned}\psi'_4 &= \sum_{k=1}^N \left\{ \sum_{\ell=1}^3 [-2\gamma h_k z_{\ell} - (Eh_k^2/12)(z_{xx})^2] W_{\ell} \right\} J \delta b_k \\ &\quad + \sum_{k=1}^N \left\{ \sum_{\ell=1}^3 [-2\gamma b_k z_{\ell} - (3Eb_k h_k^2/12)(z_{xx})^2] W_{\ell} \right\} J \delta h_k\end{aligned}\tag{39}$$

where N is the total number of elements, ℓ is the Gauss point counter, W is the weighting constant for the ℓ th Gauss point and J is the Jacobian. The beam curvature z_{xx} is calculated using a cubic polynomial for the standard beam shape functions. Because the load is in the $-z$ direction, it is necessary to change the sign of the local element y -rotation θ_y .

Next consider the functional representing the displacement z at a discrete point \hat{x}

$$\psi_5 \equiv z(\hat{x}) = \int_0^L \delta(x - \hat{x}) z(x) dx \tag{40}$$

where $\delta(x)$ is the Dirac measure at zero. The first variation of Eq. (40) is

$$\psi_5' = \int_0^L \hat{\delta}(x - \hat{x}) z'(x) dx \quad (41)$$

The adjoint equation is defined as [1]

$$a_u(\lambda, \bar{\lambda}) = \int_0^L \hat{\delta}(x - \hat{x}) \bar{\lambda}(x) dx \quad (42)$$

for all kinematically admissible virtual displacements $\bar{\lambda}$. Equation (42) has a unique solution $\lambda^{(5)}$, where $\lambda^{(5)}$ is the beam displacement due to a unit point load acting at a point \hat{x} . Using the adjoint variable method of design sensitivity analysis gives

$$\begin{aligned} \psi_5' &= \int_0^L [-h\gamma\lambda^{(5)} - (Eh^3/12)z_{xx}\lambda_{xx}^{(5)}] dx \delta b \\ &\quad + \int_0^L [-b\gamma\lambda^{(5)} - (3Eb^2h^2/12)z_{xx}\lambda_{xx}^{(5)}] dx \delta h \end{aligned} \quad (43)$$

As in the membrane displacement constraint case, only Eq.(43) needs to be solved numerically. Using the three-point Gauss quadrature technique, Eq. (43) becomes

$$\begin{aligned} \psi_5' &= \sum_{k=1}^N \left\{ \sum_{l=1}^3 [-h_k \gamma \lambda_l^{(5)} - (Eh_k^3/12) z_{xx} \lambda_{xx}^{(5)}] w_l \right\}_J \delta b_k \\ &\quad + \sum_{k=1}^N \left\{ \sum_{l=1}^3 [b_k \gamma \lambda_l^{(5)} - (3Eb_k h_k^2/12) z_{xx} \lambda_{xx}^{(5)}] w_l \right\}_J \delta h_k \end{aligned} \quad (44)$$

Finally consider the functional representing the allowable stresses in the beam as

$$\psi_6 = \int_0^L -\frac{1}{2} h E z_{xx} m_p dx \quad (45)$$

where $h/2$ is the half-depth of the beam, and m_p is a characteristic function defined on a finite element dx_p as

$$m_p = \begin{cases} \frac{1}{\int_{dx_p} dx}, & x \in dx_p \\ 0, & x \notin dx_p \end{cases} \quad (46)$$

The first variation of Eq. (45) is

$$\psi'_6 = \int_0^L \left[-\frac{1}{2} hE z'_{xx} m_p - \frac{1}{2} E z_{xx} m_p \delta h \right] dx \quad (47)$$

Replacing the variation in state z' by a virtual displacement $\bar{\lambda}$, the adjoint equation is defined as

$$a_u(\lambda, \bar{\lambda}) = - \int_0^L \frac{1}{2} hE \bar{\lambda}_{xx} m_p dx \quad (48)$$

for all kinematically admissible virtual displacements $\bar{\lambda}$. Equation (48) has a unique solution for a displacement field $\lambda^{(6)}$. Using the adjoint variable method of design sensitivity analysis gives

$$\begin{aligned} \psi'_6 = & \int_0^L \left[-h\gamma\lambda^{(6)} - (Eh^3/12)z_{xx}\lambda^{(6)}_{xx} \right] dx \delta b \\ & + \int_0^L \left[-\frac{1}{2} Ez_{xx} m_p - b\gamma\lambda^{(6)} - (3Ebh^2/12)z_{xx}\lambda^{(6)}_{xx} \right] dx \delta h \end{aligned} \quad (49)$$

where $\lambda^{(6)}$ is the solution of Eq. (48).

With the three-point Gauss quadrature numerical integration technique, the integrals in Eqs. (45), (48), and (49) become

$$\psi_6 = \sum_{k=1}^N \left\{ \sum_{\lambda=1}^3 \left(-\frac{1}{2} h_k E z_{xx} \lambda^{(6)}_{\lambda} \right) w_{\lambda} \right\} J \quad (50)$$

$$\int_0^L \frac{1}{2} E \bar{\lambda}_{xx} m_p dx \\ = \sum_{k=1}^N \left\{ \sum_{\ell=1}^3 \left(-\frac{1}{2} E[B]_{\ell} m_p \right) W_{\ell} \right\}_J \bar{d} \quad (51)$$

and

$$\psi'_6 = \sum_{k=1}^N \left\{ \sum_{\ell=1}^3 \left[-h_k \gamma \lambda_{\ell}^{(6)} - (Eh_k^3/12) z_{xx} \lambda_{xx}^{(6)} \right] W_{\ell} \right\}_J \delta b_k \\ + \sum_{k=1}^N \left\{ \sum_{\ell=1}^3 \left[-\frac{1}{2} E z_{xx} m_p - b_k \gamma \lambda_{\ell}^{(6)} \right. \right. \\ \left. \left. - (3E b_k h_k^2/12) z_{xx} \lambda_{xx}^{(6)} \right] W_{\ell} \right\}_J \delta h_k \quad (52)$$

where $[B]$ is the strain-displacement matrix, which is the second derivative of the shape functions.

2.1.3 Bending of Plates

Consider the clamped plate in Fig. 5 of variable thickness $u = t(x)$, with a distributed load $f(x)$ that consists of an externally applied pressure $F(x)$ and self weight, given by [1]

$$f(x) = F(x) + \gamma t(x) \quad (53)$$

where γ is the weight density of the material.

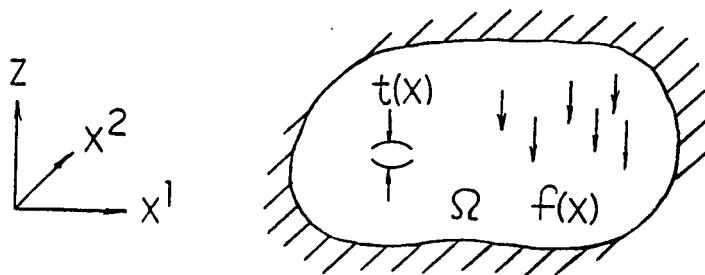


Figure 5. Clamped plate of variable thickness $t(x)$

For this design dependent loading, the energy bilinear form and the load linear form for the plate are given as [1]

$$\begin{aligned} a_u(z, \bar{z}) = & \iint_{\Omega} \hat{D}(u) [z_{11}\bar{z}_{11} + z_{22}\bar{z}_{22} + v(z_{22}\bar{z}_{11} + z_{11}\bar{z}_{22}) \\ & + 2(1-v)z_{12}\bar{z}_{12}] d\Omega \end{aligned} \quad (54)$$

and

$$l_u(\bar{z}) = \iint_{\Omega} [F + \gamma t] \bar{z} d\Omega \quad (55)$$

where $\hat{D}(u) = Et^3/[12(1-v^2)]$ is the flexural rigidity, E is Young's modulus, v is Poisson's ratio, F is the externally applied pressure, and γ is the material density. The state equation is [1]

$$a_u(z, \bar{z}) = l_u(\bar{z}) \quad (56)$$

for all kinematically admissible virtual displacements \bar{z} .

First consider the functional representing the compliance of the structure as

$$\psi_7 = \iint_{\Omega} (F + \gamma t) z d\Omega \quad (57)$$

The first variation of Eq. (57) is

$$\psi'_7 = \iint_{\Omega} [(F + \gamma t) z' + \gamma z \delta t] d\Omega \quad (58)$$

The adjoint equation is defined as

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} (F + \gamma t) \bar{\lambda} d\Omega \quad (59)$$

for all kinematically admissible displacements $\bar{\lambda}$. As in the previous cases (membranes and bending beams), Eq. (59) is identical to Eq. (57)

if $\bar{\lambda} = z$. Using the adjoint variable method of design sensitivity analysis gives

$$\begin{aligned}\psi_7' &= \iint_{\Omega} \{2\gamma z - Et^2[z_{11}^2 z_{22}^2 + 2\nu z_{11} z_{22} + 2(1-\nu)z_{12}^2]/4(1-\nu^2)\} \delta t \, d\Omega \\ &= \iint_{\Omega} [2\gamma z - \sum_{i,j=1}^2 \sigma^{ij}(z) \epsilon^{ij}(z)] \delta t \, d\Omega \quad (60)\end{aligned}$$

where $\sigma^{ij}(z)$ and $\epsilon^{ij}(z)$ are the stress and strain of the extreme fiber, given as

$$\epsilon^{ij} = -\frac{tz_{ij}}{2}, \quad i, j = 1, 2 \quad (61)$$

and

$$\begin{aligned}\sigma^{11} &= -\frac{Et}{2(1-\nu^2)} (z_{11} + \nu z_{22}) \\ \sigma^{22} &= -\frac{Et}{2(1-\nu^2)} (z_{22} + \nu z_{11}) \\ \sigma^{12} &= -\frac{Et}{2(1+\nu)} z_{12} \quad (62)\end{aligned}$$

To numerically integrate Eqs. (57) and (60), a one-point Gauss quadrature formula on a triangular element is used to correspond to the IFAD integration technique for this element. Equations (57) and (60) become

$$\psi_7 = \sum_{k=1}^N \{(F + \gamma t_k) z \, w\} J \quad (63)$$

and

$$\psi_7' = \sum_{k=1}^N [2\gamma z - \sum_{i,j=1}^2 \sigma^{ij}(z) \epsilon^{ij}(z)] w \, J \, \delta t_k \quad (64)$$

Next consider the functional representing the displacement z at a discrete point \hat{x}

$$\psi_8 \equiv z(\hat{x}) = \iint_{\Omega} \hat{\delta}(x - \hat{x}) z(x) d\Omega \quad (65)$$

The first variation of Eq. (65) is

$$\psi'_8 = \iint_{\Omega} \hat{\delta}(x - \hat{x}) z'(x) dx \quad (66)$$

The adjoint equation is defined as

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} \hat{\delta}(x - \hat{x}) \bar{\lambda}(x) d\Omega \quad (67)$$

for all kinematically admissible virtual displacements $\bar{\lambda}$. This equation has a unique solution $\lambda^{(8)}$, where $\lambda^{(8)}$ is the plate displacement due to a unit vertical load acting at a point \hat{x} . Using the adjoint variable method of design sensitivity analysis gives

$$\begin{aligned} \psi'_8 &= \iint_{\Omega} \{ \gamma \lambda^{(8)} - E t^2 [z_{11} \lambda_{11}^{(8)} + z_{22} \lambda_{22}^{(8)} + v(z_{11} \lambda_{22}^{(8)} + z_{22} \lambda_{11}^{(8)}) \\ &\quad + 2(1 - v) z_{12} \lambda_{12}^{(8)}] / 4(1 - v^2) \} \delta t \, d\Omega \\ &= \iint_{\Omega} [\gamma \lambda^{(8)} - \sum_{i,j=1}^2 \sigma^{ij}(z) \varepsilon^{ij}(\lambda^{(8)})] \delta t \, d\Omega \end{aligned} \quad (68)$$

The same numerical integration procedure is used as in the compliance case. Equation (68) becomes

$$\psi'_8 = \sum_{k=1}^N [\gamma \lambda^{(8)} - \sum_{i,j=1}^2 \sigma^{ij}(z) \varepsilon^{ij}(\lambda^{(8)})] w_j \delta t_k \quad (69)$$

Finally, consider the functional representing a locally averaged stress in the plate as

$$\psi_9 = \iint_{\Omega} g(\sigma(z)) m_p d\Omega \quad (70)$$

where $g(\sigma(z))$ may be principal stress, von Mises' stress, or some other material failure criteria and m_p is a characteristic function defined on a finite element Ω_p as

$$m_p = \begin{cases} \frac{1}{\int_{\Omega_p} d\Omega}, & x \in \Omega_p \\ 0, & x \notin \Omega_p \end{cases} \quad (71)$$

The first variation of Eq. (70) is

$$\psi'_9 = \iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(z') \right] m_p d\Omega \quad (72)$$

The adjoint equation is defined as [1]

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(\bar{\lambda}) \right] m_p d\Omega \quad (73)$$

for all kinematically admissible virtual displacement $\bar{\lambda}$. Using the adjoint variable method of design sensitivity analysis gives

$$\psi'_9 = \iint_{\Omega} [\gamma \lambda^{(9)} - \sum_{i,j=1}^2 \sigma^{ij}(z) \varepsilon^{ij}(\lambda^{(9)})] \delta t d\Omega + \iint_{\Omega} \frac{\partial g}{\partial t} \delta t d\Omega \quad (74)$$

where $\lambda^{(9)}$ is the solution of Eq. (73). For principal stress the last term on the right of Eq. (74) becomes

$$\iint_{\Omega} [(\sigma^{11} + \sigma^{22} + 2\tau_{\max})/(2t)] m_p d\Omega \quad (75)$$

where τ_{\max} is defined in Eq. (27). For von Mises' stress, this term becomes

$$\iint_{\Omega} \frac{1}{t} [(\sigma^{11})^2 - \sigma^{11}\sigma^{22} + (\sigma^{22})^2 + 3(\sigma^{12})^2]^{1/2} m_p \delta t d\Omega \quad (76)$$

The IFAD thin shell element is the element that is used for plate bending. The membrane effects can be eliminated so that only the bending term exists. This element is a hybrid element which uses a derivative smoothing technique [4]. The IFAD code evaluates the normal and shear stresses at the centroid of the triangle, but Ref. 4 stipulates that the stresses at the midside nodes of the triangle give the most accurate results. The integration of a function ϕ from its mid-stresses is [4]

$$\int \phi dA = \frac{A}{3} [\phi(0, \frac{1}{2}, \frac{1}{2}) + \phi(\frac{1}{2}, \frac{1}{2}, 0) + \phi(\frac{1}{2}, 0, \frac{1}{2})] \quad (77)$$

where A is the area of the triangle and $(0, \frac{1}{2}, \frac{1}{2})$, $(\frac{1}{2}, 0, \frac{1}{2})$ and $(\frac{1}{2}, \frac{1}{2}, 0)$ are the area coordinates of the mid-side nodes. To achieve the most accurate stresses possible, this numerical integration technique is applied on Eqs. (70), (73), and (74). These equations become

$$\begin{aligned} \psi_9 &= \sum_{n=1}^3 g(\sigma_n(z)) m_p \frac{A}{3} \\ \iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma_{ij}} \sigma_{ij}(\bar{\lambda}) \right] m_p d\Omega &= \sum_{n=1}^3 \left[\frac{\partial g}{\partial \sigma_n^{11}}, \frac{\partial g}{\partial \sigma_n^{22}}, \frac{\partial g}{\partial \sigma_n^{12}} \right] \end{aligned} \quad (78)$$

$$[E][B]_n m_p \frac{A}{3} \bar{d} = F^T \bar{d} \quad (79)$$

and

$$\psi_9' = \sum_{k=1}^N \left\{ \sum_{n=1}^3 [\gamma \lambda_n^{(9)} - \sum_{i,j=1}^2 \sigma_n^{ij}(z) \epsilon_n^{ij}(\lambda^{(9)}) + (\frac{\partial g}{\partial t})_n] \frac{A}{3} \right\} \delta t_k \quad (80)$$

where subscript n is the counter for the midside value. The term $(\partial g / \partial t)_n$ for principal and von Mises' stress is

$$[(\sigma_n^{11} + \sigma_n^{22} + \sigma_{max,n}^{22}) / (2t_k)] m_p \quad (81)$$

and

$$\frac{1}{t_k} [(\sigma_n^{11})^2 - \sigma_n^{11} \sigma_n^{22} + (\sigma_n^{22})^2 + 3(\sigma_n^{12})^2]^{1/2} m_p \quad (82)$$

respectively.

To numerically calculate the adjoint load, the shape function of the element must be known so that $\sigma^{ij}(\bar{\lambda})$ can be calculated using the finite element technique described in Section 2.1.1, Eqs. (23) and (25).

2.2 Calculation Procedure for a Built-Up Structure

The foundation of the built-up structure design sensitivity analysis method is the structural component analysis developed in Section 2.1. A built-up structure consists of various structural components that interact with each other. This interaction is taken into account by generalizing the individual components such that twisting, bending, transverse shear terms, etc. are included in the formulation of the sensitivity vector. Coordinate system precautions need to be taken to insure that the constraints and the sensitivity vectors are calculated correctly. In general, if the calculations are performed at

the local element coordinate system level, there will be no problem when components are oriented differently in the global coordinate system.

An example of a built-up structure using the structural components developed in the previous section would be a bending beam and plate problem, where a framework of beams could act as the supporting structure for the plate; i.e., a roof structure.

Figure 6 shows a built-up structure that has design variables $u = [b(x), h(x), t(x)]^T$, where $b(x)$ is the width of the beams, $h(x)$ is the height of the beams, and $t(x)$ is the thickness of the plates.

It is assumed that the plates are welded along the length of the beams. This would infer that the appropriate components in the finite element analysis must be chosen to insure kinematic compatibility along the component boundaries.

The energy bilinear form of the system equation is just the sum of the plate and beam energy bilinear equations, with an additional beam torsion term given as

$$\begin{aligned}
 a_u(z, \bar{z}) &= \sum \iint_{\Omega} \hat{D}(u) [z_{xx} \bar{z}_{xx} + z_{yy} \bar{z}_{yy} + \{(z_{yy} \bar{z}_{xx} + z_{xx} \bar{z}_{yy}) \\
 &\quad + 2(1 - v) z_{xy} \bar{z}_{xy}\}] d\Omega + \sum \int_0^L E_b \frac{bh^3}{12} z_{xx} \bar{z}_{xx} dx_l \\
 &\quad + \sum \int_0^L GJ z_{xy} \bar{z}_{xy} dx_l \\
 &= \sum a_u(z, \bar{z})_{\text{plate}} + \sum a_u(z, \bar{z})_{\text{beam}} + \sum \int_0^L GJ z_{xy} \bar{z}_{xy} dx_l
 \end{aligned} \tag{83}$$

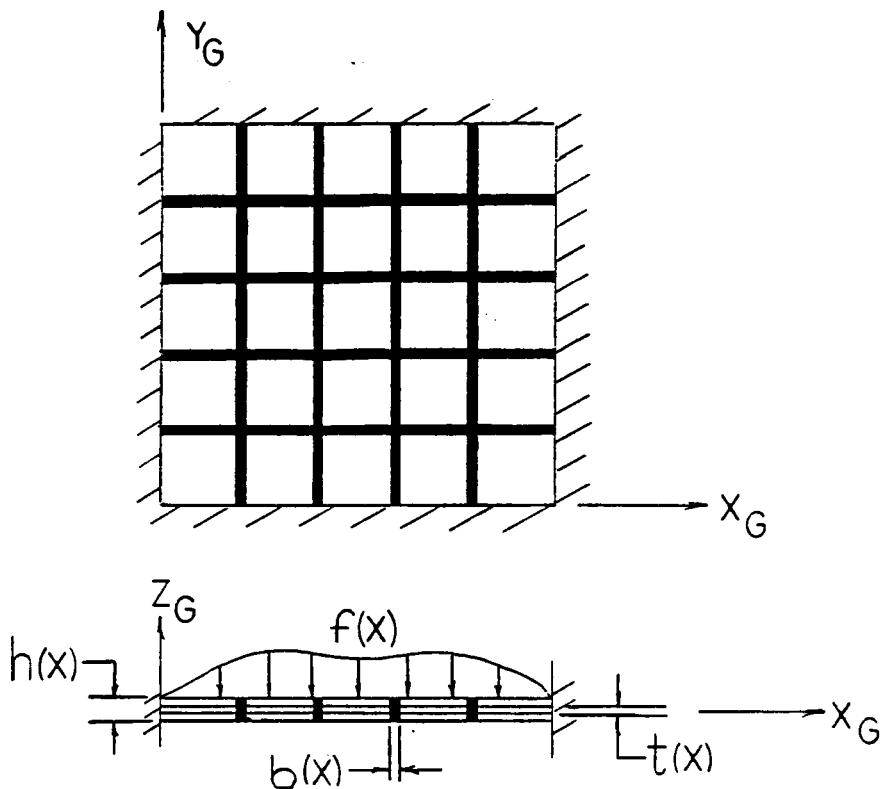


Figure 6. Roof Structure

where $a_u(z, z)$ _{plate} and $a_u(z, z)$ _{beam} are the energy bilinear forms of the plate, Eq. (54) and beam, Eq. (31), respectively, G is the modulus of rigidity, J is the torsional moment of inertia of the beam, and ℓ represents the local beam coordinate system, where x_ℓ runs along the length of the beam.

In Eq. (83) z_{xy} represents the beam torsion term. Since each structural component needs to be solved individually to make the analysis feasible with an existing finite element code, a relationship between z_{xy} and the beam rotation has to be used. This kinematic compatibility states that for the beam and plate system the term has to be equivalent to the relative angle of twist over an element length.

That is to say,

$$z_{xy} = (\theta^2 x_\ell - \theta^1 x_\ell)/L \quad (84)$$

where $\theta^2 x_\ell$ is the local element rotation at node 2 of the beam, $\theta^1 x_\ell$ is the local element rotation at node 1 of the beam, and L is the beam element length.

The load linear form of the system is

$$\lambda_u(\bar{z}) = \iint_{\Omega} [F_p + \gamma_p t + \gamma_b b h] \bar{z} d\Omega \quad (85)$$

where F_p is the externally applied plate pressure, γ_p and γ_b are the material densities for the plates and beams respectively, and \bar{z} is the virtual displacement. The state equation is [1]

$$a_u(z, \bar{z}) = \lambda_u(\bar{z}) \quad (86)$$

for all kinematically admissible virtual displacements \bar{z} .

Since the energy bilinear form of the system equation is just the addition of each structural component's energy bilinear forms, the design sensitivity equation of the system turns out also to be an additive process. The generalized design sensitivity of the built-up structure is

$$\psi' = \psi'_b \delta b + \psi'_h \delta h + \psi'_t \delta t \quad (87)$$

The only necessary step to calculating this value is the reformulation of the beam to include the torsional term. The energy bilinear form of the beam component becomes

$$a_u(z, \bar{z}) = \int_0^L E(bh^3/12) z_{xx} \bar{z}_{xx} dx + \int_0^L GJ z_{xy}^2 dx \quad (88)$$

where Eq. (84) defines z_{xy} .

If the compliance, displacement, and stress functionals of the beam - Eqs. (34), (40), and (45), respectively - remain the same, the only additional term in the design sensitivity analysis [1] is due to the differentiation of the torsional terms in the energy bilinear equation with respect to the design variables b and h . This term is defined as

$$\int_0^L \left[\frac{\partial J}{\partial h} \delta h + \frac{\partial J}{\partial b} \delta b \right] G z_{xy} \lambda_{xy} dx \quad (89)$$

For a beam with a rectangular cross section [5]

$$J = bh^3 \left[\frac{1}{3} - 0.21(b/h) \left(1 - \frac{b^4}{12h^4} \right) \right] \quad (90)$$

and the derivatives with respect to the design variables are

$$\frac{\partial J}{\partial b} = \frac{h^3}{3} - 0.042b \left(h^2 + \frac{b^4}{4h^2} \right) \quad (91)$$

and

$$\frac{\partial J}{\partial h} = bh^2 - 0.42b^2 \left(h - \frac{b^3}{12h} \right) \quad (92)$$

The compliance sensitivity of Eq. (37) becomes

$$\begin{aligned} \psi'_4 &= \int_0^L \left[-2\gamma h z - \left(Eh^3/12 \right) (z_{xx})^2 - \frac{\partial J}{\partial b} G(z_{xy})^2 \right] dx \delta b \\ &\quad + \int_0^L \left[-2\gamma b z - \left(3Ebh^2/12 \right) (z_{xx})^2 - \frac{\partial J}{\partial h} G(z_{xy})^2 \right] dx \delta h \end{aligned} \quad (93)$$

the displacement sensitivity of Eq. (43) becomes

$$\begin{aligned}\psi'_5 &= \int_0^L [-h\gamma\lambda^{(5)} - \frac{Eh^3}{12} z_{xx}\lambda_{xx}^{(5)} - \frac{\partial J}{\partial b} G z_{xy}\lambda_{xy}^{(5)}] dx \delta b \\ &\quad + \int_0^L [-2\gamma b\lambda^{(5)} - \frac{3Ebh^2}{12} z_{xx}\lambda_{xx}^{(5)} - \frac{\partial J}{\partial h} G z_{xy}\lambda_{xy}^{(5)}] dx \delta h\end{aligned}\quad (94)$$

and the stress sensitivity of Eq. (49) becomes

$$\begin{aligned}\psi'_6 &= \int_0^L [-h\gamma\lambda^{(6)} \frac{Eh^3}{12} z_{xx}\lambda_{xx}^{(6)} - \frac{\partial J}{\partial b} G z_{xy}\lambda_{xy}^{(6)}] dx \delta b \\ &\quad + \int_0^L [-\frac{1}{2} E z_{xx} m_p - b\gamma\lambda^{(6)} - \frac{3Ebh^2}{12} z_{xx}\lambda_{xx}^{(6)} - \frac{\partial J}{\partial h} G z_{xy}\lambda_{xy}^{(6)}] dx \delta h\end{aligned}\quad (95)$$

when the torsional term is added, where $\lambda^{(5)}$ and $\lambda^{(6)}$ are the solutions to the adjoint Eqs. (42) and (48), respectively.

Caution has to be taken when the constraint functionals on the system are defined. When a von Mises' stress functional is specified for a particular plate element, the allowable beam bending stress term $-\int_0^L \frac{1}{2} E z_{xx} m_p dx \delta h$ must be removed from Eq. (95), so that the design sensitivity of Eq. (87) is calculated only for the von Mises' stress functional. In the same way, if an allowable beam bending stress functional is specified for a particular beam element, the von Mises' stress term $\partial g / \partial t$ of Eq. (76) must be removed from Eq. (74), so that the design sensitivity of Eq. (87) is calculated only for the allowable beam bending stress functional. The application of this procedure is shown below for a von Mises' stress functional, a compliance functional and a displacement functional on a plate element and an allowable

bending stress functional on a beam element of the built-up structure of Fig. 6.

The functional representing a von Mises' stress constraint on a plate element is

$$\psi_{10} = \iint_{\Omega} [\sigma_{xx}^2 - \sigma_{xx}\sigma_{yy} + \sigma_{yy}^2 + 3\tau_{xy}^2]^{1/2} m_p d\Omega \quad (96)$$

The adjoint load linear form is defined as

$$\begin{aligned} & \iint_{\Omega} \left[\sum_{i,j=1}^2 \frac{\partial g}{\partial \sigma^{ij}} \sigma^{ij}(\bar{\lambda}) \right] m_p d\Omega \\ &= \left[\frac{\partial g}{\partial \sigma_{xx}}, \frac{\partial g}{\partial \sigma_{yy}}, \frac{\partial g}{\partial \tau_{xy}} \right] [E][B] m_p d\Omega \bar{d} \\ &= F^T \bar{d} \end{aligned} \quad (97)$$

where $\partial g / \partial \sigma^{ij}$ is defined in Eq. (30) and F is the adjoint equivalent nodal force. Using Eq. (87) gives the design sensitivity of the roof structure as

$$\begin{aligned} \psi'_{10} &= \sum \iint_{\Omega} [\gamma \lambda^{(10)} - \sum_{i,j=1}^2 \sigma^{ij}(z) \varepsilon^{ij}(\lambda^{(10)}) + \frac{\partial g}{\partial t}] \delta t d\Omega \\ &+ \sum \int_0^L \left[-h \gamma \lambda^{(10)} - \frac{Eh^3}{12} z_{xx} \lambda_{xx}^{(10)} - \frac{\partial J}{\partial b} G z_{xy} \lambda_{xy}^{(10)} \right] dx_l \delta b \\ &+ \sum \int_0^L \left[-b \gamma \lambda^{(10)} - \frac{3Ebh^2}{12} z_{xx} \lambda_{xx}^{(10)} - \frac{\partial J}{\partial h} G z_{xy} \lambda_{xy}^{(10)} \right] dx_l \delta h \end{aligned} \quad (98)$$

where subscript l refers to the beam local coordinate system and $\partial g / \partial t$ is defined in Eq. (76).

The functional representing a compliance constraint on a plate element is

$$\psi_{11} = \iint_{\Omega} (F + \gamma t + \gamma b h) z \, d\Omega \quad (99)$$

where γt and $\gamma b h$ are the self weight of the plate and beam, respectively. The adjoint load linear form is defined as

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} (F + \gamma t + \gamma b h) \bar{\lambda} \, d\Omega \quad (100)$$

Since Eq. (100) is identical to Eq. (99) if $\bar{\lambda} = z$, the adjoint equation does not need to be solved. Using Eq. (87) gives the design sensitivity of the built-up structure as

$$\begin{aligned} \psi'_{11} &= \sum \iint_{\Omega} [2\gamma z - \sum_{i,j=1}^2 \sigma^{ij}(z) \epsilon^{ij}(\bar{z})] \delta t \, d\Omega \\ &+ \sum \int_0^L [-2\gamma b z - E h^3 / 12 (z_{xx})^2 - \frac{\partial J}{\partial b} G(z_{xy})^2] dx_l \delta b \\ &+ \sum \int_0^L [-2\gamma b z - (3E b h^2 / 12) (z_{xx})^2 - \frac{\partial J}{\partial h} G(z_{xy})^2] dx_l \delta h \end{aligned} \quad (101)$$

where subscript l refers to the beam local coordinate system.

The functional representing the displacement z at a discrete point \hat{x} is

$$\psi_{12} \equiv z(\hat{x}) = \iint_{\Omega} \hat{\delta}(x - \hat{x}) z(x) \, d\Omega \quad (102)$$

The adjoint load linear form is defined as

$$a_u(\lambda, \bar{\lambda}) = \iint_{\Omega} \hat{\delta}(x - \hat{x}) \bar{\lambda}(x) \, d\Omega \quad (103)$$

for all kinematically admissible virtual displacements $\bar{\lambda}$. This equation has a unique solution $\lambda^{(12)}$, where $\lambda^{(12)}$ is the plate displacement due

to a unit vertical load acting at a point \hat{x} . Using Eq. (87) gives the design sensitivity of the built-up structure as

$$\begin{aligned}\psi'_{12} = & \sum \iint_{\Omega} [\gamma \lambda^{(12)} - \sum_{i,j=1}^2 \sigma^{ij}(z) \varepsilon^{ij}(\lambda^{(12)})] \\ & + \sum \int_0^L [-h\gamma \lambda^{(12)} - \frac{Eh^3}{12} z_{xx} \lambda_{xx}^{(12)} - \frac{\partial J}{\partial b} G z_{xy} \lambda_{xy}^{(12)}] dx \delta b \\ & + \sum \int_0^L [-b\gamma \lambda^{(12)} - \frac{3Ebh^2}{12} z_{xx} \lambda_{xx}^{(12)} - \frac{\partial J}{\partial h} G z_{xy} \lambda_{xy}^{(12)}] dx \delta h\end{aligned}\quad (104)$$

where subscript ℓ refers to the beam local coordinate system.

The functional representing an allowable bending stress on a beam element is

$$\psi_{13} = - \int_0^L \frac{1}{2} h E z_{xx} m_p dx \quad (105)$$

The adjoint load linear form is defined as

$$\int_0^L \frac{1}{2} h E \bar{\lambda}_{xx} m_p dx = \int_0^L \frac{1}{2} h E [B] m_p dx \bar{d} = F^T d \quad (106)$$

where F is the adjoint equivalent nodal force. Using Eq. (87) gives the design sensitivity of the built-up structures as

$$\begin{aligned}\psi'_{13} = & \sum \iint_{\Omega} [\gamma \lambda^{(13)} - \sum_{i,j=1}^2 \sigma^{ij}(z) \varepsilon^{ij}(\lambda^{(13)})] \delta t d\Omega \\ & + \sum \int_0^L [-h\gamma \lambda^{(13)} - \frac{Eh^3}{12} z_{xx} \lambda_{xx}^{(13)} - \frac{\partial J}{\partial b} G z_{xy} \lambda_{xy}^{(13)}] dx \delta b\end{aligned}$$

$$\begin{aligned}
 & + \sum \int_0^L \left[-b\gamma\lambda^{(13)} - \frac{1}{2} Ez_{xx} m_p - \frac{3Ebh^2}{12} z_{xx} \lambda_{xx}^{(13)} \right. \\
 & \quad \left. - \frac{\partial J}{\partial h} G z_{xy} \lambda_{xy}^{(13)} \right] dx_\ell dh
 \end{aligned} \tag{107}$$

where subscript ℓ refers to the beam local coordinate system.

CHAPTER III

NUMERICAL EXAMPLES

The design sensitivity of a constraint functional ψ is the differential ψ' of the constraint functional. In order to make sure the design sensitivity is accurate, an approximation $\Delta\psi$ is made using the finite difference method. It is very important that an appropriate perturbed design variable δu is selected. If δu is too small, the change in the constraint functional $\Delta\psi$ may be inaccurate due to losses of significant digits. If δu is too large, $\Delta\psi$ will be influenced by nonlinearities in the constraint functional, which in turn will cause an inaccurate design sensitivity prediction.

In all the following examples, perturbations in design of 1% and/or 5% are used, with the exception of the plate bending and built up structure examples. Because of the nonlinearity characteristics of built-up structural response, the perturbation of 0.1% was used.

3.1 Membranes

The finite element membrane model in Fig. 7 is a simple plane elastic solid that is restrained at one end and loaded with a distributed tensile load at the other end. It contains 80 isoparametric elements (IFAD plane stress element type 1104), 289 nodal points, and 560 degrees-of-freedom, with the design variable being the variable thickness $u = h(x)$. The material property constraints, Young's modulus,

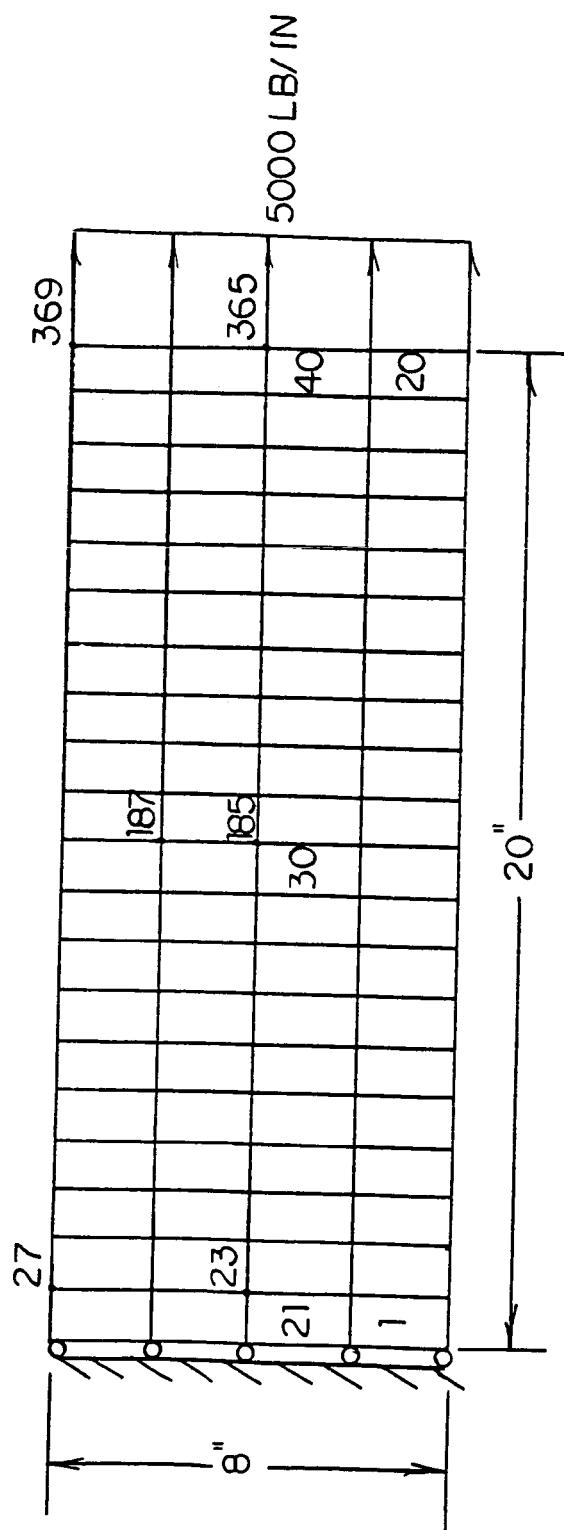


Figure 7. Plane Elastic Solid Finite Element Model

and Poission's ratio are given as $E = 3 \times 10^7$ psi and $\nu = 0.3$, respectively. Each finite element is discretized so that a constant thickness of $h = 0.5$ in. is used in order to simplify the sensitivity calculation.

The compliance sensitivity results are shown in Table 1, where $\Delta\psi_1 = \psi_1(h + \delta h) - \psi_1(h)$ and ψ' and is the predicted value calculated from Eq. (9), with design perturbations of $\delta h = 0.01h$ and $\delta h = 0.05h$. The percent accuracy of the sensitivity prediction is calculated using $\psi' \times 100 / \Delta\psi_1$.

Table 1. Membrane Design Sensitivity Check for Compliance

| δh | $\psi_1(h)$ | $\psi_1(h + \delta h)$ | $\Delta\psi_1$ | ψ' | $\psi' \times 100 / \Delta\psi_1$ |
|------------|-------------|------------------------|----------------|---------|-----------------------------------|
| 0.01h | 265.302 | 262.676 | -2.627 | -2.653 | 101.0 |
| 0.05h | 265.302 | 252.668 | -12.632 | -13.265 | 105.0 |

Several discrete points shown in Fig. 6 are selected to check accuracy of the design sensitivity of the displacement functional of Eq. (14). In order to calculate this equation, the strain ϵ^{ij} due to the adjoint load is needed. Since the adjoint load is just a unit point load at point \hat{x} , acting in the direction of the displacement, a restart of the finite element analysis is all that is needed. For every node direction, there is a separate load case that produces a strain ϵ^{ij} , which in turn is used to calculate sensitivity of displacement. Design sensitivity predictions and differences, with $\delta h = 0.05h$ are given in Table 2.

Table 2. Design Sensitivity Check for Displacement

| Node No. | Dir | $\psi_2(h)$ | $\psi_2(h+\delta h)$ | $\Delta\psi_2$ | ψ'_2 | % Accuracy |
|----------|-----|-------------|----------------------|----------------|------------|------------|
| 23 | x1 | 2.974E-04 | 2.832E-04 | -1.416E-04 | -1.487E-05 | 105.0 |
| 27 | x1 | 4.058E-04 | 3.865E-04 | -1.932E-05 | -2.029E-05 | 105.0 |
| 27 | x2 | -2.248E-04 | -2.141E-04 | 1.071E-05 | 1.124E-05 | 105.0 |
| 185 | x1 | 3.298E-03 | 3.141E-03 | -1.571E-04 | -1.649E-04 | 105.0 |
| 187 | x1 | 3.299E-03 | 3.142E-03 | -1.571E-04 | -1.650E-04 | 105.0 |
| 187 | x2 | -2.014E-04 | -1.918E-04 | 0.959E-05 | 1.007E-05 | 105.0 |
| 365 | x1 | 6.633E-03 | 6.317E-03 | -3.158E-04 | -3.316E-04 | 105.0 |
| 369 | x1 | 6.633E-03 | 6.317E-03 | -3.158E-04 | -3.316E-04 | 105.0 |
| 369 | x2 | -4.000E-04 | -3.809E-04 | 1.905E-05 | 2.000E-05 | 105.0 |

To check the stress constraint sensitivity of Eq. (22), the equivalent nodal force of the adjoint load on the right of Eq. (25) has to be calculated so that $\epsilon_{\lambda}^{ij}(\lambda^{(3)})$ is known for each constrained element. This is accomplished by a restart of the original IFAD model, with each adjoint load for an element being a separate loading case. Design sensitivity results for principal and von Mises' stress functionals are given in Table 3 for several finite elements. The perturbations are $\delta h = 0.01h$ and $\delta h = 0.05h$ for von Mises' stress and $\delta h = 0.05h$ for principal stress.

The design sensitivity calculation is performed using double precision accuracy. Since the finite difference approximation in Tables 1, 2, and 3 are no smaller than two significant digits of the actual constraint functional, loss of significant digits is minimal. Therefore, the design perturbation is not too small. With all three

Table 3. Design Sensitivity Check for Stress

(a) von Mises' Stress with $\delta h = 0.01h$

| El. No. | $\psi_3(h)$ | $\psi_3(h + \delta h)$ | $\Delta\psi_3$ | ψ'_3 | $(\psi'_3 / \Delta\psi_3 \times 100)\%$ |
|------------|-------------|------------------------|----------------|-----------|---|
| 1 | 9888.882 | 9790.973 | -97.910 | -98.889 | 101.0 |
| 10 | 9989.932 | 9891.022 | -98.910 | -99.899 | 101.0 |
| 20 | 9999.982 | 9900.972 | -99.010 | -100.000 | 101.0 |
| 21 | 8752.850 | 8666.188 | -86.662 | -87.528 | 101.0 |
| 30 | 10024.586 | 9925.333 | -99.253 | -100.246 | 101.0 |
| 40 | 9999.853 | 9900.845 | -99.008 | -100.000 | 101.0 |

(b) von Mises' Stress with $\delta h = 0.05h$

| El. No. | $\psi_3(h)$ | $\psi_3(h + \delta h)$ | $\Delta\psi_3$ | ψ'_3 | $(\psi'_3 / \Delta\psi_3 \times 100)\%$ |
|------------|-------------|------------------------|----------------|-----------|---|
| 1 | 9888.882 | 9417.984 | -470.899 | -494.444 | 105.0 |
| 10 | 9989.932 | 9514.222 | -475.711 | -499.497 | 105.0 |
| 20 | 9999.982 | 9523.793 | -476.189 | -499.998 | 105.0 |
| 21 | 8752.850 | 8336.048 | -416.802 | -437.642 | 105.0 |
| 30 | 10024.586 | 9547.225 | -477.361 | -501.230 | 105.0 |
| 40 | 9999.853 | 9523.670 | -476.183 | -499.993 | 105.0 |

(c) Principal Stress with $\delta h = 0.05h$

| El. No. | $\psi_3(h)$ | $\psi_3(h + \delta h)$ | $\Delta\psi_3$ | ψ'_3 | $(\psi'_3 / \Delta\psi_3 \times 100)\%$ |
|------------|-------------|------------------------|----------------|-----------|---|
| 1 | 10582.770 | 10078.829 | -503.941 | -529.138 | 105.0 |
| 10 | 9987.061 | 9511.487 | -475.574 | -499.353 | 105.0 |
| 20 | 10000.013 | 9523.823 | -476.191 | -500.001 | 105.0 |
| 21 | 9660.279 | 9200.266 | -460.013 | -483.014 | 105.0 |
| 30 | 10012.976 | 9536.617 | -476.808 | -500.649 | 105.0 |
| 40 | 9999.987 | 9523.797 | -476.189 | -500.000 | 105.0 |

constraint functionals, the design sensitivity results compared to the finite difference approximation are excellent. This infers that the design perturbation is not too large as to cause significant nonlinearity effects in the calculation of design sensitivity.

It is interesting to note that in Tables 1, 2, and 3 the finite difference approximation is nearly 1% of the constraint functional when $\delta h = 0.01h$ and nearly 5% of the constraint functional when $h = 0.05h$. The results also show that as δh approaches zero, $\psi'/\Delta\psi$ approaches one.

3.2 Bending of Beams

A cantilevered beam finite element model shown in Fig. 8 is loaded with a constant distributed force $f(x) = 0.03 \text{ lb/in.}$ along the entire length of the beam. It contains 20 IFAD beam elements of type 0501, each 3" in length, 121 nodal points, and 40 degrees-of-freedom, with design variables $u = [b(x), h(x)]^T$, the width and height of the beam. In Fig. 8, the element numbers are along the top of the beam and the node numbers are along the bottom of the beam. The beam has a rectangular cross-section with constant width and height $b = 0.5 \text{ in.}$ and $h = 0.75 \text{ in.}$, respectively. This gives the moment of inertia $I_y = 0.01758 \text{ in.}^4$ and the cross-sectional area $A_c = 0.375 \text{ in.}^2$. The material property constants, Young's modulus and Poisson's ratio are $E = 3 \times 10^7 \text{ psi}$ and $\nu = 0.3$, respectively. Self weight is included in the analysis.

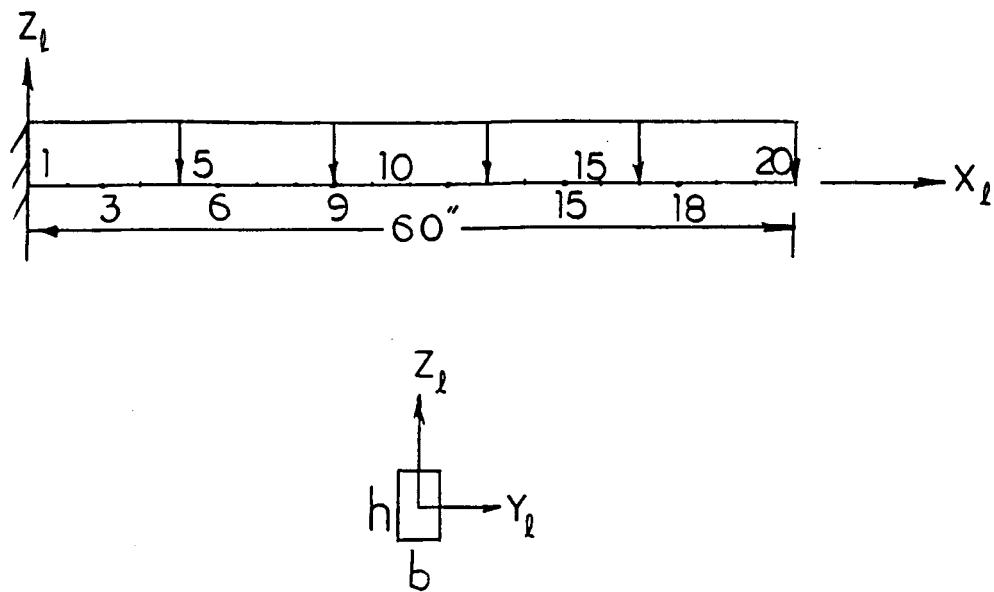


Figure 8. Cantilever Beam Finite Element Model

The compliance sensitivity results are shown in Table 4, where $\Delta\psi_4 = \psi_4(u + \delta u) - \psi_4(u)$ and ψ'_4 is the predicted value calculated from Eq. (39), with design perturbations of $\delta b = 0.05b$, $\delta h = 0.05h$ and $\delta b = 0.01b$, $\delta h = 0.01h$.

Table 4. Beam Design Sensitivity Check for Compliance

| δh | δb | $\psi_4(u)$ | $\psi_4(u + \delta u)$ | $\Delta\psi_4$ | ψ'_4 | % Accuracy |
|------------|------------|-------------|------------------------|----------------|-----------|------------|
| 0.05h | 0.05b | 1.3684 | 1.3153 | -0.0531 | -0.0601 | 113.1 |
| 0.01h | 0.01b | 1.3684 | 1.3566 | -0.0118 | -0.0120 | 102.0 |

These results show that nonlinearities in the compliance of the cantilevered beam are highly evident. If too large a perturbation in design is chosen, the sensitivity will be inaccurate.

Several discrete points along the beam are selected to check the accuracy of design sensitivity of the displacement functional of Eq. (44). In order to calculate this equation, the beam curvature due to the adjoint load is needed. Since the adjoint load is just a unit point load at the point \hat{x} acting in the $-z$ direction, a restart of the finite element analysis is all that is needed. Displacement results are shown in Table 5 for design perturbations of $\delta b = 0.05b$, $\delta h = 0.05h$ and $\delta b = 0.01b$, $\delta h = 0.01h$.

In both Tables 5(a) and 5(b), results show that the design sensitivity compared to the finite difference approximation is good, with the exception of node 3. Since the finite difference approximation is not too small in comparison to the constraint functional, loss of significant digits is not a valid reason for this inconsistency. The accuracy decreases as the node location approaches the restrained end of the beam. This is most likely due to the restraining effect, which causes rigidity in the beam and in turn gives smaller deflections.

To check the stress constraint sensitivity of Eq. (52), the equivalent nodal force of the adjoint load on the right side of Eq. (51) has to be calculated so that the curvature $\lambda_{xx}^{(6)}_l$ is known for each constraint element. This is accomplished by a restart of the original IFAD model, with each adjoint load for each element being a separate loading case. Allowable bending stress results for several finite elements are shown in Table 6 for a design perturbation of $\delta h = 0.05h$ and $\delta b = 0.05b$.

Table 5. Beam Design Sensitivity Check for Displacement

(a) $\delta b = 0.01b$ and $\delta h = 0.01h$

| Node | $\psi_5(u)$ | $\psi_5(u+\delta u)$ | $\Delta\psi_5$ | ψ'_5 | $\psi'_5 \times 100 / \Delta\psi_5$ |
|------|-------------|----------------------|----------------|--------------|-------------------------------------|
| 3 | 7.8353E-03 | 7.6473E-03 | -1.8804E-04 | -1.6082E-04 | 85.5 |
| 6 | 4.4162E-02 | 4.3102E-00 | -1.0604E-03 | -9.9992E-04 | 94.2 |
| 9 | 1.0181E-01 | 9.9365E-02 | -2.4451E-03 | -2.3554E-03 | 96.3 |
| 12 | 1.7317E-01 | 1.6901E-01 | -4.1590E-03 | -4.0441E-03 | 97.2 |
| 15 | 2.5229E-01 | 2.4623E-01 | -6.0594E-03 | -5.39211E-03 | 97.7 |
| 18 | 3.3493E-01 | 3.2686E-01 | -8.0447E-03 | -7.8836E-03 | 97.9 |
| 21 | 4.1857E-01 | 4.0852E-01 | -1.0054E-02 | -9.8701E-03 | 98.2 |

(b) $\delta b = 0.05b$ and $\delta h = 0.05h$

| Node | $\psi_5(u)$ | $\psi_5(u+\delta u)$ | $\Delta\psi_5$ | ψ'_5 | $\psi'_5 \times 100 / \Delta\psi_5$ |
|------|-------------|----------------------|----------------|-------------|-------------------------------------|
| 3 | 7.8353E-03 | 6.9743E-03 | -8.6100E-04 | -8.0412E-04 | 93.4 |
| 6 | 4.4162E-02 | 3.9306E-02 | -4.8555E-03 | -4.9959E-04 | 102.9 |
| 9 | 1.0181E-01 | 9.0619E-02 | -1.1120E-02 | -1.1777E-02 | 105.2 |
| 12 | 1.7317E-01 | 1.5412E-01 | -1.9043E-02 | -2.0220E-02 | 106.2 |
| 15 | 2.5229E-01 | 2.2454E-01 | -2.7745E-02 | -2.9605E-02 | 106.7 |
| 18 | 3.3493E-01 | 2.9810E-01 | -3.6835E-02 | -3.9418E-02 | 107.0 |
| 21 | 4.1857E-01 | 3.7253E-01 | -4.6034E-02 | -4.9350E-02 | 107.2 |

Table 6. Beam Design Sensitivity Check for Stress

| El. | $\psi_6(u)$ | $\psi_6(u+\delta u)$ | $\Delta\psi_6$ | ψ'_5 | $\psi'_5 \times 100 / \Delta\psi_6$ |
|-----|-------------|----------------------|----------------|-----------|-------------------------------------|
| 1 | 4932.767 | 4609.263 | -323.504 | -349.234 | 108.0 |
| 5 | 3110.255 | 2906.201 | -204.055 | -219.226 | 107.4 |
| 10 | 1420.622 | 1327.375 | -93.287 | -99.103 | 106.2 |
| 15 | 385.008 | 359.664 | -25.344 | -26.076 | 102.9 |
| 20 | 3.295 | 3.067 | -0.228 | -0.147 | 64.7 |

Near the end of the beam, where the allowable bending stress is near zero, the design sensitivity decreases significantly. Since the design sensitivity is the derivative of the constraint functional, and the derivative is physically interpreted as the slope of the beam, this decrease can be attributed to the large increase in slope at the free end of the beam.

3.3 Bending of Plates

The clamped plate finite element model shown in Fig. 9 is uniformly loaded with a pressure $f(x) = -1.5 \text{ lb/in.}$ in the z direction. Since the model is symmetric along two planes, only one quarter of it needs to be analyzed and symmetric boundary conditions need to be applied. The quarter model contains 100 IFAD triangular thin shell elements of type 1601, with only the bending terms active. It has 61 nodal points and 140 degrees-of-freedom.

The design variable is the plate thickness $u = t(x)$, and the material property constants, Young's Modulus and Poisson's ratio, are $E = 30.5 \times 10^6 \text{ psi}$ and $\nu = 0.3$, respectively. The constant plate thickness is $t = 0.4 \text{ in.}$ and the self-weight of the plate is neglected.

Compliance sensitivity results are shown in Table 7, where $\Delta\psi_7 = \psi_7(t + \delta t) - \psi_7(t)$ and ψ_7' is the predicted value calculated from Eq. (60), with design perturbations of $\delta t = 0.01t$ and $\delta t = 0.05t$.

Both perturbations for the compliance constraint functional give good correlation between the design sensitivity and the finite difference approximation. This implies that a five percent change in thickness is acceptable when making design improvements.

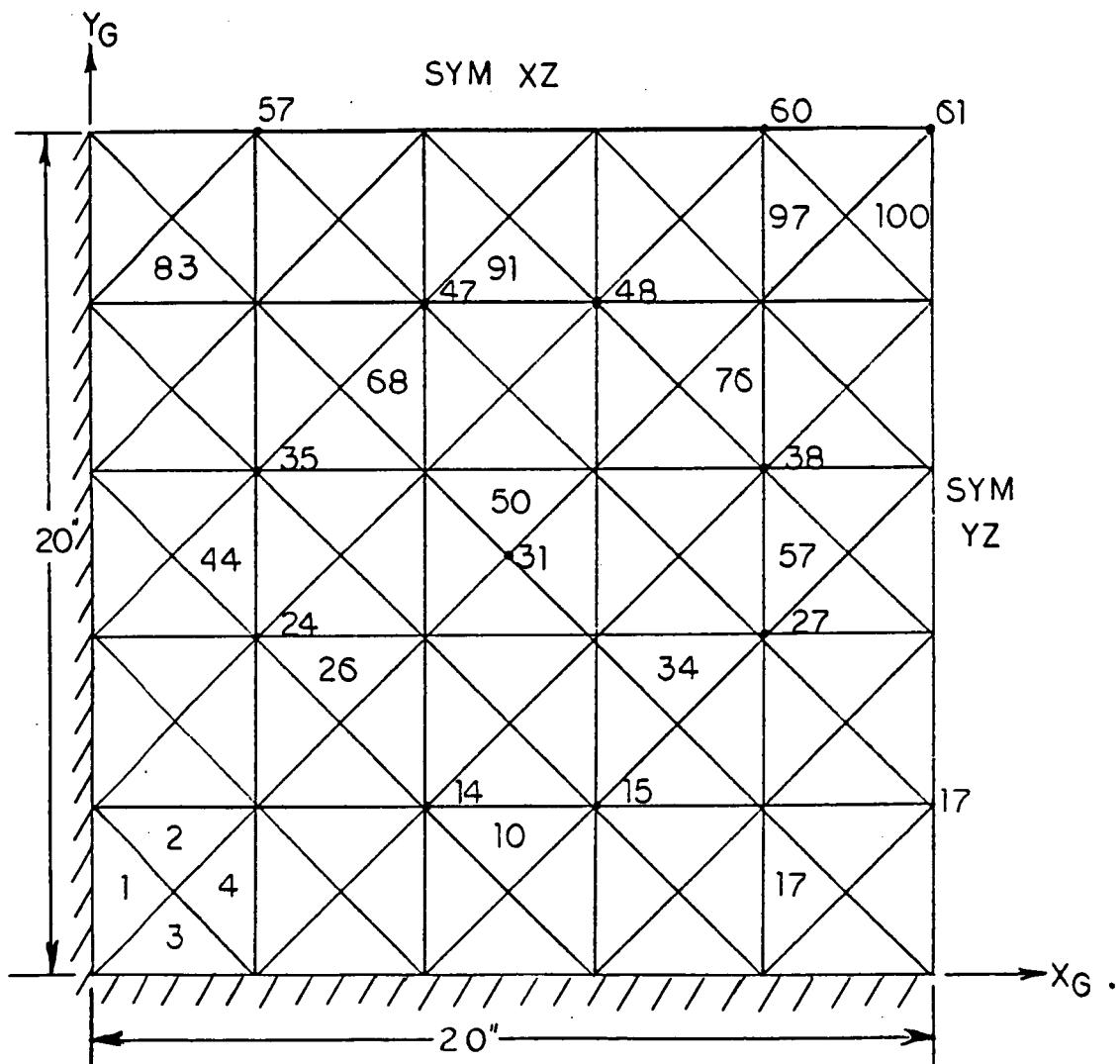


Figure 9. Bending Plate Finite Element Model

Table 7. Plate Design Sensitivity Check for Compliance

| δt | $\psi_7(t)$ | $\psi_7(t+\delta t)$ | $\Delta\psi_7$ | ψ'_7 | $\psi'_7 \times 100 / \Delta\psi_7$ |
|------------|-------------|----------------------|----------------|-----------|-------------------------------------|
| .05t | 4.9625 | 4.2868 | -0.6757 | -0.7204 | 106.6 |
| .01t | 4.9625 | 4.8165 | -0.1459 | -0.1441 | 98.7 |

Several discrete points in Fig. 8 are selected to check accuracy of the design sensitivity of the displacement functional in Eq. (69). In order to calculate this equation, just as in the membrane case, the strain $\epsilon^{ij}(\lambda^{(8)})$ due to the adjoint load is needed. A restart of the finite element analysis, using a unit point load in the -z direction for each selected point as a separate load case, accomplishes this task. Some displacement results are shown in Table 8 for a design perturbation of $\delta t = 0.01t$.

Table 8. Plate Design Sensitivity Check for Displacement

| Node | $\psi_8(t)$ | $\psi_8(t+\delta t)$ | $\Delta\psi_8$ | ψ'_8 | $\psi'_8 \times 100 / \Delta\psi_8$ |
|------|-------------|----------------------|----------------|-------------|-------------------------------------|
| 14 | 1.9033E-03 | 1.8473E-03 | -5.5976E-05 | -5.2596E-05 | 94.0 |
| 15 | 3.0497E-03 | 2.9600E-03 | -8.9692E-05 | -8.5144E-05 | 94.9 |
| 24 | 1.9033E-03 | 1.8473E-03 | -5.5976E-05 | -5.2596E-05 | 94.0 |
| 27 | 1.1258E-02 | 1.0927E-02 | -3.3109E-04 | -3.2620E-04 | 98.5 |
| 31 | 9.7772E-03 | 9.4897E-03 | -2.8754E-04 | -2.8309E-04 | 98.4 |
| 35 | 3.0497E-03 | 2.9600E-03 | -8.9692E-05 | -8.5144E-05 | 94.9 |
| 38 | 1.8450E-02 | 1.7908E-02 | -5.4262E-04 | -5.3957E-04 | 99.4 |
| 47 | 1.1258E-02 | 1.0927E-02 | -3.3109E-04 | -3.2620E-04 | 98.5 |
| 48 | 1.8450E-02 | 1.7908E-02 | -5.4262E-04 | -5.3957E-04 | 99.4 |
| 57 | 4.2639E-03 | 3.9443E-03 | -1.1952E-04 | -1.1410E-04 | 95.5 |
| 60 | 2.5084E-02 | 2.4366E-02 | -7.3773E-04 | -7.3688E-04 | 99.9 |
| 61 | 2.6942E-02 | 2.6150E-02 | -7.9237E-04 | -7.9223E-04 | 100.0 |

The design sensitivity results of Table 8 seem to substantiate the fact that nodes near a clamped edge give a somewhat less accurate prediction of the design sensitivity. However, these results are still considered good, since there is less than 15% deviation from the approximate finite difference result. Since the finite difference result is only an approximation, it is reasonable to say that the design sensitivity prediction is good every where along the plate.

A number of elements are selected to check the design sensitivity for von Mises' stress in Eq. (80). Before this can be evaluated, the nodal force of the adjoint load on the right side of Eq. (79) has to be calculated so that the strain $\epsilon^{ij}(\lambda^{(9)})$ is known for each constraint element. This is accomplished by a restart of the original IFAD model with each adjoint load for each element being a separate loading case. Von Mises' stress results are shown in Table 9 for a design perturbation of $\delta t = 0.001t$.

Recall that the design sensitivity and the constraint functional was calculated using an integration technique where the stresses were calculated at the midside nodes of the triangular element. This integration technique was used so as to get the best design sensitivity results as possible for the finite elements. This is the technique used because the element is a hybrid element [4]. The results in Table 9 are excellent when this technique is used. These results further substantiate the fact that as design perturbation approaches zero, $\psi/\Delta\psi$ approaches one.

Table 9. Plate Design Sensitivity Check for von Mises' Stress

| El. No. | $\psi_9(t)$ | $\psi_9(t+\delta t)$ | $\Delta\psi_9$ | ψ'_9 | $\psi'_9 \times 100 / \Delta\psi_9$ |
|---------|-------------|----------------------|----------------|-----------|-------------------------------------|
| 1 | 172.1862 | 171.8423 | -0.3439 | -0.3445 | 100.17 |
| 2 | 752.7383 | 751.2351 | -1.5032 | -1.5049 | 100.11 |
| 3 | 172.1861 | 171.8423 | -3.4386 | -3.4446 | 100.17 |
| 4 | 752.7383 | 751.2351 | -1.5032 | -5.0495 | 100.11 |
| 10 | 1442.8840 | 1140.0025 | -2.8815 | -2.8841 | 100.09 |
| 17 | 2457.3522 | 2452.4447 | -4.9074 | -4.9125 | 100.10 |
| 25 | 1149.0097 | 1146.7151 | -2.2947 | -2.2970 | 100.11 |
| 26 | 1331.9565 | 1329.2966 | -2.6600 | -2.6624 | 100.10 |
| 27 | 1149.0097 | 1146.7151 | -2.2946 | -2.2970 | 100.11 |
| 28 | 1331.9565 | 1329.2966 | -2.6600 | -2.6662 | 100.09 |
| 34 | 973.8975 | 971.9526 | -1.9450 | -1.9465 | 100.08 |
| 44 | 1442.8840 | 1440.0025 | -2.8815 | -2.8841 | 100.09 |
| 49 | 1284.1558 | 1281.5913 | -2.5645 | -2.5667 | 100.08 |
| 50 | 1278.5066 | 1275.9534 | -2.5532 | -2.5554 | 100.09 |
| 51 | 1274.1558 | 1281.5913 | -2.5645 | -2.5667 | 100.08 |
| 52 | 1278.5066 | 1275.9531 | -2.5532 | -2.5554 | 100.09 |
| 57 | 1110.0286 | 1107.8118 | -2.2168 | -2.2188 | 100.09 |
| 68 | 973.8975 | 971.9526 | -1.9449 | -1.9465 | 100.08 |
| 73 | 1470.1247 | 1417.2887 | -2.8360 | -2.8384 | 100.08 |
| 74 | 1629.1926 | 1625.9391 | -3.2536 | -3.2563 | 100.08 |
| 75 | 1420.1247 | 1417.2887 | -2.8360 | -2.8384 | 100.08 |
| 76 | 1629.1926 | 1625.9391 | -3.2536 | -3.2561 | 100.08 |
| 83 | 2457.3522 | 2452.4447 | -4.9074 | -4.9125 | 100.10 |
| 91 | 1110.0286 | 1107.8118 | -2.2168 | -2.2188 | 100.09 |
| 97 | 1884.4503 | 1880.6870 | -3.7633 | -3.7660 | 100.07 |
| 98 | 2010.1163 | 2006.1021 | -4.0143 | -4.0170 | 100.07 |
| 99 | 1884.4503 | 1880.6870 | -3.7633 | -3.7660 | 100.07 |
| 100 | 2010.1663 | 2006.1021 | -4.0143 | -4.0170 | 100.07 |

3.4 Built-Up Structure

A built-up structure that uses both beams and plates is shown in Fig. 10. Since it is symmetric along two planes, only a quarter is modeled. The built-up structure is clamped on two edges, with symmetric boundary conditions applied along the other two edges. The plates and the beams are considered to be welded. A uniform pressure $f(x) = -1.5 \text{ lb/in.}^2$ is applied on the top surface of the plates. The model contains 100 IFAD triangular thin shell elements of type 1601, with only the bending terms active, and 20 IFAD beam elements of type 0501. There are 61 nodal points and 140 degrees-of-freedom. There are three design variables, beam width, beam height, and plate thickness. The material constants, Young's modulus and Poisson's ratio, for both the beams and the plates are $E = 30.5 \times 10^6 \text{ psi}$ and $\nu = 0.3$, respectively. Self weight is neglected and the initial design variables are $b = 0.5 \text{ in.}$, $h = 0.75 \text{ in.}$, and $t = 0.4 \text{ in.}$

Compliance sensitivity results are shown in Table 10, where $\Delta\psi_{11} = \psi_{10}(u + \delta u) - \psi_{10}(u)$ and ψ'_{11} is the predicted design sensitivity, using Eq. (101) with a 1% design perturbation for all the design variables.

Several discrete points in Fig. 10 are selected to check the accuracy of design sensitivity of the displacement functional in Eq. (104). To calculate this equation, the strain $\epsilon^{ij}(\lambda)^{(12)}$ due to the adjoint load is obtained by doing a restart of the finite element analysis. A unit point load in the $-z$ direction for each selected point

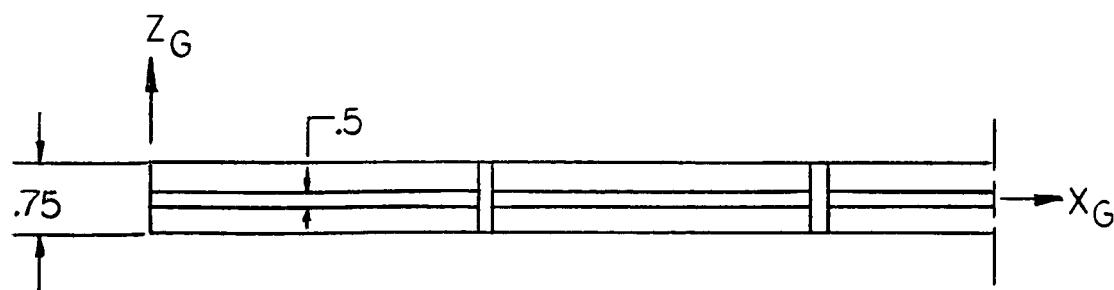
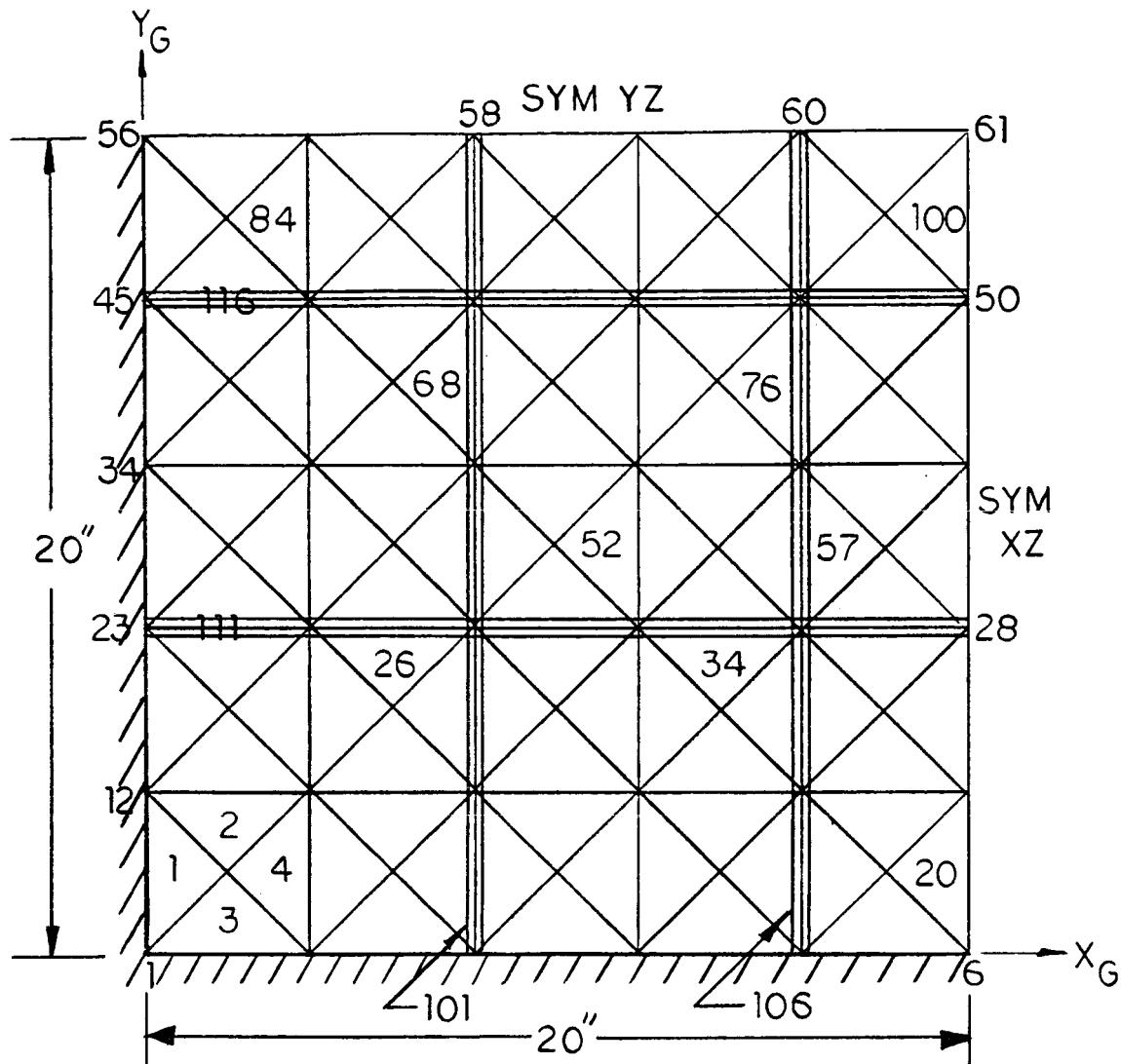


Figure 10. Built-up Structure Finite Element Model

Table 10. Built-up Structure Design Sensitivity
Check for Compliance with $\delta h = 0.01h$
 $\delta b = 0.01b$, and $\delta t = 0.01t$

| $\psi_{11}(u)$ | $\psi_{11}(u+\delta u)$ | $\Delta\psi_{11}$ | ψ'_{11} | $\psi'_{11} \times 100 / \Delta\psi_{11}$ |
|----------------|-------------------------|-------------------|--------------|---|
| 3.7200 | 3.6017 | -0.1183 | -0.1189 | 100.5 |

is specified as a separate load case. The design sensitivity results for these selected points are shown in Table 11, where a 1% perturbation for each design variable is used.

Table 11. Built-up Structure Design Sensitivity
Check for Displacement with $\delta h = 0.01h$,
 $\delta b = 0.01b$, and $\delta t = 0.01t$

| Node | $\psi_{12}(u)$ | $\psi_{12}(u+\delta u)$ | $\Delta\psi_{12}$ | ψ'_{12} | $\psi'_{12} \times 100 / \Delta\psi_{12}$ |
|------|----------------|-------------------------|-------------------|--------------|---|
| 13 | 4.768E-04 | 4.616E-04 | -1.520E-05 | -1.453E-05 | 95.6 |
| 15 | 2.294E-06 | 2.222E-03 | -7.283E-05 | -6.750E-05 | 92.7 |
| 17 | 3.064E-03 | 2.966E-03 | -9.723E-05 | -9.152E-05 | 94.1 |
| 25 | 4.125E-03 | 3.994E-03 | -1.313E-04 | -1.255E-04 | 95.6 |
| 27 | 5.421E-03 | 8.153E-03 | -2.680E-04 | -2.621E-04 | 97.8 |
| 35 | 2.294E-03 | 2.221E-03 | -7.283E-05 | -6.750E-05 | 92.7 |
| 37 | 1.095E-02 | 1.060E-02 | -3.484E-04 | -3.448E-04 | 99.0 |
| 39 | 1.485E-02 | 1.438E-02 | -4.724E-04 | -4.737E-04 | 100.3 |
| 47 | 8.421E-03 | 8.153E-03 | -2.680E-04 | -2.621E-04 | 97.8 |
| 49 | 1.755E-02 | 1.699E-02 | -5.580E-04 | -5.621E-04 | 100.7 |
| 55 | 1.955E-02 | 1.892E-02 | -6.215E-04 | -6.296E-04 | 101.3 |
| 57 | 3.064E-03 | 2.966E-03 | -9.723E-05 | -9.152E-05 | 94.1 |
| 59 | 1.485E-02 | 1.438E-02 | -4.724E-04 | -4.737E-04 | 101.3 |
| 61 | 2.025E-02 | 1.961E-02 | -6.439E-04 | -6.535E-04 | 101.5 |

Both the compliance and displacement design sensitivity results show good correlation with the approximated finite difference. This indicates that the method of design sensitivity is a good method for

predicting the response of a built-up structure for these constraint functionals. This is substantiated by the fact that correlation between the design sensitivities and the finite difference approximations for the built-up structure in Tables 10 and 11 are not that different than those in Tables 7 and 8 where plate bending results are shown.

To check the stress constraint sensitivity of Eq. (98), the equivalent nodal force of the adjoint load on the right of Eq. (97) has to be calculated so that $\epsilon^{ij}(\lambda)^{(10)}$ is known for each constrained element. A restart of the original IFAD built-up structure model is made, with each adjoint load for a finite element being a separate loading case. The design sensitivity results for the von Mises' stress functional are given in Table 12, with design perturbation $\delta t = 0.001t$.

The design sensitivity results compared to the finite difference approximations fluctuate more than would be expected, considering the excellent correlation of the von Mises' stress design sensitivities for the bending plate in Table 9. It doesn't appear that the problem is caused by the design perturbation being too small, because the finite difference approximation is no smaller than three significant digits of the actual constraint functional. It is possible that the nonlinear response of the built-up structure is partially the cause of the inconsistencies in the design sensitivities, but not the whole problem, since the design perturbation is quite small.

It is most likely that the beam contribution to the built-up structure is the major influence. The beam seems to be more influenced

by nonlinearities, as shown in Tables 4, 5, and 6. It is most probable that if a more complex beam element, such as a cubic beam, was used, design sensitivity results would improve. Unfortunately the IFAD code does not currently support this type of beam, so this cannot be verified in this study.

Table 12. Built-up Structure Design Sensitivity Check
for von Mises' Stress with $\delta t = 0.001t$,
 $\delta b = 0.001b$, and $\delta h = 0.001h$

| Element | $\psi_{10}(t)$ | $\psi_{10}(t+\delta t)$ | $\Delta\psi_{10}$ | ψ'_{10} | $\psi'_{10} \times 100 / \Delta\psi_{10}$ |
|---------|----------------|-------------------------|-------------------|--------------|---|
| 1 | 127.8318 | 127.5490 | -0.2828 | -0.3339 | 118.1 |
| 2 | 549.7750 | 548.5339 | -1.2411 | -1.2230 | 98.5 |
| 3 | 127.8318 | 127.5490 | -0.2828 | -0.3339 | 118.1 |
| 4 | 549.7750 | 548.5339 | -1.2411 | -1.2230 | 98.5 |
| 10 | 1074.7414 | 1072.3202 | -2.4212 | -2.7653 | 114.2 |
| 17 | 1828.5601 | 1824.4411 | -4.1190 | -4.2965 | 104.3 |
| 25 | 875.4135 | 873.4610 | -1.9525 | -2.3201 | 118.1 |
| 26 | 985.6012 | 983.3797 | -2.2215 | -2.6663 | 120.0 |
| 27 | 875.4135 | 873.4610 | -1.9525 | -2.3201 | 118.1 |
| 28 | 985.6012 | 983.3747 | -2.2215 | -2.6663 | 120.0 |
| 34 | 735.6485 | 734.0066 | -1.6419 | -2.2807 | 138.9 |
| 44 | 1074.7414 | 1072.3202 | -2.4212 | -2.7653 | 114.2 |
| 50 | 962.8944 | 960.7381 | -2.1563 | -2.4538 | 113.8 |
| 51 | 944.5642 | 942.4288 | -2.1354 | -2.7966 | 131.0 |
| 57 | 804.5913 | 802.7656 | -1.8257 | -2.2406 | 122.7 |
| 68 | 735.6485 | 734.0066 | -1.6420 | -2.2807 | 138.9 |
| 73 | 1074.1010 | 1071.6982 | -2.4028 | -2.7000 | 112.6 |
| 74 | 1243.6633 | 1240.8853 | -2.7780 | -3.2605 | 117.4 |
| 75 | 1074.1010 | 1071.6982 | -2.4028 | -2.7060 | 112.6 |
| 76 | 1243.6633 | 1240.8853 | -2.7780 | -3.2605 | 117.4 |
| 83 | 1828.5601 | 1824.4411 | -4.1190 | -4.2965 | 104.3 |
| 91 | 804.5913 | 802.7656 | -1.8257 | -2.2406 | 122.7 |
| 97 | 1401.1703 | 1398.0144 | -3.1559 | -3.2171 | 101.9 |
| 98 | 1517.4522 | 1514.0511 | -3.4011 | -3.6964 | 108.7 |
| 99 | 1401.1703 | 1398.0144 | -3.1559 | -3.2171 | 101.9 |
| 100 | 1517.4522 | 1514.0511 | -3.4011 | -3.6964 | 108.7 |

CHAPTER IV

CONCLUSIONS

The results of this study indicate that it is feasible to implement the theoretical design sensitivity analysis of Ref. 1 with an existing finite element code. Calculations of the design sensitivities can be accomplished outside of the finite element code using only the postprocessing data. In addition, the results show that accurate design sensitivity can be predicted without the uncertainty of numerical accuracy associated with the selection of a finite difference perturbation. However, results also indicate that the integration technique used in the calculation of the design sensitivity and the knowledge of the exact finite element shape functions used for each finite element in the finite element code is important in getting the most accurate design sensitivities possible.

Results of the built-up structure indicate that design sensitivities of the built-up structure cannot be any more accurate than the accuracy of the individual components. Care must be taken to use the best integration techniques and the same shape functions as the finite element analysis for the individual components, if at all possible.

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3. "Aplicon IFAD User's Guide," Aplicon, Inc. Cleveland, Ohio, 1983.
4. Razzaque, Abdur, "Program for Triangular Bending Elements with Derivative Smoothing," Int. Journal for Num. Methods in Eng., Vol 6, 1973, pp. 333-343.
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APPENDIX
DESIGN SENSITIVITY IFAD PROGRAM

```

PROGRAM SENSIT
CP*****
CP*
CP* SENSIT: THE MAIN PROGRAM FOR CALCULATING DESIGN SENSITIVITY
CP*
CP*****
CP*
CP* DESCRIPTION:
CP*
CP*      'SENSIT' IS THE MAIN PROGRAM FOR THE DESIGN SENSITIVITY
CP*      VECTOR CALCULATION. IT CHECKS THE ACCURACY OF THE
CP*      SENSITIVITY TO THE FINITE DIFFERENCE METHOD IF THE
CP*      TWO FINITE ELEMENT ANALYSES ( THE ORIGINAL ANALYSIS
CP*      AND THE PERTURBED ANALYSIS ) ARE ALREADY CREATED.
CP*      MAX. OF 500 ELEMENTS. IF MORE ELEMENTS ARE NEEDED THE
CP*      SVECTR.MON COMMON BLOCK FILE NEEDS TO CHANGED.
CP*
CP*****
INCLUDE 'AEGRSDR.INC' IMPLIC.SPC'
INCLUDE 'AEGRSDR.INC' CNTL.MON'
INCLUDE 'AEGRSDR.INC' SVECTR.MON'

C      EQUIVALENCE (NDAT(46),NELM),(NDAT(181),IPNAME)
C      DIMENSION PS1B(2),IPNAME(2),IPNAM1(2),IPNAM2(2)
C      CHARACTER YESNO*1

C      NT = 0
C      ISAC = 0
C      LCS = 1
C      NLC = 1

C      ASK FOR FINITE ELEMENT MODEL FILE NAME
C
C      PRINT *,'
C      PRINT *,'ENTER THE ORIGINAL PROBLEM NAME (1-8 CHARS)'
C      READ(5,1009) IPNAM1

C      ASK FOR CONSTRAINT TYPE
C
C      PRINT *,'
C      PRINT *,'ENTER CONSTRAINT TYPE: 1 = COMPLIANCE'
C      PRINT *,'                                2 = DISPLACEMENT'
C      PRINT *,'                                3 = STRESS'
C      READ(5,1006) ICT
C      IF(ICT.NE.3) GO TO 20
C      PRINT *,'
C      PRINT *,'ENTER STRESS TYPE: 1 = PRINCIPAL'
C      PRINT *,'                                2 = VON MISES'
C      PRINT *,'                                3 = BEAM ALLOWABLE'
C      READ(5,1006) IST

C      20   PRINT *,'CALCULATING ADJOINT LOADS (Y/N) ?'
C      READ(5,1000) YESNO
C      IF(YESNO.EQ.'Y') ISAC = 1
C      IF(ISAC.EQ.1) GO TO 40

C      ASK FOR THE PERTURBED FINITE ELEMENT NAME
C
C      PRINT *,'

```

```

      PRINT *, 'ENTER THE PERTURBED PROBLEM NAME (1-8 CHARS)'
      READ(5,1009) IPNAM2
C
C   OPEN AN OUTPUT FILE
C
      OPEN(UNIT=10,NAM='RESULT.DAT',TYPE='NEW')
      WRITE(10,1007) ICT
      IF(ICT.NE.3) GO TO 40
      WRITE(10,1008) IST
C
C   GET LOAD CASE START AND END NOS.
C
40   PRINT *, ''
      PRINI *, 'ENTER NO. OF LOAD CASES TO BE PROCESSED'
      READ(5,1006) NLC
      PRINI *, 'ENTER FIRST LOAD CASE NO.'
      READ(5,1006) LCS
50   LCS = LCS - 1
C
C   GET CONSTRAINED ELEMENTS FOR STRESS CALCULATION
C
      IF(ICT.NE.3) GO TO 90
      PRINI *, ''
      IF(ISAC.EQ.1) GO TO 60
      PRINT 2000, NLC
      GO TO 70
C
C   GET ELEMENTS FOR ADJOINT LOAD CALCULATION
C
60   PRINT 2001, NLC
70   DO 80 NE=1,NLC
80   READ(5,1006) ICE(NE)
90   DO 800 NC=1,NLC
      IF(ISAC.EQ.1) GO TO 100
      WRITE(10,1010) ICE(NC)
C
C   GET SENSITIVITY VECTOR
C
100  IF(NT.EQ.1) GO TO 110
      IPNAME(1) = IPNAM1(1)
      IPNAME(2) = IPNAM1(2)
      GO TO 120
110  IPNAME(1) = IPNAM2(1)
      IPNAME(2) = IPNAM2(2)
120  CALL GETSEN(PSIR,NT,NELM,IPNAME)
      IF(ISAC.EQ.1) GO TO 410
      IF(NT.GT.1) GO TO 200
      GO TO 100
C
C   CALC. CHANGE IN PLATE THICKNESS, CHANGE IN BEAM WIDTH AND DEPTH
C
200  NI = 0
      DT = DABS(TM(2)-TM(1))
      DR = DABS(BW(2)-BW(1))
      DH = DABS(BH(2)-BH(1))
      TB = DABS(PB(2)-PB(1))
C
C   CALCULATE THE PERCENT ACCURACY
C
      DFSIRDB = 0.0
      DO 300 I=1,NELM

```

```

      DPSIBDB = DPSIRDB+DPSIT(1)*HT+DPSIR(I)*DR
      *          +DPSIH(I)*DH+DPSITH(I)*TH
300   CONTINUE
      PNUM = DPSIRDB*100
400   PIEN = PSIB(2)-PSIH(1)
      IF(PDEN.EQ.0) GO TO 801
      PACCUR = PNUM/PIEN
C
      WRITE(10,*)
      WRITE(10,1004) HT,DB,DH,TH
      WRITE(10,1005) PIEN
      WRITE(10,1002) DPSIRDB
      WRITE(10,1003) PACCUR
800   CONTINUE
C
      GO TO 900
C
901   PRINT *, 'DPSI(B)*DR = 0'
C
900   CLOSE(10)
910   CONTINUE
C
C
1000  FORMAT(A)
1001  FORMAT(F8.5)
1002  FORMAT(1X,'DPSI(H)*DELTAB=',E16.8)
1003  FORMAT(1X,'PERCENT ACCURACY=',F16.8)
1004  FORMAT(1X,'CHANGE IN MEMBRANE THICKNESS =',F8.5,/,1X,'CHANGE
      * IN BEAM WIDTH =',F8.5,/,1X,'CHANGE IN BEAM DEPTH =',F8.5,
      */,1X,'CHANGE IN BENDING PLATE THICKNESS =',F8.5)
1005  FORMAT(1X,'PSI(B+DB) - PSI(H) = ',F16.8)
1006  FORMAT(I4)
1007  FORMAT(1X,'***CONSTRAINT TYPE =',I4)
1008  FORMAT(/,1X,'***STRESS TYPE =',I4)
1009  FORMAT(2A4)
1010  FORMAT(1X,'CONSTRAINT ELEMENT IS ',I4)
2000  FORMAT(1X,'ENTER',I4,' CONSTRAINT ELEMENTS, FOLLOW EACH BY
      * A RETURN')
2001  FORMAT(1X,'ENTER',I4,' ELEMENTS THAT ARE TO HAVE AN ADJOINT
      * LOAD CALCULATED. FOLLOW EACH BY A RETURN.')
C
C
      END

```

```

SUBROUTINE AL16(X,Y,C,AL,TB,THK,IT)
C*****
C*
C* AL16: ADJOINT LOAD CALCULATION FOR TRIANGULAR ELEMENT 1601
C*
C*****
C* DESCRIPTION:
C*
C*      'AL16' CALCULATES THE ADJOINT LOADS FOR THE TRIANGULAR
C* PLATE BENDING ELEMENT. AL = [C]*[R]*XMP WHERE
C* [C] IS THE DERIVATIVE OF THE STRESS FUNCTION VECTOR
C* TIMES THE ELASTICITY MATRIX. SINCE SFAN CALCULATES
C* STRESS RESULTANT'S FIRST, [AL] MUST BE MULTIPLIED BY
C* PLATE THICKNESS DIVIDE BY 2.
C* [R] IS A 3X9 MATRIX IN COLUMNS 4,5 & 6 OF [W]. XMP
C* IS THE CHARACTERISTIC FUNCTION THAT IS 1/AREA OF THE
C* ELEMENT THAT IS CONSTRAINED AND ZERO FOR ALL THE OTHER
C* ELEMENTS.
C*
C*****
C*      X      THE LOCAL ELEMENT X COORDINATE
C*      Y      THE LOCAL ELEMENT Y COORDINATE
C*      C      MATRIX [C] = [DG]*[E0]*T/2   3X3 MATRIX
C*      AL     ADJOINT LOAD VECTOR
C*      TB     TRANSFORMATION MATRIX
C*      THK    MATERIAL THICKNESS
C*      IT     MIDSIDE NODE COLUMN LOCATOR
C*
C*****
C
C      INCLUDE 'LAEGSDR.INC' IMPL1C.SPC'
C      INCLUDE 'LAEGSDR.INC' CNTL.MDN'
C
C      EQUIVALENCE (NJIA1(14),IPR)
C
C      DIMENSION X(3),Y(3),GPTS(3,3),XL(6),YL(6),W(18,7),C(3),
C      *          F(9),AL(18),R(6,3),TB(6,6),RP(6,3)
C
C      DATA GPTS/.000,.500,.500,  .500,0.000,.500,  .500,.500,0.000/
C
C*** INITIALIZE VARIABLES
C
C      DO 10 I=1,9
10    F(I) = 0.000
      DO 12 I=1,18
12    AL(18) = 0.000
      DO 14 I=1,6
      DO 14 J=1,3
         R(I,J) = 0.000
14    CONTINUE
C
C      AREA = EUTRIA(X,Y)
C      XMP = 1.00/AREA
C
C*** GET LOCAL X AND Y COORDINATES
C
C      CALL MOVESP(XL,X,3*IPR)
C      CALL MOVESF(YL,Y,3*IPR)
C      CALL SF1501(XL,YL,GPTS(1,11),W,EM)

```

```
      DO 50 M=1,9
      GASH = 0.0D0
      DO 40 J=1,3
         GASH = GASH+L(J)*W(M,J+3)
40      CONTINUE
         F(M) = F(M)+GASH*XMP
50      CONTINUE
C
C** ROTATE ADJOINT LOAD VECTOR TO GLOBAL COORDINATE SYSTEM
C
      N = 1
      DO 60 MM=1,3
         R(3,MM) = F(N)
         R(4,MM) = F(N+1)
         R(5,MM) = F(N+2)
         N = N+3
60      CONTINUE
      CALL UMXAB(18,R,RF,6,3,6)
      N1 = 0
      DO 80 M=1,3
         DO 70 M1=1,6
            AL(M1+N1) = RF(M1,M)
70      CONTINUE
         N1 = N1+6
80      CONTINUE
      DO 90 N2 = 1,18
         AL(N2) = AL(N2)*THK/2.0D0
90      CONTINUE
C
C
      RETURN
END
```

```

        FUNCTION AREAQ(X,Y)
C*****
C*
C* AREAQ: CALCULATES THE AREA OF A STRAIGHT SIDED FOUR OR
C*          EIGHT NODE ELEMENT.
C*
C*          X      GLOBAL X COORDINATES
C*          Y      GLOBAL Y COORDINATES
C*
C*****
C
C     INCLUDE 'CAEGS1R.INC' IMPLIC.SFC'
C     INCLUDE 'CAEGSDR.INC' ACCIPN.MON'
C     INCLUDE 'CAEGSDR.INC' ELEMS.MON'
C
C     DIMENSION X(4),X1(3),X2(3),Y(4),Y1(3),Y2(3),Z(4),BUF(100)
C
C     DATA IREF/1/
C
C**** CALCULATES THE AREA OF A QUADRILATERAL
C
C     IF(NUNPE.EQ.8)  GO TO 20
C
C   FOUR NODDED ELEMENT
C
C     X1(1) = X(1)
C     X1(2) = X(2)
C     X1(3) = X(4)
C     Y1(1) = Y(1)
C     Y1(2) = Y(2)
C     Y1(3) = Y(4)
C     A1 = EU1RIA(X1,Y1)
C     X2(1) = X(2)
C     X2(2) = X(3)
C     X2(3) = X(4)
C     Y2(1) = Y(2)
C     Y2(2) = Y(3)
C     Y2(3) = Y(4)
C     A2 = EU1RIA(X2,Y2)
C     GO TO 30
C
C   EIGHT NODDED ELEMENT WITH STRAIGHT SIDES
C
C20    X1(1) = X(1)
C     X1(2) = X(3)
C     X1(3) = X(5)
C     Y1(1) = Y(1)
C     Y1(2) = Y(3)
C     Y1(3) = Y(5)
C     A1 = EU1RIA(X1,Y1)
C     X2(1) = X(1)
C     X2(2) = X(5)
C     X2(3) = X(7)
C     Y2(1) = Y(1)
C     Y2(2) = Y(5)
C     Y2(3) = Y(7)
C     A2 = EU1RIA(X2,Y2)
C
C30    AREAQ = A1+A2

```

```
C      GO TO 900
C
807  PRINT 877, IERR
C
877  FORMAT(1X,'ACCELC RETURNED WITH ERROR', 14)
900  CONTINUE
C
RETURN
END
```

```

SUBROUTINE COMP(FSIB,NT,NELM)
CP*****COMP: BRANCHES TO THE APPROPRIATE ELEMENT TYPE TO CALCULATE
CP* DESCRIPTION:
CP*      'COMP' BRANCHES TO THE APPROPRIATE ELEMENT TYPE TO
CP*      CALCULATE THE COMPLIANCE AND THE COMPLIANCE SENSIT-
CP*      IVITY VECTOR.
CP*
C      INCLUDE 'DAEGSDR.INC' IMPLIC.SPC'
INCLUDE 'DAEGSDR.INC' ACC1PN.MON'
INCLUDE 'DAEGSDR.INC' CNTL.MON'
INCLUDE 'DAEGSDR.INC' ELEDES.MON'
INCLUDE 'DAEGSDR.INC' SVECTR.MON'
COMMON/LCSIDES/DLCS(90)
C      EQUIVALENCE (NDAT(97),IDBS),(NDAT(98),JNBL)
C      DIMENSION DA1N(50),FSIBB(500),FSIB(2),CFBUF(6),FSIBTB(500)
C      DATA IREF/1/
C
C      FSIB16 = 0.0
C      FSIRC5 = 0.0
C      SDPSIT = 0.0
C      SDFSIB = 0.0
C      SDPSIH = 0.0
C      SDPSTB = 0.0
C
C      SET LOAD CASE NUMBER FOR COMPLIANCE
C      L1 = LCS + NC
C
C      SETUP POINTERS
C
CALL ACCELM(1,IPNELM,1,0,0,IERR)
IF(IERR.NE.0) GO TO 800
CALL ACCFES(1,IPNFES,1,0,0,0,IERR)
IF(IERR.NE.0) GO TO 801
CALL ACCCN(1,IPNCN,1,0,0,0,IERR)
IF(IERR.NE.0) GO TO 802
CALL ACCLCS(1,IPNLCS,1,0,0,IERR)
IF(IERR.NE.0) GO TO 803
CALL ACCNOD(1,IPNNOD,1,0,0,IERR)
IF(IERR.NE.0) GO TO 806
CALL ACCEL(1,IPNELC,1,0,0,0,IERR)
IF(IERR.NE.0) GO TO 807
CALL ACCMAT(1,IPNMAT,1,0,0,0,IERR)
IF(IERR.NE.0) GO TO 808
CALL ACCEPR(1,IPNEPR,1,0,0,0,IERR)
IF(IERR.NE.0) GO TO 809
CALL ACCEEN(1,IPNEEN,1,0,0,0,IERR)
IF(IERR.NE.0) GO TO 810
C

```

```

C LOOP THROUGH THE ELEMENTS
C
C      DO 100 I=1,NELM
C             IF(I.GT.1) GO TO 50
C
C      GET INTERNAL LOAD CASE NUMBER
C
C      CALL ACCLCS(2,IPNLCS,L1,2,DLCs,IERR)
C             IF(IERR.NE.0) GO TO 805
C             ILCN = DLCs(21)
C
C      GET ELEMENT DESCRIPTORS
C
C      50     CALL ACCELM(2,IPNELM,I,2,IED,IERR)
C             IF(IERR.NE.0) GO TO 800
C
C      BRANCH TO THE APPROPRIATE ELEMENT TYPE
C
C             IF(ITYP.EQ.11) CALL COMP11(NT,I,ILCN)
C             IF(ITYP.EQ.5)  CALL COMPOS(NT,I,ILCN,PSIBB)
C             IF(ITYP.EQ.16) CALL CP16(NT,I,ILCN,PSIBTB)
C
C             PSIB16 = PSIB16+PSIBTB(I)
C             PSIBC5 = PSIBC5+PSIBB(I)
C             SDPSIT = SDPSIT+DPSIT(I)
C             SDPSIB = SDPSIB+DPSIB(I)
C             SDPSIH = SDPSIH+DPSIH(I)
C             SDPSTB = SDPSTB+DPSITB(I)
100    CONTINUE
C
C             IF(NT.GT.1) GO TO 720
C             WRITE(10,859)
C             DO 710 I=1,NELM
710    WRITE(10,857) I,DPSIT(I),DPSIB(I),DPSIH(I),DPSITE(I)
C             WRITE(10,861) SDPSIT,SDPSIB,SDPSIH,SDPSTB
C
720    IF(ITYP.EQ.11) CALL CPSI11(PSIBT,ILCN,IREF)
C
C             PSIB(NT) = PSIBT + PSIBC5 + PSIB16
C
C             WRITE(10,858) PSIB(NT)
C             PRINT 858, PSIB(NT)
C
C      CLEAN-UP EVERYTHING
C
C             CALL ACCELM(4,IPNELM,0,0,0,1ERR)
C             IF(IERR.NE.0) GO TO 800
C             CALL ACCFES(4,IPNFES,0,0,0,0,0,1ERR)
C             IF(IERR.NE.0) GO TO 801
C             CALL ACCCNID(4,IPNCNI,0,0,0,0,0,1ERR)
C             IF(IERR.NE.0) GO TO 802
C             CALL ACCLCS(4,IPNLCS,0,0,0,1ERR)
C             IF(IERR.NE.0) GO TO 805
C             CALL ACCNOD(4,IPNNOD,0,0,0,1ERR)
C             IF(IERR.NE.0) GO TO 806
C             CALL ACCELC(4,IPNELC,0,0,0,0,0,1ERR)
C             IF(IERR.NE.0) GO TO 807
C             CALL ACCMAT(4,IPNMAT,0,0,0,0,1ERR)
C             IF(IERR.NE.0) GO TO 808
C             CALL ACCEPR(4,IPNEPR,0,0,0,0,0,1ERR)

```

```
IF(IERR.NE.0) GO TO 809
CALL ACCEEN(4,IPNEEN,0,0,0,0,0,IERR)
IF(IERR.NE.0) GO TO 810
C
GO TO 820
C
C WRITE ERROR MESSAGES TO THE SCREEN
C
800 PRINT 870, IERR
GO TO 820
801 PRINT 871, IERR
GO TO 820
802 PRINT 872, IERR
GO TO 820
805 PRINT 875, IERR
GO TO 820
806 PRINT 877, IERR
GO TO 820
807 PRINT 878, IERR
GO TO 820
808 PRINT 879, IERR
GO TO 820
809 PRINT 876, IERR
GO TO 820
810 PRINT 880, IERR
GO TO 820
C
C
820 CONTINUE
C
C
857 FORMAT(13,4X,4(E16.8,4X))
858 FORMAT(1X,'PSIB=',E16.8)
859 FORMAT(1X,/,1X,'EN',6X,'SENSITIVITY 1',7X,'SENSITIVITY H',
*7X,'SENSITIVITY H',6X,'SENSITIVITY 1B')
861 FORMAT(1X,/,1X,'TOTAL=',4(E16.8,4X))
862 FORMAT(1X,'ELEMENT ',14)
870 FORMAT(1X,'ACCELM RETURNED WITH ERROR ',14)
871 FORMAT(1X,'ACCFES RETURNED WITH ERROR ',14)
872 FORMAT(1X,'ACCCND RETURNED WITH ERROR ',14)
875 FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',14)
876 FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',14)
877 FORMAT(1X,'ACCNOD RETURNED WITH ERROR ',14)
878 FORMAT(1X,'ACCELC RETURNED WITH ERROR ',14)
879 FORMAT(1X,'ACCMAT RETURNED WITH ERROR ',14)
880 FORMAT(1X,'ACCEEN RETURNED WITH ERROR ',14)
1004 FORMAT(I4)
C
C
C
RETURN
END
```

```

SUBROUTINE COMPOS(NT,I,ILCN,PSIBR)
CP*****
CP* COMPOS: CALCULATES COMPLIANCE AND SENSITIVITY FOR A BEAM
CP*
CP*****DESCRIPTION:
CP*
CP*      'COMPOS' CALCULATES THE COMPLIANCE AND THE DESIGN
CP*      SENSITIVITY FOR A 1-D BEAM IN BENDING, WITH AN
CP*      APPLIED ELEMENT FORCE IN #/IN. SELF WEIGHT IS
CP*      NEGLECTED. BEAM TORSION HAS BEEN ADDED.
CP*
CP*****C
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I       EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      ILCN    INTERNAL LOAD CASE NO.
CP*      NELM   TOTAL NO. OF ELEMENTS
CP*
CP*****C
C      INCLUDE 'AEGSIR.INC' IMPLIC.SPC'
C      INCLUDE 'AEGSIR.INC' ACCIPN.MON'
C      INCLUDE 'AEGSIR.INC' CNIL.MON'
C      INCLUDE 'AEGSIR.INC' ELEDES.MON'
C      INCLUDE 'AEGSIR.INC' SVCTR.MON'
C
C      EQUIVALENCE (NUAT(14),IP)
C
C      DIMENSION GPLW(3),PSIBR(500),DISHFF(12),X(3),Y(3),Z(3),
C      *           SHFF(12),SBUF(200),BA1N(50),CFRUF(4),ERBUF(200),
C      *           BUF(100),CD(2,6),WTW(3),C(6,2),CDL(2,6),T(3,3),
C      *           TB(6,6),COOR(3,3)
C
C      DATA GPLW/- .77459667E0, .0D0, .77459667E0/
C      DATA WTW/ .55555556E0, .88888889E0, .55555556E0/
C      DATA KT/3/,IREF/1/,MFT/1/
C
C      PSIBR(I) = 0.0
C      DFSIBG = 0.0
C      DPSIHG = 0.0
C      IF(I.GT.1) GO TO 50
C
C      GET APPLIED FORCE IN #/IN.
C
C      PRINT *, '/'
C      PRINT *, 'ENTER APPLIED FORCE IN #/IN. UNITS'
C      READ(5,1001) AF
C
C      GET APPLIED DISTRIBUTUED MOMENT
C
C      PRINT *, '/'
C      PRINT *, 'ENTER APPLIED DISTRIBUTUED MOMENT'
C      READ(5,1001) AM
C
C      GET AREA MOMENT OF INERTIA ABOUT Y-AXIS
C
50      CALL ACCEPR(2,IPNEFR,1PTAB,0,BUF,LFN,IERR)

```

```

      IF(IERR.NE.0) GO TO 809
      YI = BUF(5)
      H = 2.D0*BUF(9)
      B = 2.D0*BUF(10)
      BW(NI) = B
      BH(NT) = H
C
C     GET WEIGHT DENSITY AND MODULUS OF ELASTICITY
C
      GAMMA = 0.0D0
      E = BUF(5)
      V = BUF(7)
      G = E/(2.D0*(1.D0+V))
C
C     GET DISPLACEMENTS AT ELEMENT ENDS
C
      DO 150 J=1,NUNPE
      CALL ACCND(2,IPNCND,INFLNN(J),1,ILCN,CFBUF,LEN,IERR)
      IF(IERR.NE.0) GO TO 802
      DO 150 K=1,NDOF
      CD(J,K) = CFBUF(K)
150    CONTINUE
C
C***** EVALUATE DISPLS. AND CURVATURE AT THE GAUSS POINT USING
C     SHAPE FUNCTIONS - ONE PT. FOR CURV., THREE PT. FOR DISPL
C*****
C     GET X, Y, AND Z OF ELEMENT NODES
C
      CALL ACCELC(2,IPNELC,KINI,IREF,BUF,LEN,IERR)
      IF(IERR.NE.0) GO TO 807
      M = 1
      DO 200 J=1,9,3
      K = J+1
      L = J+2
      X(M) = BUF(J)
      Y(M) = BUF(K)
      Z(M) = BUF(L)
      M = M+1
200    CONTINUE
      DO 210 J=1,3
      COOR(1,J) = X(J)
      COOR(2,J) = Y(J)
      COOR(3,J) = Z(J)
210    CONTINUE
C
C     FORM THE ELEMENT LOCAL COORDINATE SYSTEM
C
      IN3 = INFLNN(3)
      CALL EUBTM(IN3,BE1A,COOR,T,IERR)
      CALL ZEROSP(1B,36*IF)
      DO 220 J=1,3
      DO 220 K=1,3
      TB(J,K) = T(J,K)
      TB(J+3,K+3) = T(J,K)
220    CONTINUE
      CALL UMXART(TB,CD,C,6,2,6)
      DO 230 J=1,2
      DO 230 K=1,6

```

```

          CDL(J,K) = C(K,J)
230      CONTINUE
C
C   CALCULATE ELEMENT LENGTH
C
C       DX = X(2)-X(1)
C       DY = Y(2)-Y(1)
C       DZ = Z(2)-Z(1)
C       EL = DSQRT(DX*DX+DY*DY+DZ*DZ)
C       IF(DY.EQ.0.AND.DZ.EQ.0) GO TO 236
C       DO 235 J=1,NUNPE
C           CDL(J,4) = -CDL(J,4)
235      CONTINUE
C
C   CHANGE LOCAL Y-ROTATION FROM POSITIVE TO NEGATIVE
C   IF BEAM LIES ALONG X GLOBAL AXIS
C
C       IF(DX.LT.0.001.AND.DX.GT.-0.001) GO TO 246
C       DO 240 J=1,NUNPE
C           CDL(J,5) = -CDL(J,5)
240      CONTINUE
C
246      F = -AF - GAMMA*B*XH
C
C   CALCULATE THE TWISTING ANGLE
C
C       WXY = DABS((CDL(2,4)-CDL(1,4))/EL)
C
C   EVALUATE SHAPE FUNCTIONS FOR DISPL. - THREE POINT QUADRATURE
C
C       B2 = B*B
C       B3 = B2*B
C       B4 = B3*B
C       H2 = H*H
C       H3 = H2*H
C       WRITE(10,1002) I
C       WRITE(10,1004) E,G,V
C       WRITE(10,1005) H,B
C
C       DO 300 K=1,3
C           FSI = GFLW(K)
C           CALL EU3DSB(FSI,SHPF,DDSHPF,2,EL)
C           W = (SHPF(3)*CDL(1,3)+SHPF(5)*CDL(1,5)
C                 +SHPF(9)*CDL(2,3)+SHPF(11)*CDL(2,5))
C
C   EVALUATE SHAPE FUNCTIONS FOR CURV. - THREE POINT QUADRATURE
C
C       WXX = (DDSHPF(3)*CDL(1,3)+DDSHPF(5)*CDL(1,5)
C                 +DDSHPF(9)*CDL(2,3)+DDSHPF(11)*CDL(2,5))
C       WRITE(10,860) K,W,WXX,WXY
C
C       IF(NT.GT.1) GO TO 250
C
C   CALCULATE SENSITIVITY VECTORS
C
C       PJB = H3/3.D0-.42D0*B*(H2+B4/(4.D0*H2))
C       PJH = B*H2-.42D0*B2*(H-H4/(12.D0*H3))
C       IPSIEG = IPSIEG+(-2*GAMMA*B*W-(E*H3/12)*WXX*WXX-
C                 *PJB*G*WXY*WXY)*WTW(K)*(EL/2.D0)
C       IPSIHG = IPSIHG+(-2*GAMMA*B*W-(3*E*B*H2/12)*WXX*WXX-
C                 *PJH*G*WXY*WXY)*WTW(K)*(EL/2.D0)

```

```

C
C   CALCULATE PSI(B) - INTEGRAL OF FORCE*DISPLACEMENT
C

250      PSIBB(I) = PSIBB(I) + (F*WTAM*WXY)*WTW(K)*(EL/2.10)
300      CONTINUE
         WRITE(10,1003) DPSIBG,DPSIHG
C
         IF(NT.GT.1) GO TO 820
         DPSIB(I) = DPSIBG
         DPSIH(I) = DPSIHG
C
         GO TO 820
C
C   WRITE ERROR MESSAGES TO THE SCREEN
C
802      PRINT 872, IERR
         GO TO 820
807      PRINT 878, IERR
         GO TO 820
808      PRINT 879, IERR
         GO TO 820
809      PRINT 876, IERR
         GO TO 820
C
C
820      CONTINUE
C
C
851      FORMAT(1X,'BEAM WIDTH B=',F8.5,2X,'BEAM DEPTH=',F8.5,2X
*,',E=',E9.3,2X,',IYY=',E9.3,2X,',GAMMA=',F6.5,',APPLIED FORCE
*=',F8.5)
855      FORMAT(1X,'NODE=',I2,2X,'X=',E12.5,2X,'Y=',E12.5,2X,'Z=',E12.5,2X
,',RX=',E12.5,2X,',RY=',E12.5,2X,',RZ=',E12.5)
860      FORMAT(1X,'GP=',I2,4X,'W=',E11.5,4X,'WXX=',E11.5,4X,
*',WXY=',E11.5)
870      FORMAT(1X,'ACCELM RETURNED WITH ERROR ',I4)
872      FORMAT(1X,'ACCCNL RETURNED WITH ERROR ',I4)
876      FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',I4)
878      FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
879      FORMAT(1X,'ACCMAT RETURNED WITH ERROR ',I4)
1001     FORMAT(E12.5)
1002     FORMAT(1X,'ELEMENT =',I4)
1003     FORMAT(1X,'DPSIBG=',E12.5,4X,'DPSIHG=',E12.5)
1004     FORMAT(1X,'E=',E12.5,4X,'G=',E12.5,4X,'U=',E12.5)
1005     FORMAT(1X,'HEIGHT=',E12.5,4X,'WIDTH=',E12.5)
C
C
C
         RETURN
         END

```

```

SUBROUTINE COMP11(NT,I,ILCN)
C*****
C*
C* COMP11: CALCULATES COMPLIANCE AND SENSIT. FOR PLANE STRESS
C*
C* ****
C*
C* DESCRIPTION:
C*
C*   'COMP11' CALCULATES THE COMPLIANCE AND THE DESIGN
C*   SENSITIVITY OF THE FOUR AND EIGHT NODE PLANE STRESS
C*   ELEMENT IN TRACTION WITHOUT SELFWEIGHT.
C*
C* ****
C*
C*   NI      COUNTER FOR FINITE DIFFERENCE
C*   I      EXTERNAL ELEMENT NO. BEING PROCESSED
C*   ILCN    INTERNAL LOAD CASE NO.
C*
C* ****
C
INCLUDE 'AEGSIR.INC' IMPLIC.SPC'
INCLUDE 'AEGSIR.INC' ACCIPN.MON'
INCLUDE 'AEGSIR.INC' UNTL.MON'
INCLUDE 'AEGSIR.INC' ELEIES.MON'
INCLUDE 'AEGSIR.INC' SVCTR.MON'
C
DIMENSION X(8),Y(8),Z(8),SHPF(8),GPL(2,4),DATN(50),
*           BUF(100),PSIR(2),SBUF(50),CFRUF(6),ERRUF(50),
*           DSHFGX(8),DSHFGY(8),BF(4,4B),SE(500),DSHFL(2,R),
*           SIGMA(6,4),EPSLN(6,4)
C
DATA GPL/2*-,.57735027, .57735027/-,.57735027,
*      2*.57735027,-.57735027, .57735027/
DATA KT/3/,IREF/1/
C
SE(I) = 0.
IF(NT.GT.1) GO TO 350
C
C GET ELEMENT STRESSES AND STRAINS
C
CALL ACCFES(2,IPNRES,KINT,IREF,ILCN,SBUF,LEN,IERR)
IF(IERR.NE.0) GOTO 801
LOC = LEN - 1
M = 1
DO 50 K=1,NSVAL
  SIGMA(1,K) = SRUF(M)
  SIGMA(2,K) = SBUF(M+1)
  SIGMA(3,K) = SBUF(M+3)
  M = M+4
50 CONTINUE
DO 60 K=1,NSVAL
  EPSLN(1,K) = SBUF(M)
  EPSLN(2,K) = SBUF(M+1)
  EPSLN(3,K) = SBUF(M+3)
  M = M+4
60 CONTINUE
C
C GET X AND Y FOR JACOBIAN EVALUATION
C
CALL ACCELc(2,IFNELC,KINT,IREF,BUF,LENB,IERR)

```

```

      IF(IERR.NE.0) GO TO 807
      M = 1
      DO 200 L=1,LENB,3
         J = L+1
         K = L+2
         X(M) = BUF(L)
         Y(M) = BUF(J)
         Z(M) = BUF(K)
         M = M+1
200      CONTINUE
C
C      CALCULATE FORCES AT THE GAUSS POINTS
C
      DO 250 L=1,NDOF
         DO 250 K=1,NSVAL
            BF(K,L) = 0.0
250      CONTINUE
C
C      LOOP OVER THE GAUSS POINTS
C
      DO 300 K=1,NSVAL
         PSI = GPL(1,K)
         ETA = GPL(2,K)
C
C      EVALUATE SHAPE FUNCTIONS AT THE GAUSS POINTS
C
         IF(ISTYP.EQ.2) CALL EU2DLO(PSI,ETA,K1,SHPF,DSPFL,
*                           DSHFGX,DSHFGY,DETJ,X,Y,IERR)
         IF(ISTYP.EQ.4) CALL EU2DPQ(PSI,ETA,K1,SHPF,DSPFL,
*                           DSHFGX,DSHFGY,DETJ,X,Y,IERR)
         IF(IERR.NE.0) GOTO 809
300      CONTINUE
         WRITE(10,855)
         DO 320 K=1,NSVAL
320      WRITE(10,854) K, (SIGMA(J,K),J=1,NSIG)
         WRITE(10,860)
         DO 330 K=1,NSVAL
330      WRITE(10,854) K, (EPSLN(J,K),J=1,NSIG)
         DO 340 J=1,NSIG
            DO 340 K=1,NSVAL
               SE(I) = SE(I) + SIGMA(J,K)*EPSLN(J,K)*DETJ
340      CONTINUE
C      CALCULATE SENSITIVITY VECTOR
C
         DPSIT(I) = - SE(I)
350      GO TO 820
C
C      WRITE ERROR MESSAGES TO THE SCREEN
C
801      PRINT 871, IERR
802      GO TO 820
807      PRINT 878, IERR
808      GO TO 820
809      PRINT 876, IERR
810      GO TO 820
C
C      820      CONTINUE
C

```

```
C
854  FORMAT(1X,I2,2X,3(E16.8,2X))
855  FORMAT(1X,'GP',5X,'SIGMAX(GP)',8X,'SIGMAY(GP)',8X,
*'SIGMAXY(GP)')
860  FORMAT(1X,'GP',5X,'EPSLNX(GP)',8X,'EPSLNY(GP)',8X,
*'EPSLNXY(GP)')
871  FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
876  FORMAT(1X,'EU2DFQ RETURNED WITH ERROR ',I4)
878  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
C
C
C
      RETURN
      END
```

```
SUBROUTINE CF16(NT,I,ILCN,PSIBTB)
CP*****CP*****CP*****CP*****CP*****CP*****CP*****
CP*
CP*   CP16: BRANCHES TO THE APPROPRIATE ELEMENT SUBTYPE
CP*
CP******CP*****CP*****CP*****CP*****CP*****CP*****
CP*
CP* DESCRIPTION:
CP*
CP*   'CP16' BRANCHES TO THE APPROPRIATE ELEMENT SUBTYPE
CP*   TO CALCULATE THE COMPLIANCE AND COMPLIANCE DESIGN
CP*   SENSITIVITY OF THE PLATE BENDING ELEMENT 16.
CP*   NOTE: THIS DOES NOT TAKE INTO ACCOUNT ANY MEMBRANE
CP*   STIFFNESS.
CP*
CP******CP*****CP*****CP*****CP*****CP*****CP*****
CP*
CP*   NT      COUNTER FOR FINITE DIFFERENCE
CP*   I       EXTERNAL ELEMENT NO. BEING PROCESSED
CP*   ILCN    INTERNAL LOAD CASE NO.
CP*   PSIBTB  COMPLIANCE OF A BENDING PLATE, USED FOR
CP*           CALCULATING THE FINITE DIFFERENCE
CP*
CP******CP*****CP*****CP*****CP*****CP*****CP*****
INCLUDE '[AEGSDR.INC] IMPLIC.SFC'
INCLUDE '[AEGSDR.INC] ELFDES.MON'
INCLUDE '[AEGSDR.INC] SVECTR.MON'
C
C      DIMENSION PSIBTB(500)
C
C** BRANCH TO THE APPROPRIATE ELEMENT SUBTYPE
C
C      IF(ISTYP.EQ.1)  CALL CP1601(NT,I,ILCN,PSIBTB)
C      IF(ISTYP.EQ.2)  CALL CP1602(NT,I,ILCN,PSIBTB)
C
C      RETURN
END
```

```

SUBROUTINE CP1601(NT,I,ILCN,PSIBTR)
CP*****CP1601: CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
CP*
CP* DESCRIPTION:
CP*
CP*      'CP1601' CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
CP*      FOR A TRIANGULAR BENDING ELEMENT.
CP*
CP*****CP1601: CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
CP*      FOR A TRIANGULAR BENDING ELEMENT.
CP*
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I      EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      ILCN    INTERNAL LOAD CASE NO.
CP*      PSIBTR  COMPLIANCE, USED FOR CALCULATING FINITE DIFFERENCE
CP*
CP*****CP1601: CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
C
C      INCLUDE 'AEGSIR.INC' IMPLIC.SPC'
C      INCLUDE 'AEGSIR.INC' ACCIPN.MON'
C      INCLUDE 'AEGSIR.INC' CNIL.MON'
C      INCLUDE 'AEGSIR.INC' ELEDES.MON'
C      INCLUDE 'AEGSIR.INC' SVECTR.MON'
C
C      DIMENSION X(3),Y(3),PSIB(2),SBUF(100),CPE(500),EF(3,6),
C      *          SIGMA(6),EPSLN(6),BUF(100),CFBUF(6),EQBUF(100),
C      *          PSIBTB(500),CB(3,6),Z(3)
C
C      DATA NT/3/,IREF/1/,MPT/1/
C
C      CPE(I) = 0.
C      PSIBTB(I) = 0.
C
C      GET PROPERTIES
C
C      CALL ACCEPR(2,IPNEPR,IPTAB,O,BUF,LEN,IERR)
C      IF(IERR.NE.0) GO TO 809
C      FB(NT) = BUF(25)
C      IF(NT.GT.1) GO TO 65
C
C      GET ELEMENT STRESSES AND STRAINS
C
C      CALL ACCFES(2,IPNFES,KINT,IREF,ILCN,SRUF,LEN,IERR)
C      IF(IERR.NE.0) GOTO 801
C      M = 1
C      DO 50 J=1,NDOF
C          SIGMA(J) = SBUF(J)
C 50      CONTINUE
C      M = 7
C      DO 60 J=1,NDOF
C          EPSLN(J) = SBUF(M)
C          M = M+1
C 60      CONTINUE
C
C      GET DISPLACEMENTS FOR PSI CALCULATION
C
C 65      DO 70 J=1,NUNFE
C          CALL ACCCND(2,IPNCND,INTNN(J),1,ILCN,CFBUF,LEN,IERR)

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        IF(IERR.NE.0) GO TO 802
        DO 70 K=1,NDOF
          CD(J,K) = CFBUF(K)
70      CONTINUE
C
C   GET EQUIVALENT FORCES AT THE ELEMENT NODES FOR PSI1 CALC.
C
        CALL ACCEEN(2,IPNLEN,KINT,JREF,ILCN,ERRQUF,LEN,IERR)
        IF(IERR.NE.0) GO TO 808
        M = 1
        DO 80 J=1,NUNFE
          DO 80 K=1,NDOF
            EF(J,K) = EQBUF(M)
            M = M+1
80      CONTINUE
        IF(NT.GT.1) GO TO 350
C
C   GET THE JACORIAN
C
        CALL ACCELc(2,IPNELC,KINT,IREF,BUF,LENB,IERR)
        IF(IERR.NE.0) GO TO 807
        M = 1
        DO 200 J=1,LENB,3
          X(M) = BUF(J)
          Y(M) = BUF(J+1)
          Z(M) = BUF(J+2)
          M = M+1
200     CONTINUE
        DETJ = EUTRIA(X,Y)
C
C   CALCULATE SENSITIVITY VECTOR
C
        DO 340 J=1,3
          CFE(I) = CFE(I) + SIGMA(J)*EPSLN(J)*DETJ
340     CONTINUE
        DPSITB(I) = - (CFE(I))
C
C   CALCULATE PSI(B) - INTEGRAL OF FORCE*DISPLACEMENT IN Z
C
350     DO 400 J=1,NUNFE
          PSIBTB(I) = PSIBTH(I) + EF(J,3)*CD(J,3)
400     CONTINUE
        GO TO 820
C
C   WRITE ERROR MESSAGES TO THE SCREEN
C
801     PRINT 871, IERR
        GO TO 820
802     PRINT 872, IERR
        GO TO 820
807     PRINT 877, IERR
        GO TO 820
808     PRINT 879, IERR
        GO TO 820
809     PRINT 880, IERR
        GO TO 820
C
C
820     CONTINUE
C

```

```
C  
852  FORMAT(1X,'NODE',6X,'DISP X',8X,'DISP Y',8X,'DISP '  
     *      ,8X,'ROT X',9X,'ROT Y',9X,'ROT Z')  
853  FORMAT(1X,I4,6(2X,E12.4))  
871  FORMAT(1X,'ACCFES RETURNED WITH ERROR ',J4)  
872  FORMAT(1X,'ACCNU RETURNED WITH ERROR ',J4)  
877  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',J4)  
879  FORMAT(1X,'ACCEEN RETURNED WITH ERROR ',J4)  
880  FORMAT(1X,'ACCEPK RETURNED WITH ERROR ',J4)  
C  
C  
C  
RETURN  
END
```

```

      SUBROUTINE CP1602(NF,I,ILCN,PSIBTB)
CP*****CP1602: CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
CP*
CP* DESCRIPTION:
CP*
CP*      'CP1602' CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
CP*      FOR A FOUR NODE BEAMING ELEMENT.
CP*
CP*****CP1602: CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
CP*      FOR A FOUR NODE BEAMING ELEMENT.
CP*
CP*      NF      COUNTER FOR FINITE DIFFERENCE
CP*      I       EXTERNAL NO. BEING PROCESSED
CP*      ILCN    INTERNAL LOAD CASE NO.
CP*      PSIBTB  COMPLIANCE
CP*
CP*****CP1602: CALCULATES COMPLIANCE AND DESIGN SENSITIVITY
CP*
C
C      INCLUDE 'AEGSDR.INC' IMPLIC.SPC'
C      INCLUDE 'AEGSDR.INC' ACCIFN.MON'
C      INCLUDE 'AEGSDR.INC' CNFL.MON'
C      INCLUDE 'AEGSDR.INC' ELEIES.MON'
C      INCLUDE 'AEGSDR.INC' SVECTR.MON'
C
C      DIMENSION X(4),Y(4),PSIB(2),SBUF(100),CPF(500),EF(4,6),Z(4),
C      *          SIGMA(6,4),EPSLN(6,4),BUF(100),CBUF(6),
C      *          ERBUF(100),PSIBTB(500),CD(4,6)
C
C      DATA  KT/3/,IREF/1/,MPT/1/
C
C      CPE(I) = 0.
C      PSIBTB(I) = 0.
C
C      GET PROPERTIES
C
C      CALL ACCEPR(2,IPNFR,IFTAB,0,BUF,LEN,IERR)
C      IF(IERR.NE.0) GO TO 809
C      PB(NF) = BUF(25)
C      IF(NF.GT.1) GO TO 65
C
C      GET ELEMENT STRESSES AND STRAINS
C
C      CALL ACCFES(2,IPNFES,KINI,IREF,ILCN,SBUF,LEN,IERR)
C      IF(IERR.NE.0) GO TO 801
C      M = 1
C      DO 50 K=1,NSVAL
C          J = M+1
C          L = M+2
C          SIGMA(1,K) = SBUF(M)
C          SIGMA(2,K) = SBUF(J)
C          SIGMA(3,K) = SBUF(L)
C          M = M+6
C 50      CONTINUE
C      DO 60 K=1,NSVAL
C          J = M+1
C          L = M+2
C          EPSLN(1,K) = SBUF(M)

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```

        EPSLN(2,K) = SBUF(J)
        EPSLN(3,K) = SBUF(L)
        M = M+6
60      CONTINUE
C
C   GET DISPLACEMENTS FOR PSI CALCULATION
C
65      DO 70 J=1,NUNPE
          CALL ACCCNU(2,IPNCNU,INTNN(J),1,ILCN,CFRUF,LFN,IERR)
          IF(IERR.NE.0) GO TO 802
          DO 70 K=1,NDOF
              CD(J,K) = CFRUF(K)
70      CONTINUE
C
C   GET EQUIVALENT FORCES AT THE ELEMENT NODES FOR PSI CALC.
C
          CALL ACCEEN(2,IPNEEN,KINT,IREF,ILCN,EQBUF,LEN,IERR)
          IF(IERR.NE.0) GO TO 808
          M = 1
          DO 80 J=1,NUNPE
              DO 80 K=1,NDOF
                  EF(J,K) = EQBUF(M)
                  M = M+1
80      CONTINUE
          IF(NT.GT.1) GO TO 350
C
C   GET THE JACOBIAN
C
          CALL ACCEL(2,IPNELC,KINT,IREF,BUF,LENB,IERR)
          IF(IERR.NE.0) GO TO 807
          M = 1
          DO 200 J=1,LENB,3
              X(M) = BUF(J)
              Y(M) = BUF(J+1)
              Z(M) = BUF(J+2)
              M = M+1
200     CONTINUE
          DETJ = AREAR(X,Y)
          DETJ = DETJ/4.0D0
C
C   CALCULATE SENSITIVITY VECTOR
C
          DO 340 J=1,3
              DO 340 K=1,NSVAL
                  CPE(I) = CPE(I) + SIGMA(J,K)*EPSLN(J,K)*DETJ
340     CONTINUE
          DFSITR(I) = - CPE(I)
C
C   CALCULATE PSI(B) - INTEGRAL OF FORCE*DISPLACEMENT IN Z
C
350     DO 400 J=1,NUNPE
              PSITRB(I) = PSITRB(I) + EF(J,3)*CD(J,3)
400     CONTINUE
          GO TO 820
C
C   WRITE ERROR MESSAGES TO THE SCREEN
C
801     PRINT 871, IERR
          GO TO 820
802     PRINT 872, IERR

```

```
      GO TO 820
807  PRINT 877, IERR
      GO TO 820
808  PRINT 879, IERR
      GO TO 820
809  PRINT 880, IERR
      GO TO 820
C
C
820  CONTINUE
C
C
852  FORMAT(1X,'NODE',6X,'DISP X',8X,'DISP Y',8X,'DISP '
*           ,8X,'ROT X',9X,'ROT Y',9X,'ROT Z')
853  FORMAT(1X,I4,6(2X,E12.4))
871  FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
872  FORMAT(1X,'ACCCND RETURNED WITH ERROR ',I4)
877  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
879  FORMAT(1X,'ACCEEN RETURNED WITH ERROR ',I4)
880  FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',I4)
C
C
C
      RETURN
END
```

```

      SUBROUTINE CFSI11(PSI11,I11,IREF)
C
C     INCLUDE 'IAEGSDR.INC' IMPLIC.SPC'
C     INCLUDE 'IAEGSIR.INC' ACCIN.MDN'
C     INCLUDE 'IAEGSIR.INC' LNTL.MDN'
C     INCLUDE 'IAEGSIR.INC' FLEDES.MDN'
C
C     DIMENSION DATN(50),CFBUF(6)
C
C     CALCULATE PSI(B) FOR PLATE - FORCE*DISPLACEMENT
C
C     PRINT *,' '
C     PRINT *,'ENTER NODE WHERE LOAD IS APPLIED'
C     READ(5,1004) NEXF
C     PRINT *,' '
C     PRINT *,'ENTER LOAD DIRECTION(1:X,...,6:RZ)'
C     READ(5,1004) LDIR
C
C     GET INTERNAL NODE NUMBER
C
C     CALL ACCNOD(2,IPNNOD,NEXT,2,DATN,IERR)
C     IF(IERR.NE.0) GO TO 806
C     NINT = DATN(4)
C
C     GET DISPLACEMENT AT NODE
C
C     CALL ACCCNU(2,IPNCND,NINT,IREF,IL1,CFBUF,LEN,IERR)
C     IF(IERR.NE.0) GO TO 802
C     DISP = CFBUF(LDIR)
C
C     PSI11 = 40000*DISP
C
C     WRITE ERROR MESSAGES
C
802   PRINT 872, IERR
        GO TO 820
806   PRINT 877, IERR
        GO TO 820
C
820   CONTINUE
C
C
872   FORMAT(1X,'ACCNOD RETURNED WITH ERROR ',I4)
877   FORMAT(1X,'ACCNOD RETURNED WITH ERROR ',I4)
1004  FORMAT(I4)
C
C
      RETURN
END

```

```

SUBROUTINE DISP(FSIB,NT,NELM)
CP*****
CP*
CP* DISP: BRANCHES TO THE APPROPRIATE ELEMENT TYPE FOR THE
CP*
CP*****DESCRIPTION:
CP*
CP*      'DISP' BRANCHES TO THE APPROPRIATE ELEMENT TYPE FOR
CP*      CALCULATION OF THE DISPLACEMENT CONSTRAINT AND THE
CP*      DISPLACEMENT SENSITIVITY VECTOR.
CP*
CP*****C
CP*      FSIB      DISPLACEMENT AT X
CP*      NT        COUNTER FOR FINITE DIFFERENCE
CP*      NELM     TOTAL NO. OF ELEMENTS
CP*
CP*****C
C      INCLUDE '/AEGSDR.INC' IMPLIC.SPC'
C      INCLUDE '/AEGSDR.INC' ACCIPN.MON'
C      INCLUDE '/AEGSDR.INC' CNFL.MON'
C      INCLUDE '/AEGSDR.INC' ELEFES.MON'
C      INCLUDE '/AEGSDR.INC' SVECTR.MON'
C
C      EQUIVALENCE (NDAT(97),IDBS),(NDAT(98),IDBL)
C
C      DIMENSION DATN(50),FSIB(2),CFBUF(6)
C
C      DATA IREF/1/
C
C      SDPSTB = 0.0
C      SDPSIT = 0.0
C      SDPSIB = 0.0
C      SDPSIH = 0.0
C      IF(NT.GT.1)  GO TO 10
C
C      SET ADJOINT LOAD CASE NUMBER
C
C      L2 = LCS + NC
C
C      SET ORIGINAL LOAD CASE NUMBER
C
10     L1 = 1
C
C      SETUP POINTERS
C
      CALL ACCEL(1,IPNELM, IDBS, 1, 0, IERR)
      IF(IERR.NE.0)  GO TO 800
      CALL ACCFES(1,IPNFES, IDBL, 1, L1, 0, 0, IERR)
      IF(IERR.NE.0)  GO TO 802
      CALL ACCCND(1,IPNCNU, IDBL, 1, L1, 0, 0, IERR)
      IF(IERR.NE.0)  GO TO 802
      CALL ACCNOD(1,IPNNOD, IDBS, 1, 0, IERR)
      IF(IERR.NE.0)  GO TO 806
      CALL ACCELC(1,IPNELC, IDBS, 1, 0, 0, IERR)
      IF(IERR.NE.0)  GO TO 807

```

```

      CALL ACCMAT(1,IPNMAT,IBBS,1,0,0,IERR)
      IF(IERR.NE.0) GO TO 808
      CALL ACCEPR(1,IPNEMR,IBBS,1,0,0,IERR)
      IF(IERR.NE.0) GO TO 809
C
C   LOOP THROUGH THE BUFFERS TO GET STRESSES, STRAINS ,MOMENTS,ETC.
C
C       DO 100 I=1,NELM
C
C   GET ELEMENT DESCRIPTORS
C
C       CALL ACCELM(2,IPNELM,I,JREF,IFD,IERR)
C       IF(IERR.NE.0) GO TO 800
C
C       IF(NT.GT.1) GO TO 720
C
C   BRANCH TO THE APPROPRIATE ELEMENT TYPE
C
C       IF(ITYP.EQ.11) CALL DISP11(NI,I,L1,L2,IL1)
C       IF(ITYP.EQ.5)  CALL DISP05(NI,I,L1,L2,IL1)
C       IF(ITYP.EQ.16) CALL DP16(NT,I,L1,L2,IL1)
C
C
C       SDPSIT = SDPSIT+DPSIT(I)
C       SDPSIB = SDPSIB+DPSIB(I)
C       SDPSIH = SDPSIH+DPSIH(I)
C       SDPSIB = SDPSIB+DPSIB(I)
100    CONTINUE
C
C       WRITE(10,859)
C       DO 710 I=1,NELM
710    WRITE(10,857) I,DPSIT(I),DPSIB(I),DPSIH(I),DPSITB(I)
        WRITE(10,861) SDPSIT,SDPSIB,SDPSIH,SDPSIB
C
C   CALCULATE PSI(B) - ORIGINAL DISPL AT NODE WHERE ABLT LOAD APPLIED
C
720    PRINT *, ' '
        PRINT *, 'ENTER NODE NUMBER WHERE ABLT LOAD IS APPLIED'
        READ(5,1004) NEXT
        LDIR = 3
C
C   GET INTERNAL NODE NUMBER
C
        CALL ACCNOD(2,IPNNOD,NEXT,2,DATN,IERR)
        IF(IERR.NE.0) GO TO 806
        NINT = DATN(4)
C
C   GET DISPLACEMENT AT NODE
C
        CALL ACCOND(2,IPNCND,NINT,IREF,IL1,CFBUF,LFN,IERR)
        IF(IERR.NE.0) GO TO 802
        DIS = CFBUF(LDIR)
C
        PSIB(NT) = -DIS
C
        WRITE(10,858) PSIB(NT)
        PRINT 858, PSIB(NT)
C
        IF(NT.EQ.1) GO TO 730
        WRITE(10,*)

```

```
        WRITE(10,856) NEXT
C
C C CLEAN-UP EVERYTHING
C
730  CALL ACCELM(4,IPNEIM,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 800
      CALL ACCFES(4,IPNFES,0,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 801
      CALL ACCCND(4,IPNCND,0,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 802
      IF(NT.GT.1) GO TO 750
      CALL ACCLCS(4,IPNLCS,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 803
750  CALL ACCNOD(4,IPNNOD,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 806
      CALL ACCEL(4,IPNEIC,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 807
      CALL ACCMAT(4,IPNMAT,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 808
      CALL ACCEPR(4,IPNEFR,0,0,0,IERR)
      IF(IERR.NE.0) GO TO 809
C
      GO TO 820
C
C C WRITE ERROR MESSAGES TO THE SCREEN
C
800  PRINT 870, IERR
      GO TO 820
801  PRINT 871, IERR
      GO TO 820
802  PRINT 872, IERR
      GO TO 820
805  PRINI 875, IERR
      GO TO 820
806  PRINT 877, IERR
      GO TO 820
807  PRINT 878, IERR
      GO TO 820
808  PRINT 879, IERR
      GO TO 820
809  PRINT 876, IERR
      GO TO 820
C
C
820  CONTINUE
C
C
856  FORMAT(1X,'***ADJOINT LOAD IS APPLIED AT NODE',I4)
857  FORMAT(13,4X,4(E16.8,4X))
858  FORMAT(1X,'PSIB=',E16.8)
859  FORMAT(1X,/,1X,'EN',6X,'SENSITIVITY T',7X,'SENSITIVITY H',
*7X,'SENSITIVITY H',6X,'SENSITIVITY TH')
861  FORMAT(1X,/,1X,'TOTAL=',4(E16.8,4X))
862  FORMAT(1X,'ELEMENT ',I4)
870  FORMAT(1X,'ACCELM RETURNED WITH ERROR ',I4)
871  FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
872  FORMAT(1X,'ACCCND RETURNED WITH ERROR ',I4)
875  FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)
876  FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',I4)
877  FORMAT(1X,'ACCNOD RETURNED WITH ERROR ',I4)
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```
978  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
879  FORMAT(1X,'ACCMAT RETURNED WITH ERROR ',I4)
1004 FORMAT(I4)
2000 FORMAT(A)
C
C
C
RETURN
END
```

```

SUBROUTINE DISPOS(NT,I,L1,I2,IL1)
CP*****
CP*
CP* DISPOS: CALCULATES THE DISPL. DESIGN SENSITIVITY OF A BEAM
CP*
CP*****
CP*
CP* DESCRIPTION:
CP*
CP*      'DISPOS' CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*      SENSITIVITY OF A 1-D BEAM IN BENDING, WITH AN APPLIED
CP*      ELEMENT FORCE IN #/JN. SELF WEIGHT IS NEGLECTED.
CP*      TORSION IS ACTIVE.
CP*
CP*****
CP*
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I      EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      L1     ORIGINAL EXTERNAL LOAD CASE NO.
CP*      L2     EXTERNAL ADJOINT LOAD CASE NO.
CP*      IL1    INTERNAL LOAD CASE NO. OF ORIGINAL LOAD
CP*
CP*****
C
INCLUDE 'EAEGSDR.INC' IMPL1C.SPC'
INCLUDE 'EAEGSDR.INC' ACCIPN.MON'
INCLUDE 'EAEGSDR.INC' CNTL.MON'
INCLUDE 'EAEGSDR.INC' ELEIES.MON'
INCLUDE 'EAEGSDR.INC' SVECTR.MON'
COMMON/LCSIDES/ULCS(90)

C
EQUIVALENCE (NDAT(14),IP),(NDAT(98),INBL)
DIMENSION X(3),Y(3),Z(3),IWSHF(12),DATN(50),BUF(100),
*           SHPF(12),CFRUF(6),GPLW(3),ALD(2,6),CD(2,6),WTW(3),
*           C(6,2),I(6,2),T(3,3),TB(6,6),CDL(2,6),ALDL(2,6),
*           COOR(3,3)
C
DATA GPLW/-,.77459667, .00000000, .77459667/
DATA WTW/ .555555556, .88888889, .55555556/
DATA KT/3/,IREF/1/,MPT/1/
C
DPSIBG = 0.0
DPSIHG = 0.0
IF(I.GT.1) GO TO 50
C
C REQUEST APPLIED FORCE IN LOAD/LENGTH
C
PRINT *,' '
PRINT *,'ENTER APPLIED LOAD IN [FORCE/LENGTH] '
READ(5,1001) AF
C
C GET AREA MOMENT OF INERTIA ABOUT Y-AXIS
C
50 CALL ACCEPR(2,IPNEPR,1PTAR,0,BUF,LEN,IERR)
IF(IERR.NE.0) GO TO 809
YI = BUF(5)
H = 2*BUF(9)
B = 2*BUF(10)
BH(NT) = H
BW(NI) = B
C

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```

C      GET WEIGHT DENSITY AND MODULUS OF ELASTICITY
C
C          CALL ACCMAT(2,IPNMAT,NMAT,MPT,BUF,LEN,IERR)
C          IF(IERR.NE.0) GO TO 808
C          GAMMA = 0.0D0
C          E = BUF(5)
C          V = BUF(7)
C          G = E/(2.0D0*(1.0D0+V))
C
C          IF(1.GT.1) GO TO 60
C
C      GET INTERNAL LOAD CASE NUMBER FOR ORIGINAL LOAD
C
60       CALL ACCLCS(1,IPNLCS,IDL,1,0,IERR)
C          IF(IERR.NE.0) GO TO 805
C          CALL ACCLCS(2,IPNLCS,L1,2,DLCs,IERR)
C          IF(IERR.NE.0) GO TO 805
C          IL1 = DLCs(21)
C
C      GET DISPLACEMENTS AT ELEMENT ENDS
C
C          CALL ACCCND(1,IPNCND,IDL,1,L1,0,0,IERR)
C          IF(IERR.NE.0) GO TO 802
C          DO 70 J=1,NUNPE
C              CALL ACCCND(2,IPNCND,INTNN(J),1,IL1,CBUF,LEN,IERR)
C              IF(IERR.NE.0) GO TO 802
C              DO 70 K=1,NUOF
C                  CD(J,K) = CBUF(K)
70       CONTINUE
C
C      GET INTERNAL LOAD CASE NUMBER FOR ADJOINT LOAD
C
C          CALL ACCLCS(1,IPNLCS,IDL,1,0,IERR)
C          IF(IERR.NE.0) GO TO 805
C          CALL ACCLCS(2,IPNLCS,L2,2,DLCs,IERR)
C          IF(IERR.NE.0) GO TO 805
C          ILCN = DLCs(21)
C
C      GET DISPLACEMENTS AT ELEMENT ENDS FOR ADJOINT LOAD
C
C          CALL ACCCND(1,IPNCND,IDL,1,L2,0,0,IERR)
C          IF(IERR.NE.0) GO TO 802
C          DO 100 J=1,NUNPE
C              CALL ACCCND(2,IPNCND,INTNN(J),1,ILCN,CBUF,LEN,IERR)
C              IF(IERR.NE.0) GO TO 802
C              DO 100 K=1,NUOF
C                  ALD(J,K) = CBUF(K)
100    CONTINUE
C
C***** EVALUATE DISPLS. AND CURVATURE AT THE GAUSS POINT USING
C      SHAPE FUNCTIONS - ONE PT. FOR CURV., THREE PT. FOR DISPL
C*****
C      GET X, Y, AND Z OF ELEMENT NODES
C
C          CALL ACCELc(2,IPNELC,KINT,JREF,BUF,LEN,IERR)
C          IF(IERR.NE.0) GO TO 807
C          M = 1
C          DO 200 J=1,9,3
C              K = J+1

```

```

L = J+2
X(M) = BUF(J)
Y(M) = BUF(K)
Z(M) = BUF(L)
M = M+1
200    CONTINUE
      DO 210 J=1,3
            COOR(1,J) = X(J)
            COOR(2,J) = Y(J)
            COOR(3,J) = Z(J)
210    CONTINUE
C
C FORM THE ELEMENT LOCAL COORDINATE SYSTEM FOR DISPLACEMENTS
C
      IN3 = INFINN(3)
      CALL EUBTM(IN3,BETA,COUR,1,IERR)
      CALL ZEROSP(TB,36*IP)
      DO 220 J=1,3
          DO 220 K=1,3
              TB(J,K) = T(J,K)
              TB(J+3,K+3) = T(J,K)
220    CONTINUE
      CALL UMXABT(TB,CD,C,6,2,6)
      DO 230 J=1,2
          DO 230 K=1,6
              CDL(J,K) = C(K,J)
230    CONTINUE
      CALL UMXABT(TB,ALD,B,6,2,6)
      DO 232 J=1,2
          DO 232 K=1,6
              ALDL(J,K) = D(K,J)
232    CONTINUE
C
C CALCULATE ELEMENT LENGTH
C
      DX = X(2)-X(1)
      DY = Y(2)-Y(1)
      DZ = Z(2)-Z(1)
      EL = DSQRT(DX*DX+DY*DY+DZ*DZ)
C
C CHANGE LOCAL Y-ROTATION FROM POSITIVE TO NEGATIVE IF
C BEAM LIES ALONG X GLOBAL AXIS
C
      IF(DX.LT.0.001.AND.DX.GT.-0.001) GO TO 246
      DO 240 J=1,NUMP
            CDL(J,5) = -CDL(J,5)
            ALDL(J,5) = -ALDL(J,5)
240    CONTINUE
C
246    F = -AF - GAMMA*B*B
C
C CALCULATE THE TWISTING ANGLES
C
      WXY = DABS((CDL(2,4)-CDL(1,4))/EL)
      AWXY = DARS((ALDL(2,4)-ALDL(1,4))/EL)
C
C EVALUATE SHAPE FUNCTIONS FOR DISPL. - THREE POINT QUADRATURE
C
      B2 = B*B
      B3 = B2*B
      B4 = B3*B

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```

H2 = H*XH
H3 = H2*XH
C
DO 300 K=1,3
  PSI = GPLW(K)
  CALL EU3DSB(PSI,SHPF,DDSHPF,2,EL)
  W = (SHPF(3)*CDL(1,3)+SHPF(5)*CDL(1,5)+SHPF(9)*
        * CDL(2,3)+SHPF(11)*CDL(2,5))
  AW = (SHPF(3)*ALDL(1,3)+SHPF(5)*ALDL(1,5)+SHPF(9)*
        * ALDL(2,3)+SHPF(11)*ALDL(2,5))
C
C EVALUATE SHAPE FUNCTIONS FOR CURV. - THREE POINT QUADRATURE
C
  WXX = (DDSHPF(3)*CDL(1,3)+DDSHPF(5)*CDL(1,5)+*
          * DDSHPF(9)*CDL(2,3)+DDSHPF(11)*CDL(2,5))
  AWXX = (DDSHPF(3)*ALDL(1,3)+DDSHPF(5)*ALDL(1,5)+*
          * DDSHPF(9)*ALDL(2,3)+DDSHPF(11)*ALDL(2,5))
C
C CALCULATE SENSITIVITY VECTORS
C
  PJB = H3/3.00-.42D0*B*(H+B4/(4.D0*XH))
  PJH = B*XH2-.42D0*B2*(H-B4/(12.D0*XH))
  DPSIBG = DPSIBG+(-GAMMA*XH*AW-(E*XH3/12)*AWXX*XH-
             * PJB*XH*WXY*AWXY)*WTW(K)*(EL/2.D0)
  DPSIHG = DPSIHG+(-GAMMA*B*AW-(3*E*B*XH2/12)*AWXX*XH-
             * PJH*XH*WXY*AWXY)*WTW(K)*(EI/2.D0)
300  CONTINUE
  DPSIB(I) = DPSIBG
  DPSIH(I) = DPSIHG
C
  GO TO 820
C
C WRITE ERROR MESSAGES TO THE SCREEN
C
802  PRINT 872, IERR
  GO TO 820
805  PRINT 875, IERR
  GO TO 820
807  PRINT 878, IERR
  GO TO 820
808  PRINT 879, IERR
  GO TO 820
809  PRINT 876, IERR
  GO TO 820
C
C
820  CONTINUE
C
C
851  FORMAT(1X,'BEAM WIDTH B=',F8.5,2X,'BEAM DEPTH=',F8.5,2X
      *, 'E=',E9.3,2X,'IY=',E9.3,2X,'GAMMA=',F6.5,2X,'APPLIED
      *FORCE=',F8.5)
855  FORMAT(1X,'NODE=',I2,2X,'X=',E12.5,2X,'Y=',E12.5,2X,'Z=',
      *E12.5,2X,'RX=',E12.5,2X,'RY=',E12.5,2X,'RZ=',E12.5)
860  FORMAT(1X,'GF=',I2,4X,'W=',E11.5,4X,'WXX=',E11.5,4X,'AW=',
      *E11.5,4X,'AWXY=',E11.5)
864  FORMAT(1X,'NODX=',I2,2X,'AX=',E12.5,2X,'AY=',E12.5,2X,
      *'AZ=',E12.5,2X,'ARX=',E12.5,2X,'ARY=',E12.5,2X,'ARZ=',
      *E12.5)
872  FORMAT(1X,'ACCND RETURNED WITH ERROR ',I4)
875  FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)

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876  FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',I4)
878  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
879  FORMAT(1X,'ACUMAT RETURNED WITH ERROR ',I4)
1001 FORMAT(E12.5)
C
C
      RETURN
      END
```

```

      SUBROUTINE DISP11(NT,I,L1,L2,IL1)
CP*****CALCULATES THE DISPL. SENSIT. FOR PLANE STRESS
CP*
CP*  DISPLACEMENT CONSTRAINT DESIGN
CP*  SENSITIVITY FOR THE FOUR AND EIGHT NODE PLANE STRESS
CP*  ELEMENT WITH TRACTION, SFLW WEIGHT NOT INCLUDED.
CP*
CP* DESCRIPTION:
CP*
CP*      'DISP11' CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*      SENSITIVITY FOR THE FOUR AND EIGHT NODE PLANE STRESS
CP*      ELEMENT WITH TRACTION, SFLW WEIGHT NOT INCLUDED.
CP*
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I      EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      L1     ORIGINAL EXTERNAL LOAD CASE NO.
CP*      L2     EXTERNAL ADJOINT LOAD CASE NO.
CP*      IL1    ORIGINAL INTERNAL LOAD CASE NO. RETURNED TO DISP.FOR
CP*
CP*****CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*      SENSITIVITY FOR THE FOUR AND EIGHT NODE PLANE STRESS
CP*      ELEMENT WITH TRACTION, SFLW WEIGHT NOT INCLUDED.
CP*
C
C      INCLUDE 'CAEGSDR.INC' IMPLIC.SPC'
C      INCLUDE 'CAEGSDR.INC' ACCJPN.MON'
C      INCLUDE 'CAEGSDR.INC' CNTL.MON'
C      INCLUDE 'CAEGSDR.INC' ELEDES.MON'
C      INCLUDE 'CAEGSDR.INC' SVECTR.MON'
C      COMMON/LCSLES/DLCS(90)
C
C      EQUIVALENCE (NDAT(98),IDBL)
C
C      DIMENSION SHPF(8),GPL(2,4),BUF(100),X(8),Y(8),Z(8),
C      *          DATN(50),PSJB(2),SHUF(50),DSHFGX(8),DSHFGY(8),
C      *          DSHFL(2,8),SIGMA(6,4),EPSLN(6,4),MF(4,48),SE(500)
C
C      DATA  GPL/2*-,.57735027, .57735027,-.5//35027,
C      *          2*.57735027,-.57735027, .57735027/
C      DATA  KT/3/,IREF/1/,MPT/1/
C
C      JJ = L1
C
C      GET INTERNAL LOAD CASE NUMBER
C
10   CALL ACCLCS(1,IPNLCS,IDLCS,1,0,IER)
      IF(IERR.NE.0) GO TO 805
      CALL ACCLCS(2,IFNLCS,JJ,2,IDLCS,IER)
      IF(IERR.NE.0) GO TO 805
      ILCN = DLCS(21)
C
C      SETUP POINTER FOR STRESS-STRAIN BUFFER
C
      CALL ACCFES(1,IPNFES,INRL,1,ILCN,0,0,IER)
      IF (IER.NE.0) GO TO 801
      IF(JJ.EQ.L1) IL1 = ILCN
      SE(I) = 0.0
C
C      GET ELEMENT STRESSES AND STRAINS
C
      CALL ACCFES(2,IPNFES,KINT,IREF,ILCN,SBUF,LEN,IER)
      IF(IERR.NE.0) GOTO 801

```

```

LOC = LEN - 1
M = 1
IF (JJ.EQ.L2) GO TO 55
DO 50 K=1,NSVAL
  SIGMA(1,K) = SBUF(M)
  SIGMA(2,K) = SBUF(M+1)
  SIGMA(3,K) = SBUF(M+3)
  M = M+4
50   CONTINUE
      GO TO 65
55   M = 17
      DO 60 K=1,NSVAL
        EPSLN(1,K) = SBUF(M)
        EPSLN(2,K) = SBUF(M+1)
        EPSLN(3,K) = SBUF(M+3)
        M = M+4
60   CONTINUE
65   IF (JJ.EQ.L2) GO TO 100
     JJ = L2
     GO TO 10
C
C   GET X AND Y FOR JACOBIAN EVALUATION
C
100   CALL ACCELC(2,IPNELC,KINI,JREF,RUF,LENB,IERR)
     IF(IERR.NE.0) GO TO 807
     M = 1
     DO 200 L=1,LENB,3
       X(M) = BUF(L)
       Y(M) = BUF(L+1)
       Z(M) = BUF(L+2)
       M = M+1
200   CONTINUE
C
C   CALCULATE FORCES AT THE GAUSS POINTS
C
     DO 250 L=1,NDOF
       DO 250 K=1,NSVAL
         BF(K,L) = 0.0
250   CONTINUE
C
C   LOOP OVER THE GAUSS POINTS
C
     DO 300 K=1,NSVAL
       PSI = GPL(1,K)
       ETA = GPL(2,K)
C
C   EVALUATE SHAPE FUNCTIONS AT THE GAUSS POINTS
C
       IF(ISTYP.EQ.2) CALL EU2DLQ(PSI,ETA,KT,SHPF,ISHPL,
*                         DSHPGX,DSHFGY,DETJ,X,Y,IERR)
       IF(ISTYP.EQ.4) CALL EU2DFQ(PSI,ETA,KT,SHFF,ISHPL,
*                         DSHPGX,DSHFGY,DETJ,X,Y,IERR)
       IF(IERR.NE.0) GOTO 809
300   CONTINUE
     DO 340 J=1,NSIG
       DO 340 K=1,NSVAL
         SE(I) = SE(I) + SIGMA(J,K)*EPSLN(J,K)*DETJ
340   CONTINUE
C
C   CALCULATE SENSITIVITY VECTOR
C

```

```
DPSIT(I) = - SE(I)
700  CONTINUE
C
GO TO 820
C WRITE ERROR MESSAGES TO THE SCREEN
C
801  PRINT 871, IERR
     GO TO 820
805  PRINT 875, IERR
     GO TO 820
807  PRINT 878, IERR
     GO TO 820
809  PRINT 876, IERR
     GO TO 820
C
C
820  CONTINUE
C
C
854  FORMAT(1X,I2,2X,3(E16.8,2X))
855  FORMAT(1X,'GP',5X,'SIGMAX(GP)',8X,'SIGMAY(GP)',8X,
*'SIGMAXY(GP)')
860  FORMAT(1X,'CP',5X,'EPSLNX(GP)',8X,'EPSLNY(CP)',8X,
*'EPSLNXY(GP)')
871  FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
875  FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)
876  FORMAT(1X,'E2DIPQ RETURNED WITH ERROR ',I4)
878  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
C
C
RETURN
END
```

```
SUBROUTINE DF16(NT,I,L1,L2,IL1)
CP*****CP16: BRANCHES TO THE APPROPRIATE ELEMENT SUBTYPE
CP*
CP* DESCRIPTION:
CP*
CP*      'CP16' BRANCHES TO THE APPROPRIATE ELEMENT SUBTYPE
CP*      TO CALCULATE THE DISPLACEMENT DESIGN SENSITIVITY OF
CP*      THE PLATE BENDING ELEMENT 16.
CP*      NOTE: THIS DOES NOT TAKE INTO ACCOUNT ANY MEMBRANE
CP*      STIFFNESS.
CP*
CP* NT      COUNTER FOR FINITE DIFFERENCE
CP* I       EXTERNAL ELEMENT NO. BEING PROCESSED
CP* L1     ORIGINAL EXTERNAL LOAD CASE NO.
CP* L2     EXTERNAL ADJOINT LOAD CASE NO.
CP* IL1    ORIGINAL INTERNAL LOAD CASE NO. - RETURNED VALUE
CP*
CP* INCLUDE 'AEGSDR.INC' IMPLIC.SPC'
CP* INCLUDE 'AEGSDR.INC' ELEDES.MON'
CP* INCLUDE 'AEGSDR.INC' SVCTR.MON'
C
C** BRANCH TO THE APPROPRIATE ELEMENT SUBTYPE
C
IF(ISTYP.EQ.1) CALL DF1601(NT,I,L1,L2,IL1)
IF(ISTYP.EQ.2) CALL DF1602(NT,I,L1,L2,IL1)
C
RETURN
END
```

```

SUBROUTINE DF1601(NT,I,L1,L2,IL1)
CP*****CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*
CP* DF1601: CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*
CP*****CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*
CP* DESCRIPTION:
CP*
CP*      'DF1601' CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*      SENSITIVITY VECTOR FOR A TRIANGULAR PLATE BENDING
CP*      ELEMENT.
CP*
CP*****CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I       EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      L1     ORIGINAL EXTERNAL LOAD CASE NO.
CP*      L2     EXTERNAL ADJOINT LOAD CASE NO.
CP*      IL1    ORIGINAL INTERNAL LOAD CASE NO. - RETURNED VALUE
CP*
CP*****CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
INCLUDE 'AEGSDR.INC' IMPLIC.SPC'
INCLUDE 'AEGSDR.INC' ACCIFN.MON'
INCLUDE 'AEGSDR.INC' CNTL.MON'
INCLUDE 'AEGSDR.INC' ELFDES.MON'
INCLUDE 'AEGSDR.INC' SVECTR.MON'
COMMON/LCSDES/ILCS(90)

C      EQUIVALENCE (NNAT(98),IDBL)

C      DIMENSION SIGMA(6),EPSLN(6),SBUF(100),BUF(100),CFE(500),
*           X(3),Y(3),Z(3)

C      DATA  NT/3/,IREF/1/
C
C      JJ = L1
C      CFE(I) = 0.0
C
C*** GET INTERNAL LOAD CASE NUMBER
C
10     CALL ACCLCS(1,IPNLCS,IDBL,1,0,IERR)
      IF(IERR.NE.0) GO TO 805
      CALL ACCLCS(2,IPNLCS,JJ,2,ILCS,IERR)
      IF(IERR.NE.0) GO TO 805
      ILCN = ILCS(21)

C*** GET PROPERTIES
C
      CALL ACCEPR(2,IPNEPR,IFTAB,0,BUF,LEN,IERR)
      IF(IERR.NE.0) GO TO 809
      FB(NT) = BUF(25)

C*** SETUP POINTER FOR STRESS-STRAIN BUFFER
C
      CALL ACCFES(1,IPNFES,IDL,1,ILCN,0,0,IERR)
      IF (IERR.NF.0) GO TO 801
      IF(JJ.EQ.L1) IL1 = ILCN

C*** GET ELEMENT STRESSES AND STRAINS
C

```

```

      CALL ACCFES(2,IPNFFS,KJNT,IRFF,ILCN,SBUF,LEN,IERR)
      IF(IERR.NE.0) GOTO 801
      IF (JJ.EQ.L2) GO TO 55
      DO 50 K=1,NDOF
         SIGMA(K) = SBUF(K)
50   CONTINUE
      GO TO 65
55   M = 7
      DO 60 K=1,NDOF
         EFSLN(K) = SBUF(M)
         M = M+1
60   CONTINUE
65   IF (JJ.EQ.L2) GO TO 100
      JJ = L2
      GO TO 10
C
C*** GET THE JACOBIAN
C
100    CALL ACCELC(2,IPNELC,KINT,IREF,HUF,LENR,IERR)
      IF(IERR.NE.0) GO TO 807
      M = 1
      DO 200 J=1,LENH,3
         K = J+1
         LL = J+2
         X(M) = BUF(J)
         Y(M) = BUF(K)
         Z(M) = BUF(LL)
         M = M+1
200    CONTINUE
C
      DETJ = EUTRIA(X,Y)
C
C*** CALCULATE SENSITIVITY VECTOR
C
      DO 340 J=1,3
         CPE(I) = CPE(I) + SIGMA(J)*EFSLN(J)*DETJ
340    CONTINUE
      DPSITB(I) = -CPE(I)
C
      GO TO 820
C
C*** WRITE ERROR MESSAGES TO THE SCREEN
C
801    PRINT 871, IERR
      GO TO 820
805    PRINT 875, IERR
      GO TO 820
807    PRINT 878, IERR
      GO TO 820
809    PRINT 879, IERR
      GO TO 820
C
820    CONTINUE
C
854    FORMAT(1X,I2,2X,3(E16.8,2X))
855    FORMAT(1X,'GP',5X,'SIGMAX(GP)',8X,'SIGMAY(GP)',8X,
*'SIGMAXY(GP)')
860    FORMAT(1X,'GP',5X,'EFSLNX(GP)',8X,'EPSLNY(GP)',8X,
*'EFSLNXY(GP)')
871    FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
875    FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)

```

```
878  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
879  FORMAT(1X,'ACCEFR RETURNED WITH ERROR ',I4)
C
C
RETURN
END
```

```

SUBROUTINE DF1602(NT,I,L1,I2,IL1)
CP*****
CP*
CP* DF1602: CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*
CP*****
CP*
CP* DESCRIPTION:
CP*
CP*      'DF1602' CALCULATES THE DISPLACEMENT CONSTRAINT DESIGN
CP*      SENSITIVITY VECTOR FOR A FOUR NODE PLATE BENDING
CP*      ELEMENT.
CP*
CP*****
CP*
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I      EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      L1     ORIGINAL EXTERNAL LOAD CASE NO.
CP*      L2     EXTERNAL ADJOINT LOAD CASE NO.
CP*      IL1    ORIGINAL INTERNAL LOAD CASE NO. - RETURNED VALUE
CP*
CP*****
INCLUDE 'CAEGSDR.INC' IMPLIC.SPC'
INCLUDE 'CAEGSDR.INC' ACCIPN.MON'
INCLUDE 'CAEGSDR.INC' UML.MON'
INCLUDE 'CAEGSDR.INC' ELEMFES.MON'
INCLUDE 'CAEGSDR.INC' SVECTR.MON'
COMMON/LCSDES/DLCS(90)

C      EQUIVALENCE (NDAT(98),IDBL)

C      DIMENSION SIGMA(6,4),EFSLN(6,4),SBUF(100),BUF(100),CPE(500),
*                  X(4),Y(4),Z(4)
C      DATA  KT/3/,IREF/1/
C
C      JJ = L1
C      CPE(I) = 0.0
C
C*** GET PROPERTIES
C
CALL ACCEPR(2,IPNEPR,IFTAH,0,BUF,LEN,IERR)
IF(IERR.NE.0) GO TO 809
FB(NT) = BUF(25)

C*** GET INTERNAL LOAD CASE NUMBER
C
10   CALL ACCLCS(1,IPNLCS,IDBL,1,0,IERR)
IF(IERR.NE.0) GO TO 805
CALL ACCLCS(2,IPNLCS,JJ,2,DLCS,1IERR)
IF(IERR.NE.0) GO TO 805
ILCN = DLCS(21)

C*** SETUP POINTER FOR STRESS-STRAIN BUFFER
C
CALL ACCFES(1,IPNFES,INBL,1,ILCN,0,0,IERR)
IF (IERR.NE.0) GO TO 801
IF(JJ.EQ.L1) IL1 = ILCN

C*** GET ELEMENT STRESSES AND STRAINS
C

```

```

      CALL ACCFES(2,IPNFES,KINT,IREF,ILCN,SBUF,LEN,IERR)
      IF(IERR.NE.0) GOTO 801
      M = 1
      IF (JJ.EQ.L2) GO TO 55
      DO 50 K=1,NSVAL
         J = M+1
         L = M+2
         SIGMA(1,K) = SBUF(M)
         SIGMA(2,K) = SBUF(J)
         SIGMA(3,K) = SBUF(L)
         M = M+6
50   CONTINUE
      GO TO 65
55   M = 25
      DO 60 K=1,NSVAL
         J = M+1
         L = M+2
         EPSLN(1,K) = SBUF(M)
         EPSLN(2,K) = SBUF(J)
         EPSLN(3,K) = SBUF(L)
         M = M+6
60   CONTINUE
65   IF (JJ.EQ.L2) GO TO 100
      JJ = L2
      GO TO 10
C
C*** GET THE JACOBIAN
C
100   CALL ACCELC(2,IPNELC,KINT,IREF,BUF,LENH,JERR)
      IF(IERR.NE.0) GO TO 807
      M = 1
      DO 200 J=1,LENH,3
         K = J+1
         LL = J+2
         X(M) = BUF(J)
         Y(M) = BUF(K)
         Z(M) = BUF(LL)
         M = M+1
200   CONTINUE
C
      DETJ = AREAR(X,Y)
      DETJ = DETJ/4.0D0
C
C*** CALCULATE SENSITIVITY VECTOR
C
      DO 340 J=1,3
         DO 340 K=1,NSVAL
            CFE(I) = CFE(I) + SIGMA(J,K)*EPSLN(J,K)*DETJ
340   CONTINUE
      DPSITB(I) = -CFE(I)
C
      GO TO 820
C
C*** WRITE ERROR MESSAGES TO THE SCREEN
C
801   PRINT 871, IERR
      GO TO 820
805   PRINI 875, IERR
      GO TO 820
807   PRINT 878, IERR
      GO TO 820

```

```
809 PRINT 879, IERR
GO TO 820
C
820 CONTINUE
C
854 FORMAT(1X,I2,2X,3(E16.8,2X))
855 FORMAT(1X,'GP',5X,'SIGMAX(GP)',8X,'SIGMAY(GP)',8X,
*'SIGMAXY(GP)')
860 FORMAT(1X,'GP',5X,'EPSLNX(GP)',8X,'EPSLNY(GP)',8X,
*'EPSLNXY(GP)')
871 FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
875 FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)
878 FORMAT(1X,'ACCEL0 RETURNED WITH ERROR ',I4)
879 FORMAT(1X,'ACCEFR RETURNED WITH ERROR ',I4)
C
C
RETURN
END
```

```

SUBROUTINE EU3DSB(PSI,SHPF,DDSHPF,KT,EL)
CP*****CP*****CP*****CP*****CP*****CP*****CP*****
CP*
CP* EU3DSB: BEAM SHAPE FUNCTIONS
CP*
CP* CP*****
CP* PSI      GAUSS POINT LOCATION. THE CENTER OF THE BEAM
CP* IS ZERO.
CP* SHPF     STANDARD BEAM SHAPE FUNCTIONS - RETURNED VALUE
CP* DDSHFF   SECOND DERIVATIVE OF THE SHAPE FUNCTIONS
CP*          - RETURNED VALUE
CP* KT       FLAG FOR RETURNING DDSHFF
CP*          =1 ONLY RETURN SHPF
CP*          =2 RETURN BOTH SHPF AND DDSHFF
CP* EL       ELEMENT LENGTH
CP*
CP*****CP*****CP*****CP*****CP*****CP*****CP*****
C
C      INCLUDE 'AEGSIR.INC' IMPLIC.SPC'
C
C      DIMENSION SHPF(12),DDSHFF(12)
C
C      EL2 = EL*EL
C      EL3 = EL2*EL
C      X = PSI + (EL/2)
C      X2 = XX
C      X3 = X2*XX
C
C      CALCULATE THE SHAPE FUNCTIONS
C
C      SHPF(1) = 1-X/EL
C      SHPF(2) = 1-(3*X2/EL2)+(2*X3/EL3)
C      SHPF(3) = SHPF(2)
C      SHPF(4) = SHPF(1)
C      SHPF(5) = X-(2*X2/EL)+(X3/EL2)
C      SHPF(6) = SHPF(5)
C      SHPF(7) = X/EL
C      SHPF(8) = (3*X2/EL2)-(2*X3/EL3)
C      SHPF(9) = SHPF(8)
C      SHPF(10) = SHPF(7)
C      SHPF(11) = (-X2/EL)+(X3/EL2)
C      SHPF(12) = SHPF(11)
C
C      IF(KT.EQ.1) GO TO 900
C
C      CALCULATE THE SECOND DERIVATIVE OF THE SHAPE FUNCTIONS
C
C      DDSHFF(1) = 0.0D0
C      DDSHFF(2) = (-6/EL2)+(12*X/EL3)
C      DDSHFF(3) = DDSHFF(2)
C      DDSHFF(4) = 0.0D0
C      DDSHFF(5) = (-4/EL)+(6*X/EL2)
C      DDSHFF(6) = DDSHFF(5)
C      DDSHFF(7) = 0.0D0
C      DDSHFF(8) = (6/EL2)-(12*X/EL3)
C      DDSHFF(9) = DDSHFF(8)
C      DDSHFF(10) = 0.0D0
C      DDSHFF(11) = (-2/EL)+(6*X/EL2)
C      DDSHFF(12) = DDSHFF(11)
C

```

900 CONTINUE
C
C
RETURN
END

```

SUBROUTINE GETSEN(PSIB,NT,NELM,IPNAME)
CP***** **** * **** * **** * **** * **** * **** * **** * **** * **** *
CP*
CP* GETSEN: BRANCHES TO THE APPROPRIATE CONSTRAINT TYPE.
CP*
CP* **** * **** * **** * **** * **** * **** * **** * **** * **** *
CP*
CP* DESCRIPTION:
CP*
CP*      'GETSEN' BRANCHES TO THE APPROPRIATE CONSTRAINT TYPE.
CP*      THE AVAILABLE CONSTRAINT TYPES ARE:
CP*          COMP - COMPLIANCE
CP*          DISP - DISPLACEMENT
CP*          STRESS
CP*
CP* **** * **** * **** * **** * **** * **** * **** * **** * **** *
CP*
CP*      PSIB      THE CONSTRAINT VALUE IS RETURNED FOR FINITE
CP*          DIFFERENCE EVALUATION
CP*      NT       COUNTER FOR THE FINITE DIFFERENCE
CP*      NELM     TOTAL NUMBER OF ELEMENTS IN FINITE ELEMENT
CP*          MODEL. THIS IS IN IFAD DATA BASE, AND IS
CP*          RETRIEVED WHEN DATA BASE IS OPENED.
CP*      IPNAME    NAME OF FINITE ELEMENT ANALYSIS - CHARACTER
CP*          INTERGER CONVERSION.
CP*
CP* **** * **** * **** * **** * **** * **** * **** * **** * **** *
C
C      INCLUDE 'CAEGSDR.INC' IMPLIC.SPC'
C      INCLUDE 'CAEGSDR.INC' ACCIFN.MON'
C      INCLUDE 'CAEGSDR.INC' CMIL.MON'
C      INCLUDE 'CAEGSDR.INC' ELELES.MON'
C      INCLUDE 'CAEGSDR.INC' SVECTR.MON'
C
C      COMMON /MEMORY/ IARRY(60000)
C      CHARACTER NAME$8,A$4,B$4
C
C      DIMENSION IPNAME(2),IDBPTR(4),IERDEV(2),PSIB(2)
C
C      DATA ISIZE/60000/
C
C      NT = NT+1
C
60      CALL ACCFNU(7,IPNAME,1,0,0,IERR)
         IF(IERR.NE.0) GO TO 800
C
C      OPEN THE IFAD DATABASE
C
         CALL INENTR(ISIZE,IERDEV,IPNAME,1,0,3,1STAT)
         IF (1STAT.NE.0) GO TO 810
         A = CHAR(IPNAME(1))
         B = CHAR(IPNAME(2))
         NAME = A//B
C
C      BRANCH TO THE APPROPRIATE CONSTRAINT ROUTINE
C
100     IF(ICK.EQ.1) CALL COMP(PSIB,NT,NELM)
         IF(ICK.EQ.2) CALL DISP(PSIB,NT,NELM)
         IF(ICK.EQ.3) CALL STRESS(PSIB,NT,NELM,NAME)
         GO TO 820
C

```

```
C WRITE ERROR MESSAGES TO THE SCREEN
C
800  PRINT 875, IERR
      GO TO 820
810  PRINT 876, IERR
      GO TO 820
C
C CLOSE IFAD DATABASE
C
820  CALL INEXIT(1DRPTR,IERR)
      IF(IERR.NE.0) GO TO 850
C
      GO TO 900
C
850  PRINI 877,IERR
C
900  CONTINUE
C
C FORMAT STATEMENTS
C
875  FORMAT(1X,'ACCFNU RETURNED WITH ERROR ',I4)
876  FORMAT(1X,'INENIK RETURNED WITH ERROR ',I4)
877  FORMAT(1X,'INEXIT RETURNED WITH ERROR ',I4)
1000 FORMAT(2A4)
1001 FORMAT(F8.5)
1004 FORMAT(A6)
C
C
C
RETURN
END
```

```

      SUBROUTINE LC16(X,Y,Z,XL,YL,ZL,TB)
CP***** **** * **** * **** * **** * **** * **** * **** * **** *
CP*
CP* LC16: TRANSFORMS GLOBAL COORD TO LOCAL COORD FOR '1601'
CP*
CP* ***** * **** * **** * **** * **** * **** * **** * **** *
CP*
CP* DESCRIPTION:
CP*
CP*   'LC16' TRANSFORMS THE TRIANGULAR GLOBAL COORDINATES
CP*     OF ELEMENT 1601 TO LOCAL COORDINATES
CP*
CP* ***** * **** * **** * **** * **** * **** * **** * **** *
CP*
CP*   X      GLOBAL X COORDINATE
CP*   Y      GLOBAL Y COORDINATE
CP*   Z      GLOBAL Z COORDINATE
CP*   XL     LOCAL X COORDINATE
CP*   YL     LOCAL Y COORDINATE
CP*   ZL     LOCAL Z COORDINATE
CP*   TB     TRANSFORMATION MATRIX
CP*
CP* ***** * **** * **** * **** * **** * **** * **** * **** *
C
C       INCLUDE 'DAEGSDR.INC' IMPLIC.SPC'
C       INCLUDE 'DAEGSDR.INC' ACCIPN.MDN'
C       INCLUDE 'DAEGSDR.INC' ELEIDES.MDN'
C
C       DIMENSION X(3),Y(3),Z(3),TB(6,6),COORL(3,3),XL(3),YL(3),
C       *           ZL(3),COOR(3,3),V12(3),V13(3),VN(3),T(3,3)
C
C       CHARACTER STYPE*4
C
C       DATA IREF/1/,ITYPE/1/
C
C*** INITIALIZE VARIABLES
C
C
      DO 40 I=1,3
        COOR(1,I) = X(I)
        COOR(2,I) = Y(I)
        COOR(3,I) = Z(I)
40    CONTINUE
C
C*** GET THE VECTORS PARALLEL TO THE 1-2 AND 1-3 SIDES
C
C       CALL UMVEC(COOR(1,1),COOR(1,2),V12,IERR)
C       CALL UMVEC(COOR(1,1),COOR(1,3),V13,IERR)
C
C       OBTAIN NORMAL V12 X V13
C
C       CALL UMVCRS(V12,V13,VN,0,IERR)
C
C       OBTAIN LOCAL TRANSFORMATION MATRIX T10
C
C       CALL EUTSCS(VN,T,IERR)
C
C       OBTAIN THE NODAL TRANSFORMATION MATRIX AS AN ASSEMBLAGE OF ETJ
C
C
      DO 50 K=1,3
        DO 50 J=1,3

```

```
        TB(J,K) = T(J,K)
        TB(J+3,K+3) = T(J,K)
50    CONTINUE
C
C   GET LOCAL COORDINATES
C
        CALL UMXATB(1,COOR,COORL,3,3,3)
        DO 60 I=1,3
            XL(I) = COORL(1,I)
            YL(I) = COORL(2,I)
            ZL(I) = COORL(3,I)
60    CONTINUE
C
        RETURN
END
```

```

SUBROUTINE SRST05(ILCN)
CP*****SRST05: CALCULATES THE ADJOINT LOAD FOR THE BEAM ELEMENT
CP*
CP* SRST05: CALCULATES THE ADJOINT LOAD FOR THE BEAM ELEMENT
CP*
CP* *****SRST05: CALCULATES THE ADJOINT LOAD FOR PENDING
CP* DESCRIPTION:
CP*
CP*      'SRST05' CALCULATES THE ADJOINT LOAD FOR PENDING
CP*      STRESS IN A 1-DIMENSIONAL BEAM
CP*      ELEMENT AND CREATES A RESTART FILE SO THAT A RESTART
CP*      OF THE FINITE ELEMENT MODEL CAN BE MADE.  THE
CP*      RESULTING DISPLACEMENTS CAN THEN BE USED TO CALCULATE
CP*      THE STRESS CONSTRAINT DESIGN SENSITIVITY.
CP***** THIS ROUTINE ONLY WORKS FOR BEAMS LYING IN THE
CP*      X-GLOBAL OR Y-GLOBAL PLAN.
CP*
CP* *****ILCN      INTERNAL LOAD CASE NO. (IF ORIGINAL LOAD
CP*
CP*****C
C      INCLUDE 'CAEGSDR.INC] IMPLIC.SPC'
INCLUDE 'CAEGSDR.INC] ACCIPN.MON'
INCLUDE 'CAEGSDR.INC] CNTL.MON'
INCLUDE 'CAEGSDR.INC] ELEDES.MON'
INCLUDE 'CAEGSDR.INC] SVCTR.MON'
C
C      DIMENSION X(2),Y(2),Z(2),DRSHFF(12),DATN(50),BUF(100),
*           SHFF(12),CBUF(6),GPLW(3),AL(12),CD(2,6),WTW(3),
*           IDIR(2),AL(12)
C
C      DATA GPLW/- .774596669241483D0, .0D0,
*           .774596669241483D0/
C      DATA WTW/ .5555555555555556D0, .088888888888889D0,
*           .5555555555555556D0/
C      DATA KT/3/,IREF/1/,MFT/1/
C
C      INITIALIZE VARIABLES
C
C      ND = NDOF*NUNPE
DO 10 J=1,ND
    AL(J) = 0.0
10  CONTINUE
C
C      GET DEPTH AND WIDTH OF THE BEAM
C
CALL ACCEPR(2,IPNEPR,IPTAR,O,BUF,LEN,IERR)
IF(IERR.NE.0) GO TO 809
H = 2*BUF(9)
B = 2*BUF(10)
C
C      GET MODULUS OF ELASTICITY
C
CALL ACCMAT(2,IPNMAT,NMAT,MFT,BUF,LEN,IERR)
IF(IERR.NE.0) GO TO 808
E = BUF(5)
C
C      GET X, Y, AND Z OF ELEMENT NODES

```

```

C
      CALL ACCELC(2,IPNELC,KINT,IREF,BUF,IEN,IERR)
      IF(IERR.NE.0) GO TO 807
      M = 1
      DO 200 J=1,6,3
      K = J+1
      L = J+2
      X(M) = BUF(J)
      Y(M) = BUF(K)
      Z(M) = BUF(L)
      M = M+1
200    CONTINUE
C
C   CALCULATE ELEMENT LENGTH
C
      DX = X(2)-X(1)
      DY = Y(2)-Y(1)
      DZ = Z(2)-Z(1)
      EL = DSQRT(DX*DX+DY*DY+DZ*DZ)
C
      XMP = 1.0D/EL
C
      DO 300 K=1,3
      PSI = GPLW(K)
      CALL EU3DSB(PSI,SHPF,DDSHPF,2,EL)
C
C   CALCULATE ADJOINT LOAD
C
      ALGP(3) = -.5D0*H*XMP*DDSHPF(3)
      ALGP(9) = -.5D0*H*XMP*DDSHPF(9)
      IF(DX.EQ.0.AND.DZ.EQ.0) GO TO 250
      ALGP(4) = 0.0D0
      ALGP(5) = -.5D0*H*XMP*DDSHPF(5)
      ALGP(10) = 0.0D0
      ALGP(11) = -.5D0*H*XMP*DDSHPF(11)
      GO TO 255
250    ALGP(4) = -.5D0*H*XMP*DDSHPF(5)
      ALGP(5) = 0.0D0
      ALGP(10) = -.5D0*H*XMP*DDSHPF(11)
      ALGP(11) = 0.0D0
C
C   SUM ADJOINT LOAD OVER GAUSS POINTS
C
255    DO 260 J=1,ND
      AL(J) = AL(J) + ALGP(J)
260    CONTINUE
300    CONTINUE
C
      N = -1
      DO 400 J=1,NUNFE
      DO 350 K=1,NDOF
      IF(AL(K+J+N).EQ.0.0) GO TO 350
      WRITE(11,864) IEXTNN(J),K,AL(K+J+N)
350    CONTINUE
      N = N+5
400    CONTINUE
C
C
      GO TO 820
C
C   WRITE ERROR MESSAGES TO THE SCREEN

```

```
C
802 PRINT 872, IERR
GO TO 820
807 PRINT 878, IERR
GO TO 820
808 PRINT 879, IERR
GO TO 820
809 PRINT 876, IERR
GO TO 820
C
C
820 CONTINUE
C
C
860 FORMAT(1X,'GF=',I2,4X,'W=',F11.5,4X,'WXX=',E11.5,4X,'AH=',
*E11.5,4X,'AWXX=',E11.5)
864 FORMAT(2(I4,2X),E16.4)
872 FORMAT(1X,'ACCCND RETURNED WITH ERROR ',I4)
876 FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',I4)
878 FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
879 FORMAT(1X,'ACCMAT RETURNED WITH ERROR ',I4)
1001 FORMAT(E12.5)
C
C
C
RETURN
END
```

```

      SUBROUTINE SRST11(ILCN,IE)
CP*****SRST11: CALCULATES THE ADJOINT LOAD FOR THE PLANE STRESS EL.
CP*
CP* SRST11: CALCULATES THE ADJOINT LOAD FOR THE PLANE STRESS EL.
CP*
CP* DESCRIPTION:
CP*
CP*      'SRST11' CALCULATES THE ADJOINT LOADS FOR A FOUR AND
CP*      EIGHT NODE PLANE STRESS ELEMENT AND THEN CREATES A
CP*      RESTART FILE SO THAT THE FINITE ELEMENT MODEL CAN BE
CP*      RESTARTED SO THAT THE RESULTING STRESSES AND STRAINS
CP*      CAN BE THEN USED TO CALCULATE THE STRESS CONSTRAINT
CP*      DESIGN SENSITIVITY.
CP*
CP*****INTERNAL LOAD CASE NO. OF ORIGINAL LOAD
CP* IE      EXTERNAL ELEMENT NO. CONSTRAINED
CP*
CP*****INCLUDE 'AEGSDR.INC' IMPLIC.SPC'
C INCLUDE 'AEGSDR.INC' ACCIPN.MON'
C INCLUDE 'AEGSDR.JNC' UNIL.MON'
C INCLUDE 'AEGSDR.INC' ELEDES.MON'
C INCLUDE 'AEGSDR.INC' SVECTR.MON'
C
C      DIMENSION SHPF(8),GPL(2,4),SBUF(50),BUF(100),
C      *          DSHPGX(8),USHPGY(8),DSHPL(2,8),X(8),Y(8),Z(8),
C      *          DG(3),ALGF(16),AL(16),E(3,3),U(9),C(3),B(3,16),
C      *          EMT(1)
C
C      DATA  GPL/2*-57735027, .57735027,-.57735027,
C      *          2* .57735027,-.57735027, .57735027/
C      DATA  KT/3/,IREF/1/,MPT/1/,ITYPE/1/
C
C** INITIALIZE VARIABLES
C
C      ND = NUNPE*NUOF
C      DO 10 J=1,ND
C      10  AL(J) = 0.
C          IF(IE.GT.1) GO TO 15
C
C** GET X AND Y FOR JACOBIAN EVALUATION
C
C      15  CALL ACCELC(2,IPNELL,KINT,IREF,XUF,LFNR,IERR)
C          IF(IERR.NE.0) GO TO 807
C          M = 1
C          DO 20 L=1,LENB,3
C              J = L+1
C              K = L+2
C              X(M) = BUF(L)
C              Y(M) = BUF(J)
C              Z(M) = BUF(K)
C              M = M+1
C
C      20  CONTINUE
C          AREA = AREAQ(X,Y)
C          XMP = 1.00/AREA
C

```

```

C** CALCULATE ADJOINT LOAD
C
C*** LOOP OVER GAUSS POINTS
C
    IC = 0
    M = 1
    DO 80 KK=1,NSVAL
        J = M+1
        L = M+3
C
C*** GET DERIVATIVES OF STRESS FUNCTION C
C
C*** VON MISES: C=(SIGX**2+SIGY**2-SIGX*SIGY+3*SIGXY**2)**.5
C
    IF(IC.GT.0) GO TO 25
    CALL ACCFES(2,IPNFES,KINT,IREF,ILCN,SBUF,LEN,IERR)
    IF(IERR.NE.0) GO TO 801
25   IF(IST.EQ.1) GO TO 30
    VMS = (SBUF(M)**2+SBUF(J)**2-SBUF(M)*SBUF(J)+3*
*           SBUF(L)**2)**.5
    DG(1) = .5*(2*SBUF(M)-SBUF(J))/VMS
    DG(2) = .5*(2*SBUF(J)-SBUF(M))/VMS
    DG(3) = (3*SBUF(L))/VMS
    GO TO 40
C
C*** PRINCIPAL STRESS
C
30   TMAX = ((.5*(SBUF(M)-SBUF(J))**2+SBUF(L)**2)**.5
    DG(1) = .5+.25*(SBUF(M)-SBUF(J))*(1/TMAX)
    DG(2) = .5-.25*(SBUF(M)-SBUF(J))*(1/TMAX)
    DG(3) = SBUF(L)*(1/TMAX)
C
40   M = M+4
    IC = IC+1
    PSI = GPL(1,KK)
    ETA = GPL(2,KK)
    IF(ISTYP.EQ.2) CALL EU2DLQ(PSI,FTA,KT,SHFF,ISHPL,
*                         DSHFGX,DSHFGY,NETJ,X,Y,IERR)
    * IF(ISTYP.EQ.4) CALL EU2DPQ(PSI,ETA,KT,SHFF,ISHPL,
*                         DSHFGX,DSHFGY,NETJ,X,Y,IERR)
    IF(IERR.NE.0) GO TO 809
C
C*** GET ELASTICITY MATRIX E
C
    CALL EU2ISS(D,TMF,EMT,NMAT,ITYMA1,ITYPE)
    N = 1
    DO 50 JJ=1,3
        LL = N+1
        LLL = N+2
        E(JJ,1) = D(N)
        E(JJ,2) = D(LL)
        E(JJ,3) = D(LLL)
        N = N+3
50   CONTINUE
C
C*** GET STRAIN-DISPLACEMENT MATRIX R
C
    CALL SD11(B,DSHFGX,DSHFGY,NUNPE)
C
C*** CALCULATE [DG]*[E]*[B]*MP
C

```

```
      CALL UMXAB(DG,E,C,1,3,3)
      CALL UMXAB(C,B,ALGP,1,NJ,3)
      DO 60 JJ=1,NJ
      60      ALGP(JJ) = ALGP(JJ)*XMP
C
C*** SUM ADJOINT LOAD OVER GAUSS POINTS (INTEGRATE OVR ELEM)
C
      DO 70 JJ=1,NJ
      70      AL(JJ) = AL(JJ)+ALGP(JJ)*DETJ
      80      CONTINUE
C
C** WRITE ADJOINT LOAD TO RESTART FILE
C
      N = -1
      DO 95 J=1,NUNPE
      DO 90 K=1,NUDF
          WRITE(11,2004) JEXNN(J),K,AL(K+J+N)
      90      CONTINUE
      N = N+1
      95      CONTINUE
C
      GO TO 820
C     WRITE ERROR MESSAGES TO THE SCREEN
C
      801  PRINT 871, IERR
          GO TO 820
      807  PRINT 878, IERR
          GO TO 820
      809  PRINT 876, IERR
          GO TO 820
C
C
      820  CONTINUE
C
C
      871  FORMAT(1X,'ACCFES RETURNED WITH ERROR ',(4)
      876  FORMAT(1X,'SHAPE FUNCTION ROUTINE RETURNED WITH ERROR ',
*14)
      878  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',(4)
      2001  FORMAT(A)
      2004  FORMAT(1X,I4,1X,I2,1X,E16.9)
C
C
      RETURN
      END
```

```

SUBROUTINE SRST16(ILCN,IE)
CP*****SRST16(ILCN,IE)*****
CP*
CP* SRST16: CALCULATES THE ADJOINT LOADS FOR A TRI. BENDING EL.
CP*
CP*****SRST16(ILCN,IE)*****
CP*
CP* DESCRIPTION:
CP*
CP* 'SRST16' CALCULATES THE ADJOINT LOADS FOR A TRIANGULAR
CP* PLATE BENDING ELEMENT AND CREATES A RESTART FILE SO
CP* THAT THE FINITE ELEMENT MODEL CAN BE RESTARTED. THE
CP* RESULTING STRESSES AND STRAINS ARE THEN USED IN THE
CP* STRESS CONSTRAINT DESIGN SENSITIVITY CALCULATION IN
CP* THE 'ST1601' SUBROUTINE. STRESS TYPES 1=PRINCIPAL
CP* 2 = VON MISES
CP*
CP*****SRST16(ILCN,IE)*****
CP*
CP* ILCN INTERNAL LOAD CASE NO. OF THE ORIGINAL LOAD
CP* IE EXTERNAL CONSTRAINED ELEMENT NO.
CP*
CP*****SRST16(ILCN,IE)*****
C
      INCLUDE 'CAEGSIR.INC] IMPLIC.SPC'
      INCLUDE 'CAEGSIR.INC] ACCIPN.MON'
      INCLUDE 'CAEGSIR.INC] CNIL.MON'
      INCLUDE 'CAEGSIR.INC] ELEFES.MON'
      INCLUDE 'CAEGSIR.INC] SVECTR.MON'
C
      DIMENSION X(3),Y(3),Z(3),BUF(50),AL(18),SBUF(50),JG(3),
      *          CG(3),XL(3),YL(3),ZL(3),C(3),I(9),EM(27),E(3,3),
      *          TB(6,6),SIG(3,3),ALM(18)
C
      DATA IREF/1/,ITYFE/1/
C
      DO 10 J=1,18
         AL(J) = 0.0D0
10     CONTINUE
C
C** GET X, Y AND Z
C
15     CALL ACCELC(2,IPNEIC,KINI,IREF,BUF,LENB,IERR)
      IF(IERR.NE.0) GO TO 807
      M = 1
      DO 20 L=1,LENB,3
         J = L+1
         K = L+2
         X(M) = BUF(L)
         Y(M) = BUF(J)
         Z(M) = BUF(K)
         M = M+1
20     CONTINUE
C
C** GET LOCAL COORDINATE SYSTEM
C
      CALL LC16(X,Y,Z,XL,YL,ZL,18)
C
C* GET ELASTICITY MATRIX [E]
C

```

```

      CALL EU2ISS(D,1MP,EMT,NMAT,ITYMAT,ITYPE)
      N=1
      DO 25 JJ=1,3
         E(JJ,1) = D(N)
         E(JJ,2) = D(N+1)
         E(JJ,3) = D(N+2)
         N = N+3
25     CONTINUE
C
C   GET THE THICKNESS OF THE PLATE
C
      CALL ACCEPR(2,IPNEMR,JFTAR,0,BUF,LEN,IERR)
      IF(IERR.NE.0) GO TO 809
      THK = BUF(25)
C
C** GET STRESSES AT THE MINSIDE NODES OF TRIANGLE
C
      CALL SSMU16(XL,YL,ILCN,SIG)
C
C** CALCULATE THE ADJOINT LOAD WHERE Q=[DG]*[E]*[B]*MP*T/2
C** AL(18) = (TAREA/3)*(Q(0,.5,.5)+Q(.5,0,.5)+Q(.5,.5,0)
C
      TAREA = EUTRIA(X,Y)
      DO 80 IT=1,3
C
C*** CALCULATE [DG] THE DERIVATIVE VECTOR
C
      IF(IST.EQ.1) GO TO 30
C
C*** VON MISES: G=SQRT(SIGX**2+SIGY**2-SIGX*SICY+3*SIGXY**2)
C
      VMS = DSQRT(SIG(IT,1)**2+SIG(IT,2)**2-SIG(IT,1)*SIG(IT,2)+3*
      *          SIG(IT,3)**2)
      DG(1) = .5D0*(2.D0*SIG(IT,1)-SIG(IT,2))/VMS
      DG(2) = .5D0*(2.D0*SIG(IT,2)-SIG(IT,1))/VMS
      DG(3) = (3.D0*SIG(IT,3))/VMS
      GO TO 40
C
C** PRINCIPAL STRESS
C
30     TMAX = DSQRT((.5D0*(SIG(IT,1)-SIG(IT,2))**2+SIG(IT,3)**2)
      DG(1) = .5D0+.25D0*(SIG(IT,1)-SIG(IT,2))/TMAX
      DG(2) = .5D0-.25D0*(SIG(IT,1)-SIG(IT,2))/TMAX
      DG(3) = SIG(IT,3)/TMAX
C
C*** CALCULATE [C] = [DG] * [E]
C
40     CALL UMXAR(LG,E,C,1,3,3)
C
C*** CALCULATE [AL] = [C] * [B] * T/2 * XMP
C
      CALL AL_16(XL,YL,C,ALM,18,THK,IT)
      DO 50 K=1,18
         AL(K) = AL(K) + (TAREA/3.0D0)*ALM(K)
50     CONTINUE
80     CONTINUE
C
C** WRITE ADJOINT LOAD TO RESTART FILE
C
      N = -1
      DO 95 J=1,NUNFE

```

```
DO 90 K=1,NDOF
  IF(AL(K+J+N).EQ.0.0D0) GO TO 90
  WRITE(11,2004) IEXTNN(J),K,AL(K+J+N)
90      CONTINUE
      N = N+5
95      CONTINUE
C
      GO TO 820
C  WRITE ERROR MESSAGES TO THE SCREEN
C
801    PRINT 871, IERR
      GO TO 820
807    PRINT 878, IERR
      GO TO 820
809    PRINI 879, IERR
      GO TO 820
C
C
820    CONTINUE
C
C
871    FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
878    FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
879    FORMAT(1X,'ACCEPK RETURNED WITH ERROR ',I4)
2001   FORMAT(A)
2002   FORMAT(1X,I4,2X,'DISP= ',E16.9)
2004   FORMAT(1X,I4,1X,I2,1X,E16.9)
C
C
      RETURN
      END
```

```

SUBROUTINE SSMD16(X,Y,ILCN,SIG)
CP*****CALCULATES STRESSES AT THE MIDSIDE NODES OF A TRI.
CP*
CP* SSMD16: CALCULATES STRESSES AT THE MIDSIDE NODES OF A TRI.
CP*
CP*****CALCULATES STRESSES AT THE MIDSIDE NODES OF
CP* TRIANGLE 1601. [SIG] = [EJ]*[B]*[DIS]*T/2 IS THE
CP* FINITE ELEMENT FORMULA FOR CALCULATING THE STRESS.
CP* THE STRAIN-DISPLACEMENT MATRIX [B] IS LOCATED IN
CP* COLUMNS 4,5, AND 6 OF THE [W] MATRIX. [EJ] IS THE
CP* ELASTICITY MATRIX, 3X3 FOR ISOTROPIC MATERIAL, AND
CP* [DIS] IS THE DISPLACEMENT VECTOR, WHERE THE DISPLS.
CP* ARE TAKEN AT THE NODES OF THE TRIANGLE. BECAUSE
CP* IFAD CALCULATES THE STRESS RESULTANTS, THE T/2 TERM
CP* MUST BE INCLUDED IN THIS CALCULATION.
CP*
CP*****CALCULATES STRESSES AT THE MIDSIDE NODES OF
CP* X      THE LOCAL ELEMENT X COORDINATE
CP* Y      THE LOCAL ELEMENT Y COORDINATE
CP* ILCN   THE INTERNAL LOAD CASE NUMBER FOR THE ORIGINAL
CP*        ORIGINAL MODEL
CP* SIG    THE MIDSIDE NODE STRESSES - RETURNED VALUE
CP*
CP*****CALCULATES STRESSES AT THE MIDSIDE NODES OF
C
C     INCLUDE 'AEGSDR.INC' IMPLIC.SPC'
INCLUDE 'AEGSDR.INC' ACCIPN.MON'
INCLUDE 'AEGSDR.INC' CNFL.MON'
INCLUDE 'AEGSDR.INC' ELDES.MON'
C
C     EQUIVALENCE (NDAT(14),1FR)
C
C     DIMENSION X(3),Y(3),GPTS(3,3),W(18,7),CFBUF(7),CD(3,7),
*             DIS(9),D(9),E(3,3),EMT(27),RUF(100),ER(3,9),
*             SIG(3,3),XL(6),YL(6)
C
C     DATA GPTS/0.0D0,.5D0,.5D0, .5D0,0.0D0,.5D0, .5D0,.5D0,0.0D0/
C     DATA ITYPE/1/
C
C** GET DISPLACEMENTS
C
DO 10 J=1,NUNPE
  CALL ACCCN(2,IFNCNB,INTNN(J),1,ILCN,CFBUF,LEN,IERR)
  IF(IERR.NE.0) GO TO 802
  DO 10 K=1,LEN
    CD(J,K) = CFBUF(K)
10  CONTINUE
M = 1
DO 20 J=1,NUNPE
  DIS(M) = CD(J,3)
  DIS(M+1) = CD(J,4)
  DIS(M+2) = CD(J,5)
  M = M+3
20  CONTINUE
C
C** GET ELASTICITY MATRIX

```

```

C
      CALL EU2DSS(D,TMP,EMT,NMAT,11YMAT,ITYPE)
      N = 1
      DO 30 JJ=1,3
         E(JJ,1) = D(N)
         E(JJ,2) = D(N+1)
         E(JJ,3) = D(N+2)
         N = N+3
30     CONTINUE
C
C** GET MATERIAL THICKNESS
C
      CALL ACCEPR(2,IPNEPR,IFTAB,0,BUF,LEN,IERR)
      IF(IERR.NE.0) GO TO 809
      THK = BUF(25)
C
C** GET LOCAL X AND Y COORDINATES
C
      CALL MOVESF(XL,X,3*IPR)
      CALL MOVESF(YL,Y,3*IPR)
C
C** CALCULATE STRESSES AT THE MIDSIDE NODES
C
      DO 100 INT=1,3
C
C*** GET SHAPE FUNCTION AT MIDSIDE NODE
C
      CALL SF1501(XL,YL,GPTS(1,INT),W,EB)
C
C*** [SIG] = [E]*[B]*[DIS]*T/2
C
      DO 50 M=1,9
         DO 50 K=1,3
            GASH = 0.0D0
            DO 40 J=1,3
               GASH = GASH + E(K,J)*W(M,J+3)
40     CONTINUE
            EB(K,M) = GASH
50     CONTINUE
      DO 60 I1 = 1,3
         SIG(INI,I1) = 0.0D0
         DO 60 M2 = 1,9
            SIG(INI,I1) = SIG(INI,I1)+EB(I1,M2)*WIS(M2)
60     CONTINUE
      DO 70 I2=1,3
         SIG(INT,I2) = SIG(INT,I2)*THK/2.0D0
70     CONTINUE
100    CONTINUE
      GO TO 820
C
C
C** WRITE ERROR MESSAGES TO THE SCREEN
C
802    PRINT 872, IERR
        GO TO 820
809    PRINT 879, IERR
        GO TO 820
C
C
820    CONTINUE
C

```

```
C  
872  FORMAT(1X,'ACCCNU RETURNED WITH ERROR ',)4)  
879  FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',)4)  
C  
C  
      RETURN  
      END
```

```

      SUBROUTINE SNMD16(X,Y,ILCN,EPN)
CP*****S* S* S*
CP*
CP* SNMD16: CALCULATES STRAINS AT THE MIDSIDE NODES OF A TRI.
CP*
CP* *****S* S* S*
CP*
CP* DESCRIPTION:
CP*
CP*      'SNMD16' CALCULATES STRAINSES AT THE MIDSIDE NODES OF
CP*      TRIANGLE 1601.  THE FORMULAS FOR STRAIN ARE:
CP*
CP*          EX = 1/E*(SIGX-V*SIGY)
CP*          EY = 1/E*(SIGY-V*SIGX)
CP*          EXY = SIGXY/G
CP*
CP* *****S* S* S*
CP*
CP*      X      THE LOCAL ELEMENT X COORDINATE
CP*      Y      THE LOCAL ELEMENT Y COORDINATE
CP*      ILCN    THE INTERNAL LOAD CASE NUMBER FOR THE ADJOINT
CP*              LOAD
CP*      EPN     THE MIDSIDE NODE STRAINS - RETURNED VALUE
CP*
CP* *****S* S* S*
C
C      INCLUDE 'AEGSIR.INC' IMPLIC.SPC'
C      INCLUDE 'AEGSIR.INC' ACCIPN.MON'
C      INCLUDE 'AEGSIR.INC' CNTL.MON'
C      INCLUDE 'AEGSIR.INC' ELEDES.MON'
C
C      DIMENSION X(3),Y(3),GP1S(3,3),W(18,7),CFBUF(7),LD(3,7),
C      *           DIS(9),EM1(27),BUF(100),EPN(3,3),SIG(3,3)
C
C      DATA MPT/1/
C
C** GET CONSTANTS
C
C      CALL ACCMAT(2,IPNMAT,NMAT,MPT,BUF,LEN,IERR)
C      IF(IERR.NE.0) GO TO 808
C      E = BUF(5)
C      V = BUF(7)
C      G = E/(2.D0*(1.D0+V))
C
C** GET STRESSES AT THE MIDSIDE NODES
C
C      CALL SSMD16(X,Y,ILCN,STC)
C
C** CALCULATE STRAINS AT THE MIDSIDE NODES
C
C      DO 100 IT=1,3
C          EPN(IT,1) = 1/E*(SIG(IT,1)-V*SIG(IT,2))
C          EPN(IT,2) = 1/E*(SIG(IT,2)-V*SIG(IT,1))
C          EPN(IT,3) = SIG(IT,3)/G
100    CONTINUE
C
C      GO TO 820
C
C
C** WRITE ERROR MESSAGES TO THE SCREEN
C

```

```
808 PRINT 878, IERRR
GO TO 820
C
C
820 CONTINUE
C
C
878 FORMAT(1X,'ACCMAT RETURNED WITH ERROR ',14)
C
C
RETURN
END
```

```

SUBROUTINE STRES05(NT,I,L,PSIBB)
CP***** ****
CP*
CP* STRES05: CALC. STRESS CONSTRAINT AND SENSIT. FOR A BEAM
CP*
CP* ****
CP*
CP* DESCRIPTION:
CP*
CP*      'STRES05' CALCULATES THE STRESS CONSTRAINT AND THE
CP*      DESIGN SENSITIVITY FOR THE 1-D BEAM ELEMENT IN
CP*      BENDING. INCLUDES TORSION.
CP*
CP***** ****
CP*
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I      EXTERNAL ELEMNT NO. FOR ELEMENT BEING PROCESSED
CP*      L      LOAD CASES - EXTERNAL
CP*      PSIBB  STRESS CONSTRAINT - RETURNED VALUE
CP*
CP***** ****
C
INCLUDE 'CAEGSDR.INC] IMPLIC.SPC'
INCLUDE 'CAEGSDR.INC] ACCIPN.MON'
INCLUDE 'CAEGSDR.INC] CNL.MON'
INCLUDE 'CAEGSDR.INC] ELEDES.MON'
INCLUDE 'CAEGSDR.INC] SVLCTR.MON'
COMMON/LCSIDES/DLCS(90)
C
EQUIVALENCE (NDAT(14),IP),(NDAT(98),IREBL)
C
DIMENSION X(3),Y(3),Z(3),DDSHFF(12),IATN(50),I(2),BUF(100),
*           SHFF(12),CFBUF(6),GPLW(3),AI(2,6),CD(2,6),WTW(3),
*           PSIBB(500),C(6,2),D(6,2),T(3,3),TB(6,6),CDL(2,6),
*           ALDL(2,6),CUOR(3,3)
C
DATA GPLW/- .7745966692414183D0, .0D0,
*           .7745966692414183D0/
DATA WTW/ .5555555555555556D0, .8888888888888889D0,
*           .5555555555555556D0/
DATA KT/3/,IREF/1/,MPT/1/
C
DPSIRG = 0.0D0
DPSIHG = 0.0D0
PSIBB(I) = 0.0D0
IF(I.GT.1) GO TO 50
C
C GET AREA MOMENT OF INERTIA AROUND Y-AXIS
C
50  CALL ACCEPR(2,IPNEPR,IFTAB,0,BUF,LEN,IERR)
IF(IERR.NE.0) GO TO 809
YI = BUF(5)
H = 2*BUF(9)
B = 2*BUF(10)
BH(NT) = H
BW(NT) = B
C
C GET WEIGHT DENSITY AND MODULUS OF ELASTICITY
C
CALL ACCMAT(2,IFNMAT,NMAT,MPT,RUF,LEN,IERR)
IF(IERR.NE.0) GO TO 808

```

```

      GAMMA = 0.0D0
      E = 30500000.0D0
      V = .3D0
      G = E/(2.0D0*(1.0D0+V))

C   GET INTERNAL LOAD CASE NUMBER FOR ORIGINAL LOAD
C
60    CALL ACCLCS(1,IPNLCS,IDL,1,0,IERR)
      IF(IERR.NE.0) GO TO 805
      CALL ACCLCS(2,IPNLCS,L(1),2,DLCS,IERR)
      IF(IERR.NE.0) GO TO 805
      IL1 = DLCS(21)

C   GET DISPLACEMENTS AT ELEMENT ENDS
C
      DO 70 J=1,NUNPE
         CALL ACCCN(2,IPNCND,INTNN(J),1,IL1,CFBUF,LEN,IERR)
         IF(IERR.NE.0) GO TO 802
         DO 70 K=1,NDOF
            CD(J,K) = CFBUF(K)
70    CONTINUE

C   BYPASS ADJOINT LOAD CALCULATION
C
      IF(NT.GT.1) GO TO 150

C   GET INTERNAL LOAD CASE NUMBER FOR ADJOINT LOAD
C
      CALL ACCLCS(1,IPNLCS,IDL,1,0,IERR)
      IF(IERR.NE.0) GO TO 805
      CALL ACCLCS(2,IPNLCS,L(2),2,DLCS,IERR)
      IF(IERR.NE.0) GO TO 805
      ILCN = DLCS(21)

C   GET DISPLACEMENTS AT ELEMENT ENDS FOR ADJOINT LOAD
C
      CALL ACCCN(1,IPNCND,IDL,1,ILCN,0,0,IERR)
      IF(IERR.NE.0) GO TO 802
      DO 100 J=1,NUNPE
         CALL ACCCN(2,IPNCND,INTNN(J),1,ILCN,CFBUF,LEN,IERR)
         IF(IERR.NE.0) GO TO 802
         DO 100 K=1,NDOF
            ALD(J,K) = CFBUF(K)
100   CONTINUE

C **** EVALUATE DISPLS. AND CURVATURE AT THE GAUSS POINT USING
C **** SHAPE FUNCTIONS - ONE PT. FOR CURV., THREE PT. FOR DISPL
C ****

C   GET X, Y, AND Z OF ELEMENT NODES
C
150   CALL ACCELC(2,IPNELC,KINT,IREF,BUF,LEN,IERR)
      IF(IERR.NE.0) GO TO 807
      M = 1
      DO 200 J=1,9,3
         K = J+1
         LL = J+2
         X(M) = BUF(J)
         Y(M) = BUF(K)
         Z(M) = BUF(LL)

```

```

      M = M+1
200    CONTINUE
      DO 210 J=1,3
         COOR(1,J) = X(J)
         COOR(2,J) = Y(J)
         COOR(3,J) = Z(J)
210    CONTINUE
C
C   FORM THE ELEMENT LOCAL COORDINATE SYSTEM FOR DISPLACEMENTS
C
      IN3 = INTNN(3)
      / CALL EURTM(IN3,BETA,COOR,T,IERR)
      CALL ZEROSP(1B,36*IP)
      DO 220 J=1,3
         DO 220 K=1,3
            TB(J,K) = T(J,K)
            TB(J+3,K+3) = TB(J,K)
220    CONTINUE
      CALL UMXART(1B,CD,C,6,2,6)
      CALL UMXABT(TB,ALD,D,6,2,6)
      DO 230 J=1,2
         DO 230 K=1,6
            CDL(J,K) = C(K,J)
            ALDL(J,K) = D(K,J)
230    CONTINUE
C
C   CALCULATE ELEMENT LENGTH
C
      DX = X(2)-X(1)
      DY = Y(2)-Y(1)
      DZ = Z(2)-Z(1)
      EL = DSQRT(DX*DX+DY*DY+DZ*DZ)
C
C   CHANGE LOCAL Y-ROTATION FROM POSITIVE TO NEGATIVE IF
C   BEAM LIES ALONG THE X GLOBAL AXIS
C
      IF(DX.LT.0.001.AND.DX.GT.-0.001) GO TO 245
      DO 240 J=1,NUMPE
         CDL(J,4) = -CDL(J,4)
         CDL(J,5) = -CDL(J,5)
         ALDL(J,3) = -ALDL(J,3)
240    CONTINUE
C
C   CALCULATE THE TWISTING ANGLES
C
245    WXY = DABS((CDL(2,4)-CDL(1,4))/EL)
      AWWY = DARS((ALDL(2,4)-ALDL(1,4))/EL)
C
C   EVALUATE SHAPE FUNCTIONS FOR NISPL. - THREE POINT QUADRATURE
C
      B2 = B*B
      B3 = B2*B
      B4 = B2*B2
      H2 = H*H
      H3 = H2*H
C
      DO 300 K=1,3
         FSI = GPLW(K)
         CALL EU3DSB(FSI,SHFF,DDSHFF,2,EL)
         W = (SHFF(3)*CDL(1,3)+SHFF(5)*CDL(1,5)+SHFF(9)*
*              CDL(2,3)+SHFF(11)*CDL(2,5))

```

```

      AW = (SHPF(3)*ALDL(1,3)+SHPF(5)*ALDL(1,5)+SHPF(9)*
      *          ALDL(2,3)+SHPF(11)*ALDL(2,5))
C
C EVALUATE SHAPE FUNCTIONS FOR CURV. - THREE POINT QUADRATURE
C
      WXX = (DDSHPF(3)*CBL(1,3)+DDSHPF(5)*CBL(1,5)+*
      *          DDSHPF(9)*CBL(2,3)+DDSHPF(11)*CBL(2,5))
      ANXX = (DDSHPF(3)*ALDL(1,3)+DDSHPF(5)*ALDL(1,5)+*
      *          DDSHPF(9)*ALDL(2,3)+DDSHPF(11)*ALDL(2,5))
C
C CALCULATE SENSITIVITY VECTORS
C
      XMP = 1.00/EL
      IF(NT.GT.1) GO TO 250
      STERM = .500*XMP*E*WXX
      PJB = H3/3.00-.4200*B*(H2+B4/(4.00*H2))
      PJH = B*H2-.4200*B2*(H-B4/(12.00*H3))
      DPSIBG = DPSIBG+(-GAMMA*B*AW-(E*H3/12.00)*AWXX*WXX-
      *          PJB*G*WXY*AWXY)*WTW(K)*(EL/2.00)
      IF(I.NE.ICE(NC)) GO TO 247
      DPSIHG = DPSIHG+(-GAMMA*B*AW-(3.00*E*B*H2/12.00)*AWXX*WXX-
      *          -STERM-PJH*G*WXY*AWXY)*WTW(K)*(EL/2.00)
      GO TO 250
247   DPSIHG = DPSIHG+(-GAMMA*B*AW-(3.00*E*B*H2/12.00)*AWXX-
      *          *WXX-PJH*G*WXY*AWXY)*WTW(K)*(EL/2.00)
C
250   IF(I.NE.ICE(NC)) GO TO 300
C
C CALCULATE PSI(B) - INTEGRAL OF STRESS FUNCTION FOR ELEMENT
C
      STRESS = -.500*H*E*WXX*XMP
      PSIBB(I) = PSIBB(I) + STRESS*WTW(K)*(EL/2.00)
300   CONTINUE
      IF(NT.GT.1) GO TO 820
      DPSIB(I) = DPSIBG
      DPSIH(I) = DPSIHG
C
      GO TO 820
C
C WRITE ERROR MESSAGES TO THE SCREEN
C
802   PRINT 872, IERR
      GO TO 820
805   PRINT 875, IERR
      GO TO 820
807   PRINT 878, IERR
      GO TO 820
808   PRINT 879, IERR
      GO TO 820
809   PRINT 876, IERR
      GO TO 820
C
C
820   CONTINUE
C
C
850   FORMAT(1X,'***ADJOINT LOAD IS APPLIED AT ELEMENT',I4)
851   FORMAT(1X,'BEAM WIDTH B=',F8.5,2X,'BEAM DEPTH=',F8.5,2X
      *,E='',E9.3,2X,'IYY=',E9.3,2X,'GAMMA=',F6.5,'APPLIED FORCE
      *=',F8.5)
855   FORMAT(1X,'NODE=',I2,2X,'X=',E12.5,2X,'Y=',E12.5,2X,'Z=',

```

```
*E12.5,2X,'RX=',E12.5,2X,'RY=',E12.5,2X,'RZ=',E12.5)
860  FORMAT(1X,'GP=',I2,4X,'W=',E11.5,4X,'WXX=',E11.5,4X,'AH=',
*E11.5,4X,'AWXX=',E11.5)
864  FORMAT(1X,'NODE=',I2,2X,'AX=',E12.5,2X,'AY=',E12.5,2X,
*'AZ=',E12.5,2X,'ARX=',E12.5,2X,'ARY=',E12.5,2X,'ARZ=',,
*E12.5)
872  FORMAT(1X,'ACCCND RETURNED WITH ERROR ',I4)
875  FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)
876  FORMAT(1X,'ACCEPR RETURNED WITH ERROR ',I4)
878  FORMAT(1X,'ACCELIC RETURNED WITH ERROR ',I4)
879  FORMAT(1X,'ACCMAT RETURNED WITH ERROR ',I4)
1001 FORMAT(E12.5)
1004 FORMAT(I4)
C
C
      RETURN
END
```

```

SUBROUTINE STRES11(NI,I,L,PSIBT)
CP*****STRES11: CALC. STRESS CONSTRAINT AND SENSIT. - PLANE STRESS
CP*
CP* DESCRIPTION:
CP*
CP*      'STRES11' CALCULATES THE STRESS CONSTRAINT AND THE
CP*      DESIGN SENSITIVITY FOR A FOUR OR AND EIGHT NODAL PLANE
CP*      STRESS ELEMENT WITH TRACTION, SELF WEIGHT NOT INCLUDED
CP*
CP*****COUNTER FOR FINITE DIFFERENCE
CP*      I      EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      L      EXTERNAL LOAD CASE NOS.
CP*      PSIBT. STRESS CONSTRAINT
CP*
CP*****C
C      INCLUDE 'CAEGSIR.INC] IMPLIC.SPC'
INCLUDE 'CAEGSIR.INC] ACCIPN.MON'
INCLUDE 'CAEGSIR.INC] CNTL.MON'
INCLUDE 'CAEGSIR.INC] ELEDES.MON'
INCLUDE 'CAEGSIR.INC] SVECTR.MON'
COMMON/LCSIDES/DLCS(90)
C
C      EQUIVALENCE (NDAT(98),IDBL)
C
C      DIMENSION X(8),Y(8),Z(8),SHFF(8),GPL(2,4),L(2),ILCN(2),
*          DATN(50),BUF(100),PSIBT(500),SBUF(50),CFBUF(6),
*          BF(4,48),EMI(1),ISHFGX(8),EQBUF(50),ISHFGY(8),
*          DSHPL(2,8),SIGMA(6,4),EPSLN(6,4),R(3,16),SE(500),
*          DG(3),ALGF(16),AL(16),E(3,3),I(9),C(3),PSIBPE(500)
CHARACTER YESNO*1
C
C      DATA    GPL/2*-57735027, .57735027,-.57735027,
*              2*.57735027,-.57735027, .57735027/
DATA    KT/3/,IREF/1/,MFT/1/,ITYPE/1/
C
C      SE(I) = 0.0
FSIBPE(I) = 0.0
IF(I.NE.1) GO TO 100
10     DO 50 JJ=1,2
C
C      GET INTERNAL LOAD CASE NUMBER
C
120    CALL ACCLCS(1,IPNL(1),IDBL,1,0,IERR)
IF(IERR.NE.0) GO TO 805
CALL ACCLCS(2,IPNLCS,L(JJ),2,DLC,1,IERR)
IF(IERR.NE.0) GO TO 805
ILCN(JJ) = DLC(21)
50     CONTINUE
C
C      SETUP POINTER FOR STRESS-STRAIN BUFFER
C
100    DO 165 JJ=1,2
CALL ACCFES(1,IPNFES,IDL,1,ILCN(JJ),0,0,IERR)

```

```

      IF (IERR.NE.0) GO TO 801
C   GET ELEMENT STRESSES AND STRAINS
C
      CALL ACCFES(2,IPNFES,KINT,IREF,ILCN(JJ),SBUF,LEN,IERR)
      IF(IERR.NE.0) GOTO 801
      M = 1
      IF (JJ.EQ.2) GO TO 140
      DO 130 K=1,NSVAL
         J = M+1
         LL = M+3
         SIGMA(1,K) = SBUF(M)
         SIGMA(2,K) = SBUF(J)
         SIGMA(3,K) = SBUF(LL)
         M = M+4
130     CONTINUE
      GO TO 160
140     M = 17
      DO 150 K=1,NSVAL
         J = M+1
         LL = M+3
         EPSLN(1,K) = SBUF(M)
         EPSLN(2,K) = SBUF(J)
         EPSLN(3,K) = SBUF(LL)
         M = M+4
150     CONTINUE
160     IF (JJ.EQ.2) GO TO 170
     IF(NT.GT.1) GO TO 170
165     CONTINUE
C   GET X AND Y FOR JACOBIAN EVALUATION
C
170     CALL ACCELC(2,IPNELC,KINT,IREF,BUF,LENB,IERR)
      IF(IERR.NE.0) GO TO 802
      M = 1
      DO 200 J=1,LENB,3
         K = J+1
         LL = J+2
         X(M) = BUF(J)
         Y(M) = BUF(K)
         Z(M) = BUF(LL)
         M = M+1
200     CONTINUE
      AREA = AREAQ(X,Y)
      XMF = 1.0/AREA
C   CALCULATE FORCES AT THE GAUSS POINTS
C
      DO 250 J=1,NDOF
         DO 250 K=1,NSVAL
            BF(K,J) = 0.0
250     CONTINUE
C   LOOP OVER THE GAUSS POINTS
C
      DO 300 K=1,NSVAL
         PSI = CPL(1,K)
         ETA = CPL(2,K)
C   EVALUATE SHAPE FUNCTIONS AT THE GAUSS POINTS
C

```

```

      IF(ISTYP.EQ.2) CALL EU2DLQ(PSI,ETA,K1,SHFF,DSHFL,
*                         DSHFGX,DSHFGY,DETJ,X,Y,IERR)
*                         IF(ISTYP.EQ.4) CALL EU2DPR(PSI,ETA,K1,SHFF,DSHFL,
*                         DSHFGX,DSHFGY,DETJ,X,Y,IERR)
*                         IF(IERR.NE.0) GOTO 809
300   CONTINUE
      WRITE(10,855)
      DO 320 K=1,NSVAL
320   WRITE(10,854) K, (SIGMA(J,K),J=1,NSIG)
      IF(NT.GT.1) GO TO 345
      WRITE(10,860)
      DO 330 K=1,NSVAL
330   WRITE(10,854) K, (EPSLN(J,K),J=1,NSIG)
      DO 340 J=1,NSIG
      DO 340 K=1,NSVAL
         SE(I) = SF(I) + SIGMA(J,K)*EPSLN(J,K)*DETJ
340   CONTINUE
C
C   CALCULATE SENSITIVITY VECTOR
C
      DPSIT(I) = - SE(I)
C
345   IF(I.NE.ICE(NC)) GO TO 820
C
C* CALCULATE PSI(B) - INTEGRAL OF STRESS FUNCTION C FOR ELEMENT
C
      IF(IST.EQ.1) GO TO 360
      DO 350 K=1,NSVAL
      VMS = (SIGMA(1,K)**2+SIGMA(2,K)**2-SIGMA(1,K)*
*                         SIGMA(2,K)+3*SIGMA(3,K)**2)**.5
350   PSIBPE(I) = PSIBPE(I) + VMS*DETJ
      GO TO 380
360   DO 370 K=1,NSVAL
      TMAX = ((.5*(SIGMA(1,K)-SIGMA(2,K)))**2+SIGMA(3,K)**2)
*                         **.5
370   PSIBPE(I) = PSIBPE(I)+(.5*(SIGMA(1,K)+SIGMA(2,K))+TMAX)
*                         *DETJ
380   PSIBT(I) = PSIBPE(I)*XMP
C
C
      GO TO 820
C   WRITE ERROR MESSAGES TO THE SCREEN
C
800   PRINT 870, IERR
      GO TO 820
801   PRINT 871, IERR
      GO TO 820
805   PRINT 875, IERR
      GO TO 820
807   PRINT 878, IERR
      GO TO 820
809   PRINT 876, IERR
      GO TO 820
C
C
820   CONTINUE
C
C
850   FORMAT(1X,'***ADJOINT LOAD IS APPLIED AT ELEMENT',14)
851   FORMAT(1X,'TYPE OF STRESS IS ',A4)
854   FORMAT(1X,12,2X,3(E16.8,2X))

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```
855  FORMAT(1X,'GF',5X,'SIGMAX(GF)',8X,'SIGMAY(GF)',8X,
*'SIGMAXY(GF)')
860  FORMAT(1X,'GF',5X,'EPSLNX(GF)',8X,'EPSLNY(GF)',8X,
*'EPSLNXY(GF)')
870  FORMAT(1X,'ACCELM RETURNED WITH ERROR ',I4)
871  FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
875  FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)
876  FORMAT(1X,'EU2DPU RETURNED WITH ERROR ',I4)
878  FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
1004 FORMAT(I4)
2001 FORMAT(A4)
C
      RETURN
END
```

```

SUBROUTINE ST1601(NT,I,L,FSIBTR)
CP*****
CP*
CP* ST1601: DESIGN SENSITIVITY VECTOR FOR A BENDING PLATE
CP*
CP*****
CP*
CP* DESCRIPTION:
CP*
CP*      'ST1601' COMPUTES THE DESIGN SENSITIVITY VECTOR FOR
CP*      A TRIANGULAR BENDING PLATE ELEMENT.
CP*
CP*****
CP*
CP*      NT      COUNTER FOR FINITE DIFFERENCE
CP*      I      EXTERNAL ELEMENT NO. BEING PROCESSED
CP*      L      EXTERNAL LOAD CASE NOS.
CP*      FSIBTR  STRESS CONSTRAINT FOR BENDING PLATE
CP*
CP*****
INCLUDE 'DAEGSDR.INC' IMPLIC.SPC'
INCLUDE 'DAEGSDR.INC' ACCIFN.MON'
INCLUDE 'DAEGSDR.INC' CNTL.MON'
INCLUDE 'DAEGSDR.INC' ELFDES.MON'
INCLUDE 'DAEGSDR.INC' SVECTR.MON'
COMMON/LCSIDES/DLCS(90)

C      EQUIVALENCE (NIAT(98),IDBL)

C      DIMENSION X(3),Y(3),Z(3),SIG(3,3),EPN(3,3),L(2),ILCN(2),
*                  SE(500),BUF(100),FSIBTR(500),SBUF(50),FSIBFE(500)

C      DATA  KT/3/,1REF/1/,MPI/1/,ITYPE/1/

C
C      SE(I) = 0.0D0
C      FSIBTR(I) = 0.0D0
C      FSIBFE(I) = 0.0D0
C
20    DO 50 JJ=1,2
C      GET INTERNAL LOAD CASE NUMBER
C
C      CALL ACCLCS(1,IPNLCS,IDBL,1,0,IERR)
C      IF(IERR.NE.0) GO TO 805
C      CALL ACCLCS(2,IPNLCS,L(JJ),2,DLCS,IERR)
C      IF(IERR.NE.0) GO TO 805
C      ILCN(JJ) = DLCS(21)

C      GET PROPERTIES
C
C      CALL ACCEPR(2,IPNEPR,IPTAB,0,BUF,LEN,IERR)
C      IF (IERR.NE.0) GO TO 809
C      PB(NT)=BUF(25)
C      IF(NT.GT.1) GO TO 100
50    CONTINUE
C      GET X AND Y FOR JACOBIAN EVALUATION
C
100   CALL ACCELIC(2,IPNELC,KINT,IREF,BUF,LEN,IERR)
      IF(IERR.NE.0) GO TO 807

```

```

M = 1
DO 110 J=1,LENB,3
  K = J+1
  LL = J+2
  X(M) = BUF(J)
  Y(M) = BUF(K)
  Z(M) = BUF(LL)
  M = M+1
110  CONTINUE
C
C     GET STRESSES FROM ORIGINAL LOAD CASE
C
C         CALL SSMD16(X,Y,ILCN(1),SIG)
C         IF(NT.GT.1) GO TO 120
C
C     GET STRAINS FROM ADJOINT LOAD
C
C         CALL SNMD16(X,Y,ILCN(2),EPN)
C
120  AREA = EUTRIA(X,Y)
      XMP = 1.00/AREA
C
C     START INTEGRATION LOOP
C
      DO 400 IT=1,3
C
        VMS = DSQRT(SIG(IT,1)**2+SIG(IT,2)**2-SIG(IT,1)*SIG(IT,2)
*           +3*SIG(IT,3)**2)
        TMAX = DSQRT((.5*(SIG(IT,1)-SIG(IT,2))**2+SIG(IT,3)**2)
        IF(NT.GT.1) GO TO 345
        IF (I.NE.1:NC) GO TO 320
        IF (IST.EQ.1) GO TO 300
        IF (IST.GT.2) GO TO 320
C
C     CALCULATE VON MISES STRESS SENSITIVITY TERM
C
        SE(I)=SE(I)+(AREA/3.00)*VMS*XMP/PB(N)
        GO TO 320
C
C     CALCULATE PRINCIPAL STRESS SENSITIVITY TERM
C
300  SE(I)=SE(I)+(AREA/3.00)*(.500*(SIG(IT,1)+SIG(IT,2)+2
*           *TMAX))*XMP/PB(N)
C
C     CALCULATE THE SENSITIVITY VECTOR
C
320  DO 340 J=1,3
      SE(I) = SE(I) - (AREA/3.00)*SIG(IT,J)*EPN(IT,J)
340  CONTINUE
      PSIBTB(I) = SE(I)
C
345  IF(I.NE.1:NC) GO TO 400
C
C* CALCULATE PSI(B) - INTEGRAL OF STRESS FUNCTION G FOR ELEMENT
C
      IF(IST.EQ.1) GO TO 360
      PSIBTB(I) = PSIBTB(I) + (AREA/3.00)*VMS*XMP
      GO TO 400
360  PSIBTB(I) = PSIBTB(I)+(AREA/3.00)*( .5*(SIG(IT,1)+SIG(IT,2))
*           +TMAX)*XMP
400  CONTINUE

```

```
C
C          GO TO 820
C  WRITE ERROR MESSAGES TO THE SCREEN
C
800    PRINT 870, IERR
        GO TO 820
801    PRINT 871, IERR
        GO TO 820
805    PRINT 875, IERR
        GO TO 820
807    PRINT 878, IERR
        GO TO 820
809    PRINT 876, IERR
        GO TO 820
C
C
820    CONTINUE
C
C
850    FORMAT(1X,'***ADJOINT LOAD IS APPLIED AT ELEMENT',I4)
851    FORMAT(1X,'***TYPE OF STRESS IS ',A4)
854    FORMAT(1X,12.2X,3(E16.8,2X))
855    FORMAT(1X,'GP',5X,'SIGMAX(GP)',8X,'SIGMAY(GP)',8X,
*'SIGMAXY(GP)')
860    FORMAT(1X,'CP',5X,'EPSLNX(GP)',8X,'EPSLNY(CP)',8X,
*'EPSLNXY(GP)')
862    FORMAT(1X,'ELEMENTI ',I4)
870    FORMAT(1X,'ACCELM RETURNED WITH ERROR ',I4)
871    FORMAT(1X,'ACCFES RETURNED WITH ERROR ',I4)
875    FORMAT(1X,'ACCLCS RETURNED WITH ERROR ',I4)
876    FORMAT(1X,'ACCEFR RETURNED WITH ERROR ',I4)
878    FORMAT(1X,'ACCELC RETURNED WITH ERROR ',I4)
1004   FORMAT(I4)
2001   FORMAT(A4)
C
        RETURN
        END
```

```

C
C ELEMENT ATTRIBUTES COMMON
C
COMMON/ELEIDES/ IED(50),INFN(32),IEXTNN(32),IBLR(4),IAF(32)
EQUIVALENCE (IED(1),ITYP)      , (IED(2),ISTYP)      , (IED(3),NUNFE),
*          (IED(4),NDOF)      , (IED(5),MAXDOF)    , (IED(6),NUELL),
*          (IED(7),ILUMP)     , (IED(8),IACTU)     ,
*          (IED(9),NRFT)     , (IED(10),NFXT)     ,
*          (IED(11),KINT)     , (IED(12),KNEXT)   , (IED(13),KLIN),
*          (IED(14),IESM)     , (IED(15),NINT)     , (IED(16),INCDPT),
*          (IED(17),ISDP)     , (IED(18),IROUN)   , (IED(19),NOC),
*          (IED(20),IMATP)    , (IED(21),IMATC)   , (IED(22),MREL),
*          (IED(23),NUMREL)   , (IED(24),NMAT)    , (IED(27),IPTRAR),
*          (IED(28),ISFTAB)   , (IED(29),BETA)    ,
*          (IED(31),NSVAL)   , (IED(32),NSIG)    , (IED(43),NSIG)

COMMON/SVECTR/ DPSIT(500),DPSIR(500),DPSIH(500),DPSITB(500),
*          TM(2),BW(2),RH(2),FB(2),ICT,ISAC,LCS,NIC,NC,
*          IST,ICE(200)

C
C*** CURRENT IPNT POINTER STORAGE FOR ACCESS ROUTINE CALLS
C
COMMON/ACCIPM/IPNFLM(2),IPNNOD(2),IPNNEC(2),IPNEMM(2),IPNEMM(2),
*          IPNEDK(2),IPNELC(2),IPNENH(2),IPNBER   ,IPNMAT  ,
*          IPNNCF(2),IPNAFL(3),IPNEEN(2),IPNAND(2),IPNEFR(2),
*          IPNNSF(2),IPNBME(2),IPNFEFS(2),IPNLCS(2),IPNSTK  ,
*          IPNRES   ,IPNASD   ,IPNCLP(2),IPNEFR   ,IPNMPK  ,
*          IPNLMI(2),IPNBLK   ,IPNCND(2),IPNNDF(2),IPNSGM(2),
*          IPNNRF   ,IPNTEM   ,IPNISS(2),IPNSTH

C
C*** GLOBAL CONTROL PARAMETERS
C
COMMON /CNIL/ NETY(200),NWAT(300),NLINE,NWID4,NWID1,NAUX,
*          IHEAUR(132),IAUX(33,5)

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